

Utilizing Swelling Force to Decrease the Ice Adhesion Strength

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Abstract

The phase transformation that occurs during water freezing process is accompanied by volume expansion and the release of latent heat. The swelling force generated by this phase transformation can have a harmful impact on structural safety and integrity, as it can lead to bursting in roads, water pipes and reservoir dams. So, why not effectively adopt the swelling force as the active de-icing power to diminish the stability of the contact interface. This paper proposes a new method to remove this accumulated ice by using polymethyl methacrylate (pmma) and 6061 aluminum alloy with pits as substrate materials. Pits were filled with solutions of different freezing points; owing to the different freezing point between the pit solution and water, their phase transformations occurred at different time, where the solutions in the pit would freeze more slowly than the surface water. The generated phase swelling force directly acted on the contact interface and decreased the stability of the interface to decrease the

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23 ice adhesion strength. The experimental results showed that the ice adhesion strength
24 was obviously affected and reduced by the swelling force in contrast to the ice adhesion
25 strength on the smooth sample, and the reduction in ice adhesion strength changed
26 depending on the filling solution. Compared to the ice adhesion strength of the
27 specimen without pits, the frozen ice was completely separated from the ice-pmma
28 interface owing to the water filling the pit. The ice adhesion strength on the surface of
29 the aluminum alloy sample filled with 10% ethanol solution was reduced by 81.42%.
30 Utilizing the phase swelling force to reduce the adhesion strength enhances the active
31 de-icing ability of the material, providing a novel method for developing new anti-icing
32 methods.

33 **Keywords:** De-icing; Phase transformation; Swelling force; Phase change time
34 difference; Ice adhesion strength; Contact interface

35

36 **1. Introduction**

37

38 Ice adhesion on exposed surfaces is considered as a potential hazard in many
39 engineering fields including in aircraft, wind turbines, power lines, high speed trains
40 and other industrial areas ([Bewilogua et al., 2009](#); [Carriveau et al., 2012](#); [Cucchiella et](#)
41 [al., 2012](#); [Caliskan et al., 2013](#); [Zhang et al., 2015](#)). It is well known that ice adhesion
42 can also degrade the operational reliability and durability of equipment, even posing a
43 great hazard to people's lives and causing the socio-economic loss. Serious examples
44 include the 2008 ice storm in southern China, and the 1998 ice storm in northeast North
45 America ([Ruan et al., 2016](#); [Petrenko et al., 2011](#); [Stone et al., 2008](#)).

46 Conditions such as these have prompted researchers and engineers to develop
47 practical and economical anti-icing or de-icing methods. More than 30 kinds of de-icing
48 methods have been formed in the pursuit of materials with excellent ice-phobic
49 properties, which can be classified in three function categories: heating, mechanical
50 scraping and chemical agents. While these methods are widely used in engineering,
51 many shortcomings still exist, in terms of energy consumption, environmental impact
52 and cost ([Parent et al., 2011](#); [Koenig et al., 2011](#); [Makkonen et al., 2012](#)).

53 Since the discovery of superhydrophobic surfaces represented by the lotus leaf
54 phenomenon and recent developments in materials fabrication, an appealing method
55 for mitigating ice adhesion is to use icephobic coatings to repel ice or reduce ice
56 adhesion on an exposed surface ([Zheng et al., 2017](#)). Superhydrophobic surfaces are
57 regarded as a promising way to remove accumulated ice because of their extraordinary
58 water-repellency. Therefore, it is no surprise that recent research in this field has
59 focused predominantly on the use and development of superhydrophobic surfaces. To
60 demonstrate the dual role in delaying nucleation played by superhydrophobic surfaces,
61 [Alizadeh et al \(2012\)](#) utilized infrared thermometry and high-speed photography to
62 measure and observe the freezing process of droplets on superhydrophobic surfaces.
63 However, recent literatures on how hydrophobic and superhydrophobic surfaces can
64 reduce ice adhesion strength or repel water have featured poor durability ([Kulinich and
65 Farzaneh, 2009, 2011](#); [Lazauskas et al., 2013](#)). Meanwhile, many shortcomings have
66 appeared during actual use, such as poor pollution resistance, high preparation cost and
67 other disadvantages ([Karmouch et al., 2010](#); [Varanasi et al., 2010](#); [Jung et al., 2011](#);

68 [Kulinich et al., 2011](#)). Despite numerous efforts to mitigate these problems, a simple,
69 effective and inexpensive anti-icing technique has yet to be found.

70 A phase transformation must occur when water freezes and this freezing is
71 accompanied by a volume increase and the generation of an expansive force. This force
72 has an impacted on engineering structures in cold regions, such as reservoirs, marine
73 structures, breakwaters and retaining walls ([Healy et al., 2006](#); [She et al., 2006](#); [Iliescu
74 et al., 2007](#)). For instance, when the South-to-North Water Diversion crosses into cold
75 regions, the expansive load generated by icing acts on the ditch, greatly impacting its
76 performance and operational safety ([Fu et al., 2015](#)).

77 If this swelling force could be harnessed in a reasonable and effective manner, it
78 could become a useful anti-icing or de-icing solution. In cold settings, water or moisture
79 attached to a material surface would be frozen into the ice, and the stability of the ice-
80 substrate surface greatly influences the ice adhesion. Hence, this work proposes a new
81 de-icing model: ones that takes the phase swelling force as the active power to impact
82 the stability of the contact surface in order to reduce the ice adhesion strength, and
83 making it very easy to remove accumulated ice.

84

85 **2. Materials and methods**

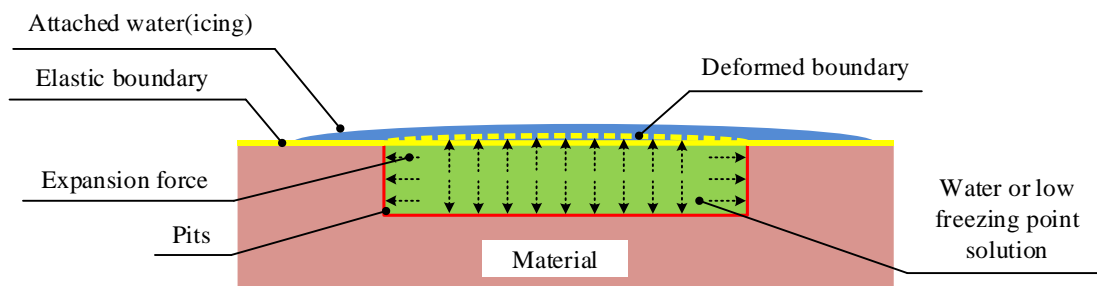
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87 **2.1 Anti-icing model and theory**

88

89 This study puts forward an active de-icing model that uses the expansive force to
90 remove accumulating ice, as shown in Fig. 1. The substrate has a pit filled with water
91 or solutions that have a lower freezing point than water (0 °C). Therefore, there is a

92 difference in phase transition time between the water and the media located in the pit.
 93 The surface of the material is covered by an elastic film. At low temperatures, water or
 94 moisture attaches to the film in an adhesive manner, which freezes first and becomes
 95 attached to the surface of the material. Owing to the thermal conductivity and the lower
 96 freezing point, the solution under the membrane begins to freeze later than the water
 97 attached to the membrane.



98
 99 Fig 1. Schematic of the proposed anti-icing model

100
 101 During the freezing process, the solution undergoes the stage of volume expansion
 102 and freezes into a pointy ice-drop (Peters et al., 2009; Enríquez et al., 2012; Snoeijer et
 103 al., 2012; Chaudhary et al., 2014). The size changes significantly after freezing into ice
 104 compared to the height of the water droplets, as shown in Fig. 2 where, H is significantly
 105 larger than h . Therefore, the swelled load generated by the freezing solution filling the
 106 pit would directly act on the elastic film and causes deformation. This would result in
 107 the contact interface becoming defective, affecting the contact stability of the interface
 108 between the material and ice. The ice adhesion strength would therefore decrease,
 109 making the accumulation ice easy to remove.

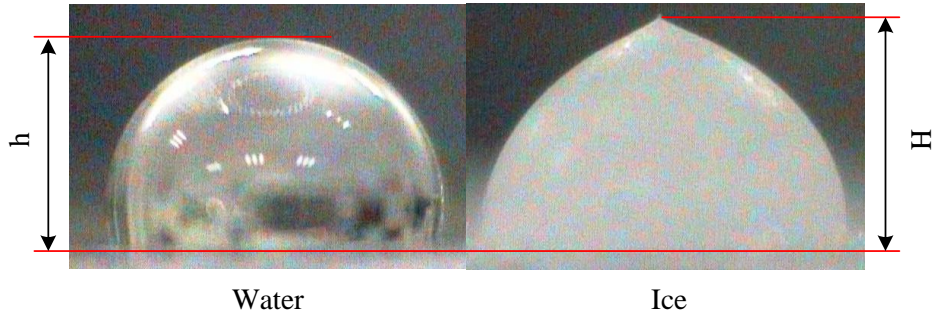


Fig 2. Droplet shapes after freezing

2.2 Materials

To demonstrate the effectiveness of this de-icing model, experiments were performed using a cup method to fabricate ice for testing, as shown in Fig. 3. In order to eliminate the influence of thermal conductivity on this anti-icing model, our tests employed 6061 aluminum alloy and polymethyl methacrylate (pmma) with thermal conductivities of 237 W/m·k and 0.2 W/m·k respectively, to represent materials with good and poor thermal conductivities. All samples were 60 mm×60 mm×6 mm (L×W×H) in size, and the specimens with the pits were covered by a biaxially oriented polypropylene (bopp) film as the elastic contact interface. The pits were machined using a milling method, where pits 30 mm in diameter and 3.5 mm deep, were filled with water or other lower freezing point solutions such as the ethanol solution, glycol solution, glycerine solution.

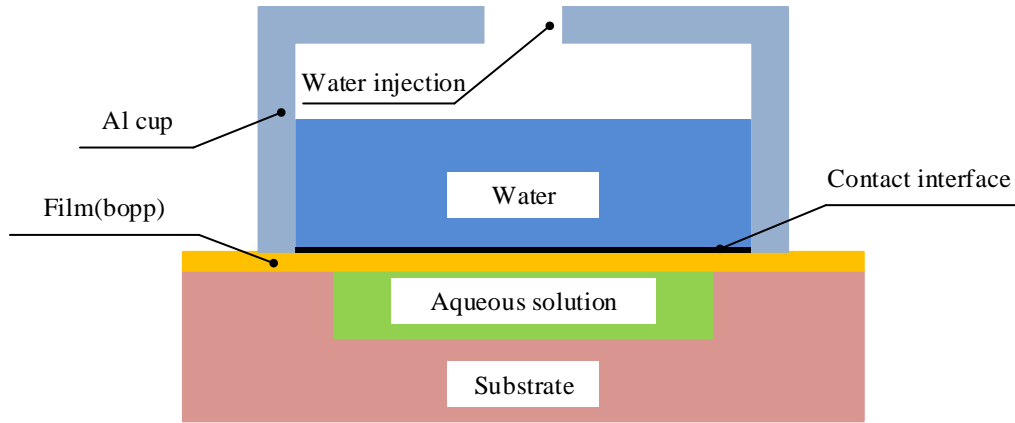


Fig 3. Schematic of the anti-icing model

2.3 Characterization of the frozen medium

In addition to being filled with water, the pits could be filled with different mass concentrations of ethanol solution and glycol solution during different experiments; ethanol solutions and glycol solutions with mass concentrations of 10%, 15%, 20% were used. The differences in freezing temperature between water and the different solutions are shown in Table 1.

Table 1 Freezing points of test solutions (°C)

Mass concentration	Ethanol solution	Glycol solution
10%	-4.7	-3.5
15%	-6.8	-5.3
20%	-10.4	-8.8

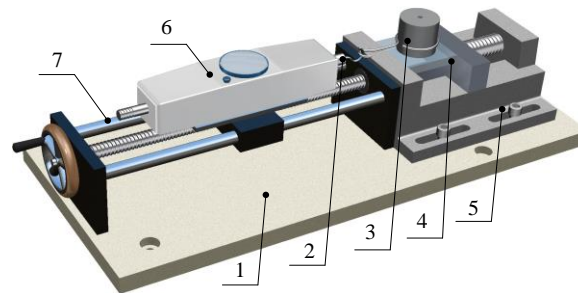
The temperature change curves were recorded during the freezing process of these aqueous solutions under the same ambient temperature. The temperature of the liquid was measured by a K-type thermocouple embedded in the sample pit, having an accuracy of $\pm 1.0\%$.

142

143 2.4 Experimental conditions

144

145 During the experiments, the entire anti-icing model was placed in a climate
146 chamber controlled to an ambient temperature at $-25\text{ }^{\circ}\text{C}$ and was frozen for 1 h, the
147 temperature accuracy of the climate chamber was $\pm 0.01\text{ }^{\circ}$. The phenomenon of ice
148 adhesion could be regarded as ice, a special adhesive, attaching to the material surface
149 under low temperature conditions. Therefore, the test device was designed according to
150 the ASTM-D3528 (2008) standard, as shown in Fig. 4. The experiment adopted the
151 more intuitive and simple unit N to evaluate the shear ice adhesion strength. The inner
152 diameter of the aluminum cup was 32 mm.



153

154 1. Base; 2. Connecting ring; 3. Aluminum alloy cup; 4. Sample; 5. Vice;

155

6. Draft gauge; 7. Rally stand.

156

Fig 4. Ice adhesion strength test device

157

158 The accumulated ice was peeled off from the material surface by pushing the draft
159 gauge, and the maximum force was recorded during the peeling process. In this paper,
160 the ice adhesion force is defined as the tangential ice adhesion strength because it can
161 be easily compared to the results of other works. The precision of the draft gauge is 0.1
162 N.

163

164 3. Results

165

166 3.1 Ice adhesion strength

167

168 Pits of aluminum alloy and pmma were filled with water and different mass
 169 concentrations of ethanol and glycol solutions, and the ice adhesion strength on the
 170 smooth sample (without pits) was tested as a reference. The samples were labeled as *A*,
 171 *B*, *C*, *D*, *E*, *F*, *G*, *H*, and the characteristics of each sample are shown in Table 2.

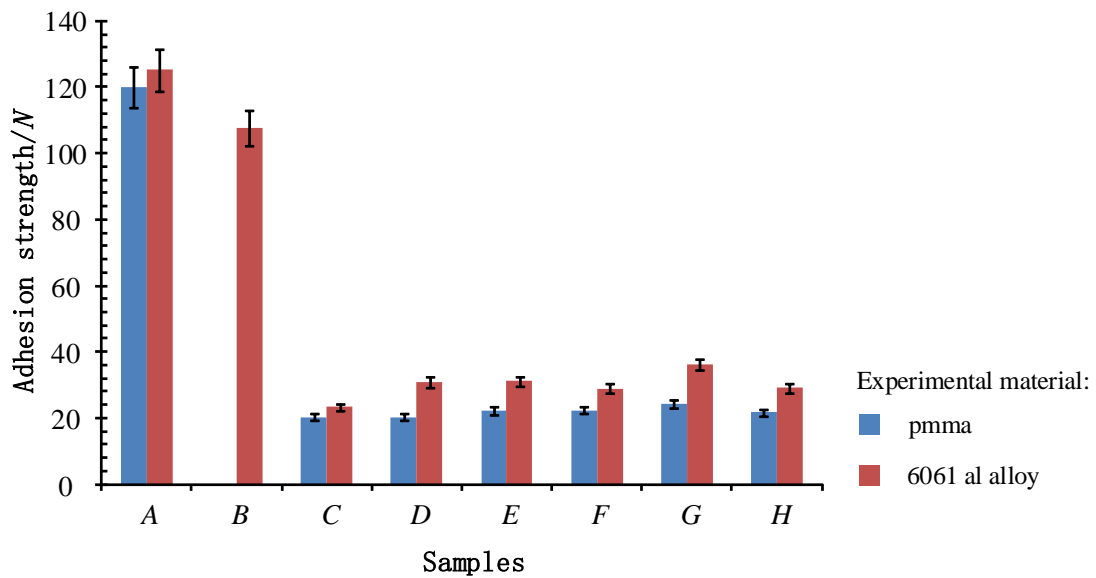
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Table 2 Sample descriptions

Medium	None	Water	Ethanol solution			Glycol solution		
	(without pit)		10%	15%	20%	10%	15%	20%
Name	A	B	C	D	E	F	G	H

173

174 Eight different samples were tested twenty times each, and the average results was
 175 taken as the ice adhesion strength of the sample in question. Fig. 5 summarizes the
 176 experimental results.



177

178 Fig 5. Shear ice adhesion strength. 1) Adhesion strength on the B_{pmma} sample was 0 N.
179 2) A-smooth sample; B-the pit of sample filled with water; C, D, E- the sample pit full
180 of 10%, 15%, 20% mass concentration of ethanol solution, respectively; F, G, H- full
181 of 10%, 15%, 20% mass concentration of glycol solution, respectively.

182
183 The adhesion strengths of samples with the solution-filled pits were substantially
184 lower than that in smooth specimen; in particular, the ice adhesion strength of sample
185 B_{pmma} was 0 N, with a 100% reduction rate. The ice adhesion strength of $B_{6061\text{ al}}$ which
186 had formed with 107.74 N, was obviously larger than that of $C_{6061\text{ al}}-H_{6061\text{ al}}$. The ice
187 adhesion strength of the aluminum alloy specimens was obviously larger than in the
188 case of the pmma surfaces. No matter whether the pit filled with ethanol solution or
189 glycol solution, the ice adhesion strength on the aluminum alloy and pmma had similar
190 growth trends. When the pits were filled with ethanol solution, the ice adhesion strength
191 increased gradually with increasing mass concentration in the ethanol solution, while
192 the growth rate gradually decreased with this trend. In addition, ice adhesion strength
193 of the samples containing of glycol solutions first increased and then diminished with
194 increasing in mass concentration. For example, the ice adhesion strength of aluminum
195 alloy samples with different mass concentrations of ethanol solution were 23.25 N,
196 30.85 N, and 31.1 N, respectively, and the strengths of samples $F_{6061\text{ al}}-H_{6061\text{ al}}$ were
197 28.86 N, 36.2 N, and 29.17 N, respectively.

198

199 **3.2 Surface topography after testing**

200

201 Owing to the elasticity of the attached film, the swelling load generated by freezing

202 of the different solutions in the pits can act on the surface, such that the contact surface
203 could produce different surface morphologies. Fig. 6 shows the surface topography
204 after the ice adhesion strength tests.



205
206 Fig 6. Surface topography of pmma specimen filled with water after freezing and
207 peeling the accumulated ice

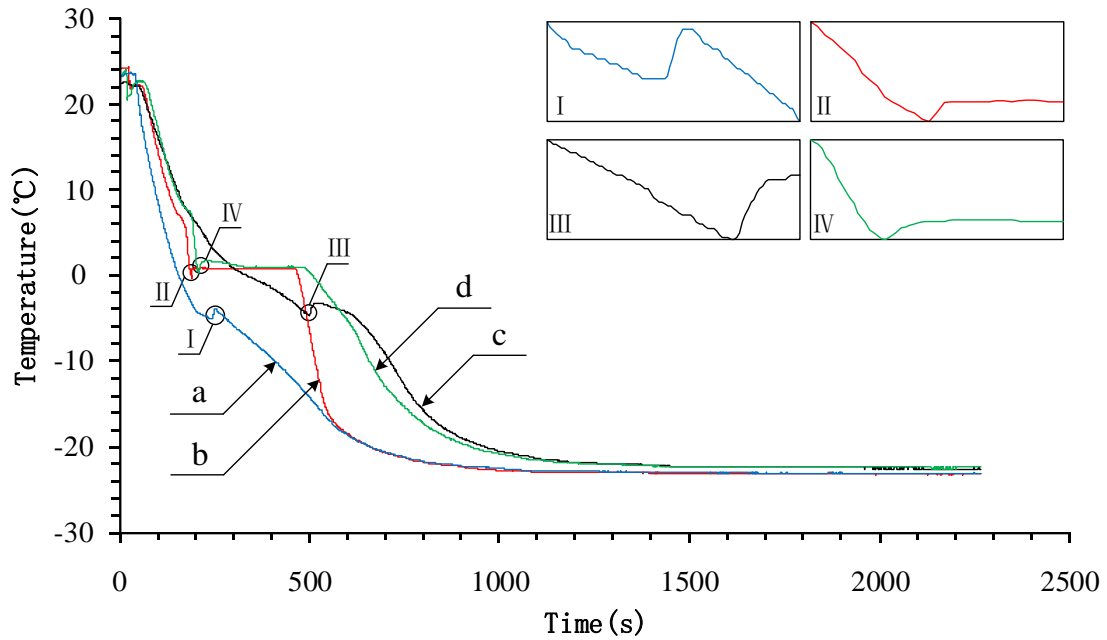
208
209 The morphology of the freezing interface obviously changed, and the area of the
210 pit featured irregular deformation because the solution froze and underwent the volume
211 expansion. The membrane of the sample with water in the pit generated the largest
212 expansive deformation, as shown in Fig. 6.

213

214 3.3 Freezing characteristics of the solution

215

216 The purpose of using the phase change time differential between the two kinds of
217 freezing media was to adopt the swelling force and to reduce the ice adhesion strength.
218 Therefore, it is necessary to understand the temperature variation during freezing
219 process. Under similar conditions, the temperatures of several kinds of solutions
220 adopted in the ice adhesion strength tests and water attached on the covered film were
221 measured. Taking the 10% mass concentration of ethanol solution as an example, the
222 curves of the change in temperature of the solution in the pits and water were recorded
223 using a thermal conductor (± 0.01 °C) and are shown in Fig. 7.



224

225 Fig 7. Changes in solution temperature during the freezing process: (a) temperature
 226 curve of solution in pit of 6061 aluminum alloy; (b) temperature curve of water attached
 227 on 6061 aluminum alloy; (c) temperature curve of solution in pit of pmma; (d)
 228 temperature curve of water attached on pmma.

229

230 As shown in Fig. 7, the freezing times of the media in the pits were later than those
 231 of the water attached on the membrane surfaces. This was especially apparent for pmma
 232 with its poor thermal conductivity, where a large time difference between two kinds of
 233 media in the freezing time was observed.

234

235 During the freezing process, the temperature variations of both the solution in pits
 236 and the water attached to the film were measured, and the differences in the phase
 237 transition behavior of the two media are given in Table 3.

237

Table 3 Phase transition time differences between water and pit solutions (s)

	Materials	6061 Aluminum	Polymethyl
Solution		alloy	methacrylate (pmma)

Water	43	306.67
10% Ethanol solution	141	502.33
15% Ethanol solution	285.75	760.75
20% Ethanol solution	520.75	971
10% Glycol solution	95.33	465
15% Glycol solution	195	642.67
20% Glycol solution	305.33	878.75

238

239 As the mass concentration increases, the difference in phase transformation time
 240 between the water and test solution increases in magnitude. At the same time, the
 241 thermal conductivity of the sample would also affect the phase transition time
 242 differently between water and the test solutions.

243

244 **4. Discussion**

245

246 Based on the experimental results, this anti-icing model is effective for reducing
 247 the ice adhesion strength. In this setup, the swelling force associate with the phase
 248 change would destroy the freezing interface, and have a great influence on decreasing
 249 the ice adhesion strength. By comparing the freezing strengths on 6061 aluminum alloy
 250 and pmma (representing materials with good and poor thermal conductivity
 251 respectively), the thermal conductivity of the freezing substrate has a minimal influence
 252 on the anti-icing model, in terms of reducing the ice adhesion strength.

253 Owing to the thermal conductivity and freezing point of the liquid in the pits, there
 254 was a difference in the order of freezing between the water attached on the film and the
 255 medium located in the pits. At $-25\text{ }^{\circ}\text{C}$, water above the membrane begin to freeze,

256 forming a stable and smooth contact interface. By prolonging the freezing time, the
 257 medium in the pits begins to undergo phase change, and the latent heat of the phase
 258 transformation was released during the process, of which the expansion force is one
 259 forms. During the freezing process, we assumed that the phase transformation
 260 expansion of the lower freezing point solution was caused primarily by the water
 261 component in solution, regardless of the molecular interactions between ethanol/ glycol
 262 and water. Therefore, the latent heat of solidification in these lower freezing point
 263 solutions filled was equal to the energy released by freezing the water component of
 264 the solution. The theoretical calculated values for the latent heat of solidification of
 265 each solution are given in Table 4.

266 Table 4 Theoretical solidification latent heats of sample solutions (*kJ/L*)

Medium	Water	Ethanol solution			Glycol solution		
		10%	15%	20%	10%	15%	20%
Latent heat	334.39	295.50	277.18	259.11	311.18	296.34	281.05

267
 268 The freezing process of the aqueous solution was quick and released a high amount
 269 of energy, as shown in Fig. 7 and Table 4, and volume expansion occurred. The solution
 270 in the pit underwent a rapid phase change and release of expansive energy akin to an
 271 explosion, leading to a very high energy density. Since the sides of the pit were covered
 272 by an elastic boundary, the released expansion energy only acted on the elastic film
 273 causing film deformation, and turning the stable and smooth interface into a rugged one,
 274 as shown in Fig. 8.

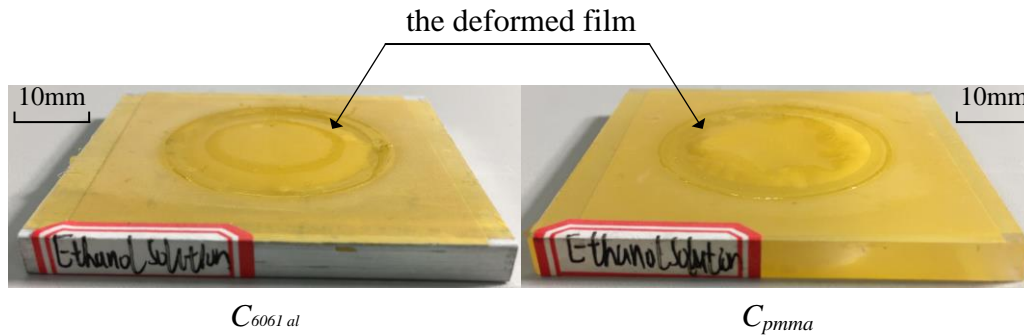


Fig 8. Deformed elastic membranes

Of all tested specimens, the freezing strength of B_{pmma} filled with water in the pit was the lowest, at 0 N. However, the ice adhesion strength of B_{6061al} was slightly lower than that of the smooth aluminum specimen, which was higher than that of the other samples. Since the phase difference of sample B_{6061al} was less than in any other sample, the attached water was frozen first. Shortly, after the above surface water froze, the medium located in the pit began to freeze along with a volume expansion that caused deformation in the elastic film. The anti-icing model continued to be refrigerated in the climate chamber, and the interface between the deformed membrane and the ice would be reformed. Although the ice adhesion strength on the reformed interface was reduced, the reduction rate was small. The interface of B_{6061al} still had a small amount of ice slag after peeling off the ice, but the surface of B_{pmma} free of ice residue and water in the pit where the volume expansion occurred, and the ice attached on the surface had completely peeled off.

When the pit is filled with liquid having a lower freezing point than water, there is a difference in phase transition time between the test liquid and water. This causes volume expansion and the release of swelling energy by freezing the solution, to deform

294 the elastic boundary, and destroy the contact stability and continuity. Thus, the freezing
295 strength is reduced.

296

297 **5. Conclusions**

298

299 In summary, the ice on the polymethyl methacrylate (pmma) substrates having pits
300 filled with water were thoroughly separated from the sample surface, and the ice
301 adhesion strength of B_{pmma} was the smallest, 0 N. Different kinds of solutions had
302 different effects on the ice adhesion strength reduction rate based on material type, but
303 the ice adhesion strength on different samples with pit were remarkably reduced
304 compared to those on samples without pits.

305 The proposed de-icing model achieved a good de-icing effect and reduced the ice
306 adhesion strength in experimental studies. It was found that the influence of the
307 substrate's thermal conductivity was small. During the de-icing model, pits on the
308 substrates were filled with water or other solutions with lower freezing points compared
309 to water. Because of this, there was a phase transition time difference during the de-
310 icing models. In the cold surroundings, the water is firstly frozen the ice owing to the
311 thermal conductivity of the material itself. When the solution in the pit began to solidify,
312 it underwent expansion associated with this phase transformation. The swelling force
313 generated in a short time acted on the elastic contact interface to cause film deformation.
314 Furthermore, this destroys the stability of the interface between the ice and the sample
315 surface. Thus, the ice adhesion strength could be reduced and the aim of de-icing would
316 be achieved.

317 Based on the experiment results, this paper provides a novel method for
318 developing anti-icing methods at low cost, with high de-icing efficiency and minimal
319 pollution, and we get an inspiration, such as the fabrication of the microscopic structure
320 to contain the solution, or similar to the honeycomb structure attached on the material
321 to improve the active de-icing performance of substrate.

322

323 **Acknowledgments**

324

325 This study was financially supported by the International Exchanges Scheme
326 Between the Royal Society and the NSFC (grant number. 51711530236).

327

328 **References**

329

330 [ASTM D3528-96\(2008\). Standard test and method for strength properties of double lap](#)
331 [shear adhesive joints by tension loading \[S\].](#)

332 [Alizadeh, A., Yamada, M., Li, R., et al, 2012. Dynamics of ice nucleation on water](#)
333 [repellent surfaces. Langmuir 28\(6\), 3180-3186.](#)

334 [Bewilogua, K., Bräuer, G., Dietz, A., et al, 2009. Surface technology for automotive](#)
335 [engineering. CIRP Annals – Manuf. Technol. 58\(2\), 608-627.](#)

336 [Carriveau, R., Edrissy, A., Cadieux, P., et al, 2012. Ice adhesion issues in renewable](#)
337 [energy infrastructure. J. Adhes. Sci. Technol. 26\(4-5\), 447-461.](#)

338 [Cucchiella, F., D'Adamo, I., 2012. Estimation of the energetic and environmental](#)
339 [impacts of a roof-mounted building-integrated photovoltaic systems. Renew.](#)
340 [Sustain. Energy. Rev. 16\(7\), 5245-5259.](#)

341 Caliskan, F., Hajiyev, C., 2013. [A review of in-flight detection and identification of](#)
342 [aircraft icing and reconfigurable control](#). *Prog. Aerosp. Sci.* 60, 12-34.

343 Chaudhary G., Li, R., 2014. [Freezing of water droplets on solid surfaces: An](#)
344 [experimental and numerical study](#). *Exp. Therm. Fluid Sci.* 57, 86-93.

345 Enríquez, O.R., Marín, Á.G., Winkels, K.G., 2012. [Freezing singularities in water](#)
346 [drops](#). *Phys. Fluids.* 24(9), No. 091102.

347 Fu, H., Yang, K., Guo, X.L., et al, 2015. [Safe operation of inverted siphon during ice](#)
348 [period](#). *J. Hydrodyn.* 27(2), 204-209.

349 Healy, D., Hicks, F.E., 2006. [Experimental study of ice jam formation dynamics](#). *J. Cold*
350 [Reg. Eng. 20\(4\), 117-139.](#)

351 Iliescu, D., Bake, I., 2007. [The structure and mechanical properties of river and lake](#)
352 [ice](#). *Cold Reg. Sci. Technol.* 48(3), 202-217.

353 Jung, S., Dorrestijn, M., Raps, D., et al, 2011. [Are superhydrophobic surfaces best for](#)
354 [icephobicity?](#). *Langmuir*, 27(6), 3059-3066.

355 Koenig, G.G., Ryerson, C.C., 2011. [An investigation of infrared deicing through](#)
356 [experimentation](#). *Cold Reg. Sci. Technol.* 65(1), 79-87.

357 Karmouch, R., Ross, G.G., 2010. [Experimental study on the evolution of contact angles](#)
358 [with temperature near the freezing point](#). *J. Phys. Chem. C.* 114(9), 4063–4066.

359 Kulinich, S.A., Farzaneh, M., 2009. [How wetting hysteresis influences ice adhesion](#)
360 [strength on superhydrophobic surfaces](#). *Langmuir*, 25(16), 8854-8856.

361 Kulinich, S.A., Farhadi, S., Nose, K., et al, 2011. [Superhydrophobic surfaces: are they](#)
362 [really ice-repellent?](#). *Langmuir*, 27(1), 25-29.

363 Kulinich, S.A., Farzaneh, M., 2011. [On ice-releasing properties of rough hydrophobic](#)
364 [coatings. Cold Reg. Sci. Technol. 65\(1\), 60-64.](#)

365 Lazauskas, A., Guobiene, A., Prosyčėvas, I., et al, 2013. [Water droplet behavior on](#)
366 [superhydrophobic SiO₂ nanocomposite films during icing/deicing cycles. Mater.](#)
367 [Charact. 82, 9-16.](#)

368 Makkonen, L., 2012. [Ice adhesion —theory, measurements and countermeasures. J.](#)
369 [Adhes. Sci. Technol. 26\(4-5\), 413-445.](#)

370 Peters, I., Snoeijer, J.H., Daerr, A., et al, 2009. [Coexistence of two singularities in](#)
371 [dewetting flows regularizing the corner tip. Phy. Rev. Lett. 103\(11\), No. 114501.](#)

372 Parent, O., Ilinca, A., 2011. [Anti-icing and de-icing techniques for wind turbines:](#)
373 [Critical review. Cold Reg. Sci. Technol. 65\(1\), 88-96.](#)

374 Petrenko, V.F., Sullivan, C.R., Kozlyuk, V., 2011. [Variable-resistance conductors \(VRC\)](#)
375 [for power-line de-icing. Cold Reg. Sci. Technol. 65\(1\), 23-28.](#)

376 Ruan, M., Wang, J.W., Liu, Q.L., et al, 2016. [Superhydrophobic and anti-icing](#)
377 [properties of sol-gel prepared alumina coatings. Russian J. Non-Ferr. Met. 57\(6\),](#)
378 [638-645.](#)

379 Snoeijer, J.H., Brunet, P., 2012. [Pointy ice-drops: How water freezes into a singular](#)
380 [shape. Am. J. Phy. 80\(9\), 764-771.](#)

381 Stone, R., 2008. [Natural disasters. Ecologists report huge storm losses in China's forests.](#)
382 [Science 319\(5868\), 1318-1319.](#)

383 She, Y., Hicks, F., 2006. [Modeling ice jam release waves with consideration for ice](#)
384 [effects. Cold Reg. Sci. Technol. 45\(3\), 137-147.](#)

- 385 Varanasi, K.K., Deng, T., Smith, J.D., et al, 2010. Frost formation and ice adhesion on
386 superhydrophobic surfaces. *Appl. Phys. Lett.* 97(23), No. 234102.
- 387 Zheng, H.K., Chang, S.N, Zhao, Y.Y, 2017. Anti-icing & icephobic mechanism and
388 applications of superhydrophobic/ultra slippery surface. *Prog. Chem.* 29(1), 102-
389 118.
- 390 Zhang, P, Lv, F.Y, 2015. A review of the recent advances in superhydrophobic surfaces
391 and the emerging energy-related applications. *Energy* 82, 1068-1087.