

# Constraints on the presence of post-perovskite in Earth's lowermost mantle from tomographic-geodynamic model comparisons

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## Abstract

Lower mantle tomography models consistently feature an increase in the ratio of shear-wave velocity ( $V_S$ ) to compressional-wave velocity ( $V_P$ ) variations and a negative correlation between shear-wave and bulk-sound velocity ( $V_C$ ) variations. These seismic characteristics, also observed in the recent SP12RTS model, have been interpreted to be indicative of large-scale chemical variations. Other explanations, such as the lower mantle post-perovskite (pPv) phase, which would not require chemical heterogeneity, have been explored less. Constraining the origin of these seismic features is important, as geodynamic simulations predict a fundamentally different style of mantle convection under both scenarios. Here, we investigate to what extent the presence of pPv explains the observed high  $V_S/V_P$  ratios and negative  $V_S-V_C$

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correlation globally. We compare the statistical properties of SP12RTS with the statistics of synthetic tomography models, derived from both thermal and thermochemical models of 3-D global mantle convection. We convert the temperature fields of these models into seismic velocity structures using mineral physics lookup tables with and without pPv. We account for the limited tomographic resolution of SP12RTS using its resolution operator for both  $V_S$  and  $V_P$  structures. This allows for direct comparisons of the resulting velocity ratios and correlations. Although the tomographic filtering significantly affects the synthetic tomography images, we demonstrate that the effect of pPv remains evident in the ratios and correlations of seismic velocities. We find that lateral variations in the presence of pPv have a dominant influence on the  $V_S/V_P$  ratio and  $V_S-V_C$  correlation, which are thus unsuitable measures to constrain the presence of large-scale chemical variations in the lowermost mantle. To explain the decrease in the  $V_S/V_P$  ratio of SP12RTS close to the CMB, our results favour a pPv-bearing CMB region, which has implications for the stability field of pPv in the Earth's mantle.

*Keywords:* Seismic tomography, Tomographic filtering, Composition of the mantle, Geodynamic modelling, Mineral physics

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## 1. Introduction

Tomographic models typically display an increase in the ratio of shear-wave velocity variations ( $d\ln V_S = \delta V_S/V_S$ ) to compressional-wave velocity variations ( $d\ln V_P$ ) up to values of 2.5–3.5 in the lowermost mantle, accompanied by a strong negative correlation between shear-wave and bulk-sound velocity variations ( $d\ln V_C$ ) (e.g. Su and Dziewonski, 1997; Ishii and

7 Tromp, 1999; Masters et al., 2000; Della Mora et al., 2011; Koelemeijer et al.,  
8 2016). The depth extent of these seismic features varies (Fig. 1). Models  
9 based on body-wave data typically show high ratios throughout the lower  
10 mantle, whereas models based on longer period data feature lower ratios.  
11 Model SP12RTS contains a marked decrease in the ratio near the core-mantle  
12 boundary (CMB), a robust feature due to the incorporation of CMB Stoneley  
13 mode data (Koelemeijer et al., 2016).

14 [Fig. 1 about here.]

15 Traditionally, observations of a high ratio of  $\text{dln}V_S$  over  $\text{dln}V_P$  (from  
16 hereon termed *S/P ratio*) and a negative correlation between  $\text{dln}V_S$  and  
17  $\text{dln}V_C$  (from hereon termed *S-C correlation*) have been interpreted as evi-  
18 dence for compositional heterogeneity (e.g. Su and Dziewonski, 1997; Mas-  
19 ters et al., 2000; Moulik and Ekström, 2016), as purely thermal effects (in  
20 the absence of temperature-dependent phase changes) only produce a S/P  
21 ratio of up to  $\sim 2.5$  (Karato and Karki, 2001). Specifically, two large-low-  
22 velocity provinces (LLVPs) underneath the Pacific and Africa, which cover  
23  $\sim 25$  percent of the core surface, are thought to be chemically distinct, as  
24 these feature the largest increase in the S/P ratio, have a pronounced neg-  
25 ative S-C correlation (Masters et al., 2000; Koelemeijer et al., 2016) and  
26 show a large deviation from purely thermal velocity variations (Simmons  
27 et al., 2010; Tesoniero et al., 2016). In the past, this interpretation has  
28 been corroborated by normal-mode density models that indicated that the  
29 LLVPs have a higher-than-average density (Ishii and Tromp, 1999; Trampert  
30 et al., 2004). However, recent studies have found both dense (Moulik and  
31 Ekström, 2016; Lau et al., 2017) and light LLVPs (Koelemeijer et al., 2017).

32 Determining the origin of the large-scale LLVPs is important, as isochemi-  
33 cal and thermochemical convection models predict distinct thermochemical  
34 evolutionary pathways, different geochemical residence times, a contrasting  
35 distribution and magnitude of CMB heat flow, and, hence, models of outer  
36 core convection.

37 Before observations of a high S/P ratio and negative S-C correlation can  
38 be interpreted as solely due to chemical heterogeneity, other mechanisms need  
39 to be considered. As suggested in the past (Tsuchiya et al., 2004; Wookey  
40 et al., 2005), the lower mantle post-perovskite phase (pPv) also provides an  
41 possible explanation for these seismic features without the need for large-scale  
42 chemical variations. An increase in  $V_S$  and a decrease in  $V_P$  accompanies the  
43 phase transition from bridgmanite (brg) to pPv (e.g. Murakami et al., 2004;  
44 Oganov and Ono, 2004; Tsuchiya et al., 2004), resulting in an increased S/P  
45 ratio and a negative S-C correlation. In addition, the presence of a phase  
46 transition introduces artefacts in radially-averaged depth profiles of seismic  
47 velocities and their ratios (Styles et al., 2011). Although, in principle, the  
48 properties of pPv thus explain seismic characteristics of global tomography  
49 models (Davies et al., 2012, 2015), its stability field is composition-dependent  
50 and remains poorly constrained by mineral physics (Cobden et al., 2014). In  
51 addition, it has not been investigated yet whether: (i) the occurrence of pPv  
52 is expected to be widespread enough to influence radially-averaged seismic  
53 properties; (ii) the effect of pPv is observable in large-scale global tomography  
54 models; and thus whether (iii) global tomography can be used to constrain  
55 its stability field.

56 Here, we aim to establish whether the presence of pPv or chemical het-

57 erogeneity is the dominant factor in explaining the globally observed high  
58 S/P ratio and negative S-C correlation in the lowermost mantle. In addition,  
59 we investigate whether global tomography can provide insights into the sta-  
60 bility field of post-perovskite. To this end, we study the seismic properties  
61 of geodynamic models with and without pPv, and compare these to seismic  
62 tomography models. As in previous studies (Schuberth et al., 2009a; Davies  
63 et al., 2012), we ensure that our comparisons are meaningful, especially in  
64 terms of the amplitudes, by utilising a tomographic resolution operator (Rit-  
65 sema et al., 2007). Although studies have filtered  $V_S$  structures in the past,  
66 using for example the resolution operator of S40RTS (Ritsema et al., 2011),  
67 joint filters for  $V_S$  and  $V_P$  structures are not readily available. Here, we use  
68 the resolution operator of SP12RTS (Koelemeijer et al., 2016), which filters  
69 both  $\text{dln}V_S$  and  $\text{dln}V_P$  structures simultaneously and has an improved resolu-  
70 tion close to the CMB due to the inclusion of Stoneley mode data. Therefore,  
71 comparisons of SP12RTS with filtered geodynamic models enable us to in-  
72 vestigate the origin of the high S/P ratio near 2500 km depth, its decrease  
73 towards the CMB and the negative S-C correlation in the lowermost mantle.

74 This paper is organised as follows: In Section 2, we provide a brief descrip-  
75 tion of model SP12RTS and the geodynamic models used in this study, be-  
76 fore introducing the SP12RTS tomographic resolution operator (Section 2.3).  
77 Subsequently, we discuss the effects of reparameterisation and tomographic  
78 filtering on synthetic tomography models in Section 3, demonstrating that  
79 the effect of pPv remains evident throughout these processing steps. In Sec-  
80 tion 4 we compare SP12RTS with the geodynamic models, discussing their  
81 properties and the important effects of data weighting and the Clapeyron

82 slope in the tomographic inversions. These comparisons indicate that pPv  
83 plays a dominant role in explaining lowermost mantle characteristics of global  
84 seismic tomography models, even within the LLVPs. Finally, in Section 5 we  
85 discuss the implications of our results in light of the current state of knowl-  
86 edge in mineral physics, showing that tomographic-geodynamic comparisons  
87 can potentially be used to constrain the stability field of pPv.

## 88 **2. Model specifications and resolution operator**

89 We briefly review model SP12RTS and the geodynamic models explored  
90 in this study. We refer the reader to Koelemeijer et al. (2016) for further  
91 details on model SP12RTS and to Schuberth et al. (2009b) and Davies et al.  
92 (2012) for a more extensive discussion of the geodynamic modelling and  
93 mineral physics conversions.

### 94 *2.1. Seismic model SP12RTS*

95 SP12RTS is a whole-mantle, long-wavelength model of shear-wave and  
96 compressional-wave velocity variations, obtained using the same inversion  
97 procedure as S-wave velocity model S40RTS (Ritsema et al., 2011). To opti-  
98 mise data coverage, normal-mode splitting function measurements, Rayleigh  
99 wave phase-velocity measurements and teleseismic body-wave traveltimes  
100 were combined, with varying weighting factors between the three data sets.  
101 Compared to S40RTS, P-wave traveltime data were added and the normal-  
102 mode splitting function data set was significantly increased (143 modes in-  
103 stead of 49). By including 33 new modes sensitive to  $V_P$  variations, as well  
104 as 9 CMB Stoneley modes with an unique sensitivity to the lowermost man-  
105 tle (Koelemeijer et al., 2013), P-wave velocity variations were independently

106 constrained in the inversion. The model was parameterised laterally in spher-  
107 ical harmonics up to angular order 12, limiting us to consider large-scale  
108 structure only.

109 Fig. 2 shows the velocity structure of SP12RTS in the lowermost mantle.  
110 The long-wavelength  $V_S$  structure is practically identical to that of S40RTS,  
111 and SP12RTS contains many features observed in other tomographic models.  
112 Large regions of low shear- and compressional-wave velocities (LLVPs) exist  
113 underneath the Pacific and Africa, increasing in strength towards the CMB.  
114 The LLVP under the Pacific is more circular, whereas the African LLVP  
115 is elongated in the North-South direction, and both are surrounded by a  
116 ring of higher velocities.  $V_S$  amplitudes increase continuously with depth,  
117 whereas  $V_P$  variations only increase from  $\sim 2500$  km depth. However, their  
118 geographic patterns are strongly correlated at all depths. The  $V_C$  variations,  
119 constructed using  $\ln V_S$  and  $\ln V_P$  following the method of Masters et al.  
120 (2000), are negatively correlated with  $V_S$  variations, both within and outside  
121 the LLVPs. The negative S-C correlation and S/P ratio peak at a depth  
122 of 2500 km before decreasing towards the CMB (Fig. 1). Although such  
123 a decrease had been observed previously (Romanowicz, 2001; Della Mora  
124 et al., 2011), it was generally attributed to poor data coverage near the  
125 CMB. However, in case of SP12RTS, Koelemeijer et al. (2016) showed that  
126 this is a robust feature due to the incorporation of CMB Stoneley modes.

127 [Fig. 2 about here.]

## 128 2.2. Geodynamic models

129 We use high-resolution global mantle circulation models similar to those  
130 presented in Schubert et al. (2009b) and Davies et al. (2012). We generate

131 temperature and compositional fields using a modified and benchmarked ver-  
132 sion of the spherical mantle convection code TERRA (Baumgardner, 1985;  
133 Davies et al., 2013), which solves for the conservation equations of mass, mo-  
134 mentum and energy at infinite Prandtl number (i.e. no inertial forces). We  
135 prescribe isothermal conditions at the surface (300 K) and CMB (4000 K). We  
136 specify a free slip boundary condition at the CMB, while we prescribe surface  
137 velocities according to 200 Myr of plate motion history (Seton et al., 2012),  
138 at discrete 1 Myr intervals. A fine discretisation ( $\sim 25$  km cells, resulting  
139 in about 80 million grid points) allows us to simulate mantle flow at Earth-  
140 like convective vigour, which is essential for generating synthetic structures  
141 that are comparable to seismic observations of Earth’s present-day mantle.  
142 Our models include internal heating in the mantle, compressibility and a  
143 temperature-depth dependent viscosity. The Supplementary Material con-  
144 tains further details on these parameters and the model initiation procedure,  
145 with key model parameters listed in Supplementary Table S1.

146 Similarly to Davies et al. (2012), we focus on two end-member scenarios  
147 for describing temperature variations within the mantle: (i) a purely ther-  
148 mal model with no chemical heterogeneity (‘TH’ models from hereon); and  
149 (ii) a thermochemical ‘pile’ model, where chemically distinct material fo-  
150 cuses into large-scale structures in the lowermost mantle (‘TC’ models from  
151 hereon). We convert modelled temperature, pressure and compositional fields  
152 into elastic parameters using lookup tables generated using a thermodynamic  
153 mineralogical model for a simplified six-component system of mantle com-  
154 position (Stixrude and Lithgow-Bertelloni, 2011). We opt to use such a  
155 self-consistent mineralogical model, where the thermodynamics of the sys-



156 tem dictate the stability field of pPv and thus its Clapeyron slope, instead of  
157 assuming a constant Clapeyron slope (see Supplementary Fig. S1 and Sup-  
158 plementary Material). This way, we incorporate the non-linear pressure and  
159 temperature dependence of material properties and account for non-linear  
160 thermodynamic effects on phase transitions.

161 We perform the conversion using two versions of the lookup tables for  
162 each chemical composition, one including and the other excluding pPv from  
163 the database. Hence, we obtain four synthetic tomography models: models  
164 TH-pPv and TC-pPv where pPv is included, and models TH-nopPv and  
165 TC-nopPv where pPv is not present in the lowermost mantle. For TH-pPv  
166 models, we also test the influence of the assumed Clapeyron slope using ex-  
167 trapolated (i.e. not physically constrained) mineral physics tables, described  
168 in more detail in the Supplementary Material. In the conversion, we assume  
169 a pyrolitic mantle composition for the TH models, whereas TC models con-  
170 tain an additional basalt component, which comprises  $\sim 3\%$  of the mantle's  
171 volume (see Supplementary Table S2). We do not include the dynamic effects  
172 of the post-perovskite transition in the geodynamic simulations themselves,  
173 only at the conversion stage to seismic velocities. However, as we limit our-  
174 selves to the interpretation of large-scale statistical properties, we do not  
175 expect our results to change significantly (see Supplementary Material).

176 [Fig. 3 about here.]

177 Fig. 3 illustrates present-day snapshots of the temperature field,  $V_S$  struc-  
178 ture and pPv occurrence in the geodynamic models in the lowermost mantle.  
179 Remnants of old slabs are visible above the CMB in all models. These down-

180 wellings modulate the location of hot material such that it becomes concen-  
 181 trated into large-scale structures beneath Africa and the Pacific. The Pa-  
 182 cific anomaly is approximately circular, while the African anomaly is a NW-  
 183 SE trending structure, extending southeastwards into the Indian Ocean. In  
 184 TH models, these structures comprise clusters of plumes and interconnected  
 185 hot (slow), linear ridges, whereas in TC models they represent discontinu-  
 186 ous chemical ‘piles’. These piles cover around 40% of the CMB, with the  
 187 highest temperatures (lowest S-wave velocities) predicted at their edges. At  
 188  $\sim 2480$  km depth, pPv is present locally in high-velocity regions (pyrolite  
 189 composition) in both TH and TC models, resulting in increased  $V_S$  am-  
 190 plitudes. With depth, its occurrence becomes more wide-spread and the  
 191 mineral physics tables predict that pPv is present everywhere at  $\sim 2750$  km  
 192 depth, even for basaltic material (see Supplementary Fig. S1). We observe  
 193 the strongest velocity variations around 2575 km depth, where large regions  
 194 of bridgmanite material transform to post-perovskite. These large velocity  
 195 variations are due to the removal of the radial average at each depth and  
 196 expected for a phase transition (Styles et al., 2011). The presence of pPv  
 197 affects  $V_P$  variations in a similar way, except that it reduces their amplitudes  
 198 rather than increasing them (Supplementary Fig. S2).

### 199 2.3. Seismic resolution operator

200 Following Ritsema et al. (2007), we define the resolution operator  $\mathcal{R} =$   
 201  $\mathbf{G}^\dagger \mathbf{G}$ , where  $\mathbf{G}$  is the operator of the seismic forward problem and  $\mathbf{G}^\dagger$  is its  
 202 generalised inverse. We modify the geodynamic prediction of seismic hetero-  
 203 geneity (the “true” input model  $\mathbf{m}^{\mathbf{IN}}$ ) by multiplying it with  $\mathcal{R}$  to obtain a

204 “filtered” output model  $\mathbf{m}^{\text{OUT}}$  as if imaged by tomographic inversion:

$$\mathbf{m}^{\text{OUT}} = \mathcal{R} \cdot \mathbf{m}^{\text{IN}}. \quad (1)$$

205  $\mathcal{R}$  fully describes the spatially heterogeneous resolution of the tomographic  
 206 model. We have to compute  $\mathcal{R}$  on the basis of the same damping parameter  
 207  $\epsilon$  as the tomographic model. In SP12RTS,  $\epsilon$  was 0.005, corresponding to  
 208  $\sim 1200$  unknowns, which we therefore adopt here as well.

209 In contrast to S40RTS, SP12RTS is a tomographic model of both  $V_S$  and  
 210  $V_P$  variations, hence the model vector  $\mathbf{m}$  consists of two parts:

$$\mathbf{m} = \begin{pmatrix} \mathbf{S} \\ \mathbf{P} \end{pmatrix}, \quad (2)$$

211 where  $\mathbf{S}$  and  $\mathbf{P}$  are model vectors describing  $\text{dln}V_S$  and  $\text{dln}V_P$ , respectively.

212 We rewrite Equation 1 as follows:

$$\begin{pmatrix} \mathbf{S}^{\text{OUT}} \\ \mathbf{P}^{\text{OUT}} \end{pmatrix} = \begin{pmatrix} \mathcal{R}_{\text{SS}} & \mathcal{R}_{\text{SP}} \\ \mathcal{R}_{\text{PS}} & \mathcal{R}_{\text{PP}} \end{pmatrix} \begin{pmatrix} \mathbf{S}^{\text{IN}} \\ \mathbf{P}^{\text{IN}} \end{pmatrix}, \quad (3)$$

213 where  $\mathcal{R}_{\text{SS}}$  and  $\mathcal{R}_{\text{PP}}$  are the diagonal blocks of  $\mathcal{R}$  detailing how  $V_S$  structure  
 214 maps into  $V_S$  structure (ditto for  $V_P$ ). The off-diagonal blocks of  $\mathcal{R}$ , i.e.  $\mathcal{R}_{\text{SP}}$   
 215 and  $\mathcal{R}_{\text{PS}}$ , contain information about how  $V_S$  and  $V_P$  structures map into  
 216 each other (i.e. leakage of structure).

217 The resolution operator is dominantly diagonal (Koelemeijer et al., 2016),  
 218 but  $\mathcal{R}_{\text{SP}}$  and  $\mathcal{R}_{\text{PS}}$  are not strictly zero. Therefore, some artefacts arise during  
 219 tomographic filtering. Hence, it is crucial to use the full resolution operator  
 220 incorporating the off-diagonal blocks when filtering geodynamic models. We  
 221 note that the resolution of SP12RTS in the lower mantle is similar for  $\text{dln}V_S$   
 222 and  $\text{dln}V_P$ , which is important when considering their ratio.

### 223 **3. Effects of tomographic filtering on the S/P ratio and S-C corre-** 224 **lation**

225 To ensure meaningful comparisons – geodynamic models contain typically  
226  $\sim 80$  million grid points, whereas SP12RTS was constructed with only  $\sim 3500$   
227 parameters – we first have to reparameterise all original geodynamic models  
228 to the SP12RTS parameterisation (i.e. 21 splines with depth and spherical  
229 harmonics up to degree 12). Reparameterisation leads to a drastic reduction  
230 in the model dimensionality, broadening structures and reducing amplitudes  
231 of negative anomalies (low velocities) more ( $\sim 20$ - $50\%$  lower) than those of  
232 positive anomalies ( $\sim 0.5$ - $15\%$  lower) (Fig. 4a–b). Subsequently, we multiply  
233 the reparameterised models with  $\mathcal{R}$ , which effectively acts as a low-pass filter  
234 (Ritsema et al., 2007; Schuberth et al., 2009a), causing structures to broaden  
235 and weaken further (Fig. 4c). As the reparameterisation and filtering affect  
236  $V_S$  and  $V_P$  structure differently in different locations, we explicitly consider  
237 here their effects on the S/P ratio and S-C correlation.

238 [Fig. 4 about here.]

#### 239 *3.1. Global properties*

240 In this paper, we always compute the velocity ratios and correlations with  
241 respect to each model’s radial average. In addition, we consistently compute  
242 them using the spherical harmonic coefficients where possible, which allows  
243 us to consider different spherical harmonic degrees directly. For the high-  
244 resolution models, which are not parameterised in spherical harmonics, we  
245 use the RMS velocities, which results generally in the same curves (Koele-  
246 meijer et al., 2016). The resulting values are larger compared to using the

247 median of the distribution (Koelemeijer et al., 2016). However, we prefer  
248 this approach as it means we do not divide by small values, which require  
249 special treatment (Tesoniero et al., 2016).

250 The presence of pPv is evident in the depth profiles of the original geody-  
251 namic models (Fig. 5a). At lowermost mantle depths where bridgmanite and  
252 pPv coexist (i.e. lateral variations in the presence of pPv occur), the S/P  
253 ratio increases and we observe a pronounced, negative S-C correlation. Both  
254 the S/P ratio and the S-C correlation curves peak around 2650 km depth,  
255 when most material has transformed to pPv. We only observe a single peak  
256 in the S/P ratio, rather than the typical peak-trough behaviour of a phase  
257 transition (Styles et al., 2011), as the RMS velocities are always positive.

258 Upon reparameterisation (Fig. 5b), minor artefacts are present in the  
259 model with pPv, because the smooth spline interpolation cannot capture the  
260 sharp depth changes in the ratio and correlation. We find stronger arte-  
261 facts after tomographic filtering (Fig. 5c), primarily due to the non-zero  
262 off-diagonal terms of  $\mathcal{R}$ . This especially affects the S-C correlation as we  
263 construct  $\text{dln}V_C$  using  $\text{dln}V_S$  and  $\text{dln}V_P$ , both with their own limited resolu-  
264 tion. For model TH-pPv, the filtering results in a negative S-C correlation at  
265 depths as shallow as  $\sim 1800$  km. In addition, the thermal model without pPv  
266 (TH-nopPv), originally displaying a positive S-C correlation, now displays a  
267 small, negative S-C correlation that is entirely artificial. When we consider  
268 degree 2 structure only, artefacts are smaller and the S-C correlation of model  
269 TH-nopPv remains positive (Fig. 5c).

270 Despite the artefacts mentioned above, the effect of pPv remains evident  
271 throughout the processing steps, even when we account for the limited to-

272 tomographic resolution. We consistently observe a high S/P ratio and negative  
273 S-C correlation due to pPv in the TH models, as also noted by Della Mora  
274 et al. (2011). The same trends are observed for TC models (Supplementary  
275 Fig. S3), although the presence of additional basalt material in the lowermost  
276 mantle complicates the patterns. On the contrary, the correlation between  
277  $\text{dln}V_S$  and  $\text{dln}V_P$  (S-P correlation) is high in all geodynamic models, even af-  
278 ter filtering (Supplementary Fig. S4). Therefore, we cannot use this property  
279 to probe for the presence of pPv and/or chemical heterogeneity.

280 [Fig. 5 about here.]

### 281 3.2. Fast and slow clusters

282 For lowermost mantle structure, clusters of fast and slow velocities cap-  
283 ture the differences between the LLVPs and the ambient mantle and thus  
284 provide more insights into the nature of seismic anomalies (Lekić et al., 2012).  
285 As the Clapeyron slope of the brg-pPv phase transition is positive (Cobden  
286 et al., 2014), we expect the transition to occur at shallower depth in cold  
287 regions (fast velocities in TH models) than in hot regions (slow velocities).  
288 Consequently, the S/P ratio and S-C correlation peak at different depths in  
289 regions of fast and slow velocities, giving rise to a depth offset between the  
290 two. Here, we consider whether such a depth offset remains distinct after  
291 reparameterisation and filtering.

292 We split every geodynamic model into two clusters using the fast ( $\text{dln}V_S >$   
293  $0$ ) and slow ( $\text{dln}V_S < 0$ ) anomalies of the models themselves. We compute the  
294 geographic locations of both clusters at a reference depth of 2850 km and sub-  
295 sequently use this for all depths in the mantle, similar to Lekić et al. (2012).

296 We exclude all points for which  $d\ln V_S$  or  $d\ln V_P$  are smaller than 0.01%. This  
297 approach is different from Koelemeijer et al. (2016) who split SP12RTS into  
298 fast and slow clusters using the vote map of Lekić et al. (2012). However,  
299 the vote map is based on the geographic distribution of seismic anomalies.  
300 Using the same approach for geodynamic models would not be meaningful,  
301 as the distribution of seismic structure depends on plate reconstructions and  
302 unknown initial conditions.

303 Using the cluster definition described above, original geodynamic models  
304 indeed feature a depth offset of  $\sim 100$  km between the fast and slow cluster,  
305 especially in the S-C correlation (Fig. 6). After reparameterisation (Fig. 6b),  
306 the offset decreases ( $\leq 50$  km) due to the broad spline spacing of SP12RTS in  
307 the lowermost mantle. Tomographic filtering removes this remaining depth  
308 offset, and we observe almost no difference in the filtered clusters (Fig. 6c).  
309 This implies that even if there is a depth offset between fast and slow velocity  
310 regions, it is not resolved by SP12RTS. It is thus not surprising that no  
311 depth offset was observed in SP12RTS itself (Koelemeijer et al., 2016). By  
312 incorporating a finer depth parameterisation, future studies may be able to  
313 improve on this.

314 [Fig. 6 about here.]

## 315 4. Results

### 316 4.1. Tomographic-geodynamic model comparisons

317 The amplitudes of SP12RTS (Fig. 2, third column) are most compatible  
318 with those observed in filtered TH models (Fig. 4c), whereas the ampli-  
319 tudes in filtered TC models are too large (Davies et al., 2012), particularly

320 for  $\text{dln}V_P$ . Nevertheless, all geodynamic models reproduce the large-scale  
321 patterns of SP12RTS at this depth, with low velocity anomalies at the loca-  
322 tions of the LLVPs, surrounded by higher-than-average velocities. We focus  
323 from hereon only on the S/P ratio and S-C correlation within a given model  
324 (computed directly from the spherical harmonic coefficients), removing the  
325 dependence on the plate reconstructions employed in the geodynamic sim-  
326 ulations. We do not calculate tomographic-geodynamic model correlations,  
327 as these quantities would primarily inform us about the uncertainties in the  
328 plate reconstructions, rather than help us to constrain the origin of seismic  
329 anomalies.

330 Models with pPv match SP12RTS well below depths of  $\sim 2300$  km (Fig. 7)  
331 as they display an increased S/P ratio and a more negative S-C correlation  
332 in the lower mantle. However, the S/P ratio peaks  $\sim 100$  km deeper than in  
333 SP12RTS. Although models without pPv also feature a (small) negative S-C  
334 correlation (an artefact of the tomographic filtering as shown in the previous  
335 section), they fail to produce a high S/P ratio. The difference between models  
336 with and without pPv is particularly strong for degree-2 structure (Fig. 7b),  
337 where models with pPv are in close agreement with SP12RTS in the lower-  
338 most mantle (below  $\sim 2300$  km depth). Between 1700 km and 2300 km, all  
339 geodynamic models fail to reproduce the negative S-C correlation observed  
340 in SP12RTS. The addition of a chemically distinct phase (model TC-pPv)  
341 changes the amplitude of the S/P ratio, but it does not significantly improve  
342 the overall match with SP12RTS. Therefore, we conclude that both TH and  
343 TC models reproduce the main statistical properties of SP12RTS equally  
344 well, if pPv is present.



345

[Fig. 7 about here.]

346 Although there is no difference between fast and slow clusters after to-  
347 mographic filtering (Fig. 6), TH-pPv and TC-pPv (i.e. geodynamic models  
348 with pPv) reproduce the high S/P ratio and negative S-C correlation in both  
349 clusters and thus match the large-scale characteristics of SP12RTS (Fig. 8).  
350 Hence, pPv could also be used as an explanation for observations of a high  
351 S/P ratio and negative S-C correlation inside LLVPs, even though we expect  
352 these to be hotter than the surrounding mantle. However, one should keep  
353 in mind that the seismically slow regions (i.e. LLVPs) in filtered models also  
354 incorporate cold regions (i.e. with pPv) in the high-resolution models. Note  
355 also that pPv is not necessarily present at the same depths in both clusters  
356 (this depth sensitivity is lost during tomographic filtering). In addition, we  
357 have not imposed its presence in the LLVPs – this is a consequence of physi-  
358 cally constrained dynamic models combined with mineral physics predictions  
359 for a reasonable mantle composition. Thus, our results merely imply that it  
360 is plausible for post-perovskite to be present within the seismically-imaged  
361 LLVPs and that its presence there explains tomographic features.

362

[Fig. 8 about here.]

#### 363 *4.2. Effects of inversion data weighting*

364 SP12RTS contains data from body waves, surface waves and normal  
365 modes, with weighting factors imposed between the different data sets. For  
366 the default SP12RTS model, the data weights were chosen to balance the  
367 sensitivities of body-wave and normal-mode data (Koelemeijer et al., 2016).

368 To investigate the robustness of our results, we repeat our tomographic-  
 369 geodynamic model comparison for inversions dominated either by normal-  
 370 mode splitting functions or body-wave traveltimes. This means that we mul-  
 371 tiply our reparameterised models by  $\mathcal{R}_s$  (normal-modes dominated) and  $\mathcal{R}_t$   
 372 (body-waves dominated) and compare these with the corresponding versions  
 373 of SP12RTS (i.e. SP12RTS<sub>s</sub> and SP12RTS<sub>t</sub>, respectively).

374 Models filtered using  $\mathcal{R}_s$  (normal-modes dominated) show a clear differ-  
 375 ence due to the presence of pPv (Fig. 9a), with the best match again when  
 376 pPv is present (Fig. 9). For models filtered with  $\mathcal{R}_t$  (body-waves dominated),  
 377 we observe that the high S/P ratio and negative S-C correlation are artificially  
 378 smeared upwards to depths of  $\sim 2000$  km. A likely reason for this is that our  
 379 filtering does not capture the uncertainties in the underlying theory of the  
 380 tomographic inversion, in this case ray theory. Neglecting finite-frequency  
 381 effects in combination with vertical ray paths thus leads to artificial high  
 382 S/P ratios and a negative S-C correlation in the body-wave dominated in-  
 383 versions (Malcolm and Trampert, 2011). Thus, we argue that studies of the  
 384 S/P ratio based on body-wave ray theory (e.g. Su and Dziewonski, 1997;  
 385 Della Mora et al., 2011) cannot be used to distinguish between thermal and  
 386 chemical variations, consistent with recent work by Tesoniero et al. (2016).

387 [Fig. 9 about here.]

388 A spectral decomposition of model TH-pPv filtered using  $\mathcal{R}_s$ ,  $\mathcal{R}$  and  $\mathcal{R}_t$   
 389 further illustrates the importance of the data weighting on the robust retrieval  
 390 of the S/P ratio and S-C correlation (Supplementary Fig. S5). We recover  
 391 the features of the reparameterised model (a high S/P ratio and negative S-  
 392 C correlation at all spherical harmonic degrees) well using  $\mathcal{R}_s$  (normal-mode

dominated) for even spherical harmonic degrees. For SP12RTS (filtering using  $\mathcal{R}$ ), we recover even degrees up to  $l = 10$ . However, the odd degrees display more artefacts, as the self-coupled splitting function data only constrain even-degree structure. When using  $\mathcal{R}_t$  (body-waves dominated), we observe an increase in the S/P ratio at lowermost mantle depths and an artificial upward smearing of the negative S-C correlation to depths of 1800 km for all spherical harmonic degrees. This demonstrates that the depth extent of the negative S-C correlation depends on the weighting of the data sets, with more severe smearing occurring when we give more weight to body-wave data (if treated with ray theory). This is a possible explanation for the differences between previous tomographic models: the body-wave model of Su and Dziewonski (1997) featured a negative S-C correlation throughout the mantle, whereas the long-period model of Masters et al. (2000) only contained a negative correlation in the lowermost mantle (Fig. 1). We speculate that these studies imaged the same structures, filtered and smeared differently due to the differences in theoretical approximations in their respective inversion schemes.

#### 4.3. Influence of the Clapeyron slope

The mineral physics table for pyrolite used here predicts that pPv is present everywhere at the CMB due to the shallowing of the Clapeyron slope at high temperature (see Supplementary Fig. S1). To test the influence of the Clapeyron slope on the S/P ratio and S-C correlation, as well as their fit to SP12RTS, we use two additional mineral physics tables as described in the Supplementary Material and shown in Fig. 10a). In these tables, “TH-pPv-extra” and “TH-pPv-extra100”, we assume a constant Clapeyron

418 slope of  $\sim 13$  MPa/K (i.e. the one found at low temperatures) and linearly  
419 extrapolate (i.e. non-physical) the phase boundary down to the CMB. This  
420 way, we enforce a pPv-free CMB while at shallower depth either pPv is  
421 everywhere except in the lowest velocity regions (TH-pPv-extra) or pPv only  
422 occurs as lenses in the highest velocity regions (TH-pPv-extra100) (Fig. 10b).

423 For the TH-pPv-extra model, we observe increased S/P ratios down to  
424 the CMB (Fig. 10c), whereas the TH-pPv-extra100 model results in lower  
425 S/P ratios. For both these models, the peak in the S/P ratio also occurs at  
426 greater depth as the stability field is shifted downwards. The different mineral  
427 physics tables produce a larger variation in the S/P ratio and S-C correlation  
428 compared to Fig. 7b. As the mineral physics tables are characterised by a  
429 different areal extent of pPv (Fig. 10b), we suggest that this areal extent has  
430 a strong control on the S/P ratio and S-C correlation, an idea we explore  
431 further in Section 5.1. We also note that even the effect of small lenses of  
432 pPv (the TH-pPv-extra100 model) is observable in the synthetic tomography  
433 images.

434 The shape of the S-C correlation curve for degree 2 is reproduced best  
435 by the original TH-pPv model, as the S-C correlation remains negative for  
436 the extrapolated tables (Fig. 10d). This is confirmed by calculating the L2-  
437 norm between the S/P ratio and S-C correlation curves of SP12RTS and the  
438 geodynamic models (Fig. 10e–f). Lower misfits are generally found when pPv  
439 has a larger areal extent (higher “pPv coverage”) as in the original TH-pPv  
440 model, particularly for the L2-norm based on the S-C correlation. On the  
441 other hand, models with pPv lenses and a pPv-free CMB region (the TH-  
442 pPv-extra and TH-pPv-extra100 models) do not reproduce the decrease in

443 the S/P ratio in SP12RTS and the increase in the S-C correlation close to the  
444 CMB, resulting in a higher misfit. A spectral decomposition of the different  
445 models also suggests that the original TH-pPv model provides the closest fit  
446 to the seismic characteristics of SP12RTS at other spherical harmonic degrees  
447 (Supplementary Fig. S6). These results imply that the statistical properties  
448 of SP12RTS, particularly the positive values of the S-C correlation close to  
449 the CMB, are matched best by a pPv-bearing CMB region, an idea that is  
450 consistent with work by Cobden et al. (2012) using core diffracted phases.

451 [Fig. 10 about here.]

## 452 5. Discussion

453 We observe only small differences between isochemical and thermochemi-  
454 cal models, whereas the areal extent of pPv makes a large difference (Fig. 10).  
455 Here, we will first discuss the dominant controls on the S/P ratio and S-C  
456 correlation. Then, we discuss the influence of the uncertainties in the miner-  
457 alogical model on our results. Subsequently, we indicate which seismological  
458 features our geodynamic models cannot explain, before ending by consider-  
459 ing the implications of our results on the the presence of pPv and the nature  
460 of lower mantle heterogeneity.

### 461 5.1. Dominant controls on the S/P ratio and S-C correlation

462 The large similarity in S/P ratio and S-C correlation for TH and TC  
463 models (despite the presence of large-scale chemical heterogeneity result-  
464 ing in a different planform of convection) is partly due to the fact that the

465 reparameterisation and tomographic filtering act as low-pass filters (see Sec-  
466 tion 3). However, the S-C correlation is already markedly negative in high-  
467 resolution models with pPv (TH-pPv in Fig. 5a and TC-pPv in Supplemen-  
468 tary Fig. S3a). The reason for this is that a similar amount of pPv is present  
469 at any given depth in both TH and TC scenarios (Fig. 3). Although the  
470 hotter areas have a larger extent in the TC-pPv model, they contain basaltic  
471 material, which transforms to pPv at shallower depths due to the negative  
472 Clapeyron slope for basalt at high temperatures (Supplementary Fig. S1b).  
473 In addition, the geotherms and temperature distributions of both TH and  
474 TC models are similar with the majority of temperatures close to the average  
475 (Supplementary Fig. S1). The large similarity in the distribution of pPv re-  
476 sults in almost indistinguishable values of the S/P ratio and S-C correlation,  
477 with only a small effect from the assumed mantle composition. Tesoniero  
478 et al. (2016) came to a similar conclusion, although they considered different  
479 compositions for one-dimensional profiles rather than lateral compositional  
480 variations.

481 The assumed CMB temperature has also only a minor effect on the S/P  
482 ratio and S-C correlation (Supplementary Fig. S7). Again, the geotherms and  
483 temperature distributions throughout the mantle are similar (Supplementary  
484 Material and Supplementary Fig. S8). The CMB temperature only affects the  
485 excess plume temperatures, not the temperature of subducting material, and  
486 slow clusters (hot areas) thus show (slightly) larger differences. However,  
487 after filtering, only the slow cluster with  $T_{CMB}=4400$  K is distinguishable  
488 (Supplementary Fig. S7c). Consequently, we cannot place constraints on the  
489 CMB temperature using our tomographic-geodynamic model comparisons.

490 Throughout our results, we observe that the areal extent of pPv intro-  
491 duces the largest variations in the S/P ratio and S-C correlation curves (see  
492 Fig. 10 and Supplementary Fig. S6). Supplementary Fig. S9 illustrates this  
493 further, by plotting the percentage coverage of pPv at any depth versus the  
494 S/P ratio and S-C correlation in the high-resolution models. S/P ratios larger  
495 than  $\sim 3$  and strongly negative values of the S-C correlation are observed only  
496 for a pPv coverage of 10–90 %. These findings thus imply that in fact it is a  
497 partial coverage of pPv (i.e. lateral variations in pPv presence) that produce  
498 larger ratios and a negative S-C correlation, rather than pPv being present  
499 everywhere or nowhere. This is consistent with the notion that lateral varia-  
500 tions in a phase transition have a large effect on averaged quantities (Styles  
501 et al., 2011).

502 Fig. 10f indicates a clear trend between the L2 norm based on the S-C  
503 correlation and the percentage coverage of pPv at 2700 km depth. Thermo-  
504 chemical (TC) models and models with different CMB temperatures follow  
505 the same trend, indicating again that the lateral areal extent of pPv has  
506 the strongest effect on the S/P ratio and S-C correlation. Therefore, these  
507 seismic characteristics can only be used to determine the areal extent of pPv  
508 and not the composition of the lowermost mantle or CMB temperature.

### 509 *5.2. Mineral physics uncertainties*

510 We assume a pyrolitic mantle composition, which is a reasonable choice  
511 according to recent studies (Davies et al., 2012; Zhang et al., 2013; Shim et al.,  
512 2017), and an additional basaltic component in the TC case. Although iron-  
513 rich compositions have been suggested as representative for LLVPs, a basaltic  
514 composition was favoured by Davies et al. (2012) based on its high density

515 and ability to produce a negative S-C correlation. Given the dominance of  
516 pPv on the S/P ratio and S-C correlation, we believe that the main effect of a  
517 different mantle composition is to shift the stability field of pPv in depth and  
518 thus to change the lateral distribution of pPv. For example, it would occur  
519 shallower for MORB or iron-rich material and deeper for harzburgite or Al-  
520 rich material (Cobden et al., 2014). The uncertainty in mantle composition  
521 is thus addressed by our tests with the extrapolated mineral physics tables,  
522 even though these are un-physical.

523 To convert the temperature and composition fields to seismic velocities,  
524 we have opted to use a thermodynamic mineralogical model (Stixrude and  
525 Lithgow-Bertelloni, 2011) in which the Clapeyron slope of the brg-pPv tran-  
526 sition is non-linear for both pyrolite and basalt. This is in contrast to the  
527 general notion of a constant Clapeyron slope assumed in past studies, but the  
528 thermodynamic approach is preferable given its self-consistency and the fact  
529 that no experimental measurements exist for temperatures above  $\sim 3000$  K. In  
530 fact, there is no reason to expect a linear Clapeyron slope for the phase tran-  
531 sition and our results for the extrapolated tables show that a linear Clapeyron  
532 slope does not improve the fit to the seismic data. Furthermore, the values of  
533 3–13 MPa/K in the mineralogical model are consistent with Clapeyron slope  
534 estimates from experiments and theoretical calculations (e.g. Hirose, 2006;  
535 Stixrude and Lithgow-Bertelloni, 2011; Cobden et al., 2014).

536 The mineralogical tables are reproducible using an alternative software  
537 implementation of the Gibbs free energy minimisation algorithm and equa-  
538 tion of state calculations for the same database (Chust et al., 2017). Thus,  
539 the database parameters are the primary control on the phase transition



540 depth and the values of the Clapeyron slopes. We may need to re-evaluate  
541 the robustness of our findings after additional experimental data at high  
542 temperature become available, or for other choices of parameters in the min-  
543 eralogical tables (e.g. the crystal structure of Ca-Pv (Stixrude et al., 2007)).  
544 However, until then, our results show that for widely-used parameters, a pPv-  
545 bearing CMB region explains several lower mantle characteristics of global  
546 tomography models. This is consistent with work by Mosca et al. (2012) and  
547 Cobden et al. (2012), who, based on a large range of mineralogical models,  
548 also favoured models with pPv to explain lower mantle seismological obser-  
549 vations.

### 550 *5.3. Mid-mantle discrepancy*

551 A discrepancy remains between SP12RTS and the geodynamic models  
552 between 1800 km and 2300 km depth, where SP12RTS features an increased  
553 S/P ratio and the onset of a negative S-C correlation (Fig. 7). Given that  
554 we account for the limited tomographic resolution, we cannot explain this  
555 discrepancy with pPv, or more accurately, not with the parameters con-  
556 straining the stability field of pPv in the different mineral physics tables.  
557 As mentioned before, the stability field of pPv is not well constrained in  
558 high-pressure, high-temperature experiments, even for pure MgSiO<sub>3</sub> (Cob-  
559 den et al., 2014). Differences of 5–10 GPa in the transition pressure exist  
560 due to the pressure standard used in experiments (Tsuchiya et al., 2004; Hi-  
561 rose, 2006) and additional errors of 5–10 GPa could be introduced due to  
562 reversing the phase boundary. Therefore, it is possible that pPv is present at  
563 (slightly) shallower depths than currently assumed. However, given the small  
564 changes in peak depth for different Clapeyron slopes (Fig. 10), we question

565 whether it would explain the discrepancy entirely.

566 The iron spin transition provides another explanation for the discrepancy  
567 at 1800–2300 km depth, as this gradually affects seismic properties without  
568 producing sharp discontinuities (e.g. Stackhouse et al., 2007; Wentzcovitch  
569 et al., 2009). The effect of the spin transition in bridgmanite remains de-  
570 bated, but for ferropericlase, the spin transition has a clear effect on the  
571 seismic velocities. It primarily changes the bulk modulus (e.g. Wentzcovitch  
572 et al., 2009; Marquardt et al., 2009), which results in a drop of  $V_P$  with  
573 no change in  $V_S$ ; hence the S/P ratio increases and the S-C correlation be-  
574 comes negative. The depth range where this effect is expected depends on  
575 temperature, occurring typically deeper and over a wider depth range with  
576 increasing temperature, e.g. around 75 GPa (1700 km depth) for a temper-  
577 ature of 2500 K (Marquardt et al., 2009). This effect of the spin transition,  
578 unaccounted for in the mineralogical model employed here, could help to re-  
579 solve the discrepancy at mid-mantle depths. Whether incorporating changes  
580 in the oxidation state of iron, as suggested recently by Shim et al. (2017),  
581 or shear softening of Ca-Pv (Stixrude et al., 2007) improves the fit between  
582 SP12RTS and the geodynamic models further, remains to be seen. Finally,  
583 we cannot exclude the possibility that a negative S-C correlation at these  
584 depths (1800–2300 km) is due to the presence of chemical heterogeneity, i.e.  
585 tall, chemically distinct LLVPs. Although it would be difficult to predict  
586 their exact composition, the presence of MORB or iron-rich material (due  
587 to the accumulation of subducted crust or core-reaction products) would  
588 cause the pPv transition to occur at shallower depth, thereby reducing the  
589 mid-mantle discrepancy.

590 *5.4. Implications for lower mantle structures*

591 We show that the features of SP12RTS are best reproduced by the original  
592 mineral physics table, and thus by a pPv-bearing CMB region (Fig. 10e–f).  
593 We propose two different scenarios to achieve this, based on our tomographic-  
594 geodynamic comparisons. One possibility is that the Clapeyron slope of the  
595 brg-pPv transition in pyrolite shallows at high temperature, as predicted by  
596 the original mineral physics table (Supplementary Fig. S1a). Alternatively,  
597 the Clapeyron slope has a higher, constant slope, but the entire stability  
598 field of pPv is shifted to shallower depths than has been considered here.  
599 A shallower stability field of pPv would likely give rise to a shallower peak  
600 depth of the S/P ratio. This may thus improve the mismatch in peak depth  
601 currently observed between SP12RTS and the geodynamic models with pPv  
602 (Fig. 7), given that no improvement is observed for a change in the CMB  
603 temperature. To distinguish between the two proposed scenarios, mineral  
604 physics measurements of bridgmanite/pPv at high temperature ( $>3000$  K)  
605 and pressures above 115 GPa are required.

606 For a pPv-bearing CMB region, pPv needs to be stable at temperatures  
607 as high as 3600–4000 K. Whether such temperatures are too high remains  
608 debated, as solidus temperatures vary between  $\sim 4150$  K (Andrault et al.,  
609 2011) and  $3570 \pm 200$  K (Nomura et al., 2014). Nevertheless, our results  
610 for different CMB temperatures indicate that even for a CMB temperature  
611 of 3600 K, the characteristics of SP12RTS are reproduced best by models  
612 with pPv everywhere, including inside the LLVPs (Supplementary Fig. S7).  
613 The occurrence of pPv within the LLVPs remains debated (Garnero et al.,  
614 2016), complicated by uncertainties in estimates of its stability field and

615 its dependence on chemical composition (Cobden et al., 2014). However,  
616 recent normal-mode studies (Koelemeijer et al., 2017) and body-wave studies  
617 (Cobden et al., 2012) have favoured the presence of pPv within the LLVPs.  
618 When considering the presence of pPv inside tomographically-imaged LLVPs,  
619 it is also important to keep in mind that they may contain smaller-scale  
620 features (i.e. cold regions containing pPv), which are lost due to the limited  
621 resolution in tomography.

622 For the two possible scenarios described above, it is unlikely that the  
623 geotherm crosses the phase boundary a second time just above the CMB for  
624 CMB temperatures of 3600–4400 K. Hence, seismic observations of paired  
625 discontinuities can no longer be explained by a double crossing of the phase  
626 transition, as assumed by previous authors in efforts to constrain the CMB  
627 heat flux (e.g. Hernlund et al., 2005; Lay et al., 2008). Instead, the stishovite-  
628 seifertite transition in the silicate system could potentially explain these ob-  
629 servations (Grocholski et al., 2013). In addition, the temperature-pressure  
630 dependence of the Clapeyron slope may reconcile differences observed in the  
631 depth of the D'' discontinuity without the need to invoke local chemical het-  
632 erogeneity.

## 633 **6. Conclusions**

634 By comparing the statistical properties of tomographic model SP12RTS  
635 with synthetic tomography models derived from geodynamic simulations with  
636 and without post-perovskite and/or chemical heterogeneity, we have shown  
637 that:

- 638 1. We can identify the signature of pPv in global tomography models,

- 639 even when accounting for the limited resolution of seismic tomography.
- 640 2. Lateral variations in the presence of pPv give rise to a negative S-C  
641 correlation and high S/P ratio below 2300 km depth, explaining seismic  
642 characteristics.
  - 643 3. Due to the dominant control of pPv, one cannot constrain the compo-  
644 sition of the lowermost mantle using seismic observations of the S/P  
645 ratio and S-C correlation.
  - 646 4. The characteristics of SP12RTS are reproduced best for a CMB region  
647 covered by pPv, implying the presence of pPv inside the LLVPs.
  - 648 5. Two scenarios are proposed for the brg-pPv transition: a shallowing of  
649 the Clapeyron slope at high temperature or a shallower stability field  
650 for pPv.
  - 651 6. Our comparisons cannot be used to constrain the CMB temperature  
652 due to our limited tomographic resolution.
  - 653 7. Observed differences in the predicted depth of the negative S-C corre-  
654 lation, across a number of studies, are likely related to the data types  
655 used in the inversion procedures, with body-wave models artificially  
656 smearing the signal upwards to shallower depths.
  - 657 8. A discrepancy between SP12RTS and geodynamic predictions remains  
658 at mid-mantle depths (1800–2300 km), which could be due to uncer-  
659 tainties in the mineralogical model, unaccounted effects of the spin  
660 transition and/or the presence of shallower chemical heterogeneity.

661 Throughout our comparisons, we have stressed the importance of tomo-  
662 graphic filtering. This aids not only the identification of robust features  
663 in tomographic models, but it is also essential for meaningful comparisons

664 between tomographic and geodynamic models. The tomographic filter of  
665 SP12RTS, which filters both  $V_S$  and  $V_P$  structures jointly without any a-  
666 priori constraints, has an improved resolution close to the CMB compared to  
667 other studies and has been developed specifically to enable comparisons of  
668 seismic velocity ratios and correlations. Consequently, interested parties are  
669 encouraged to incorporate the SP12RTS filtering software (available online).

670 Despite the uncertainties in mantle composition and assumptions in the  
671 geodynamic modelling, we have demonstrated that a pPv-bearing CMB re-  
672 gion is preferred for explaining the decrease in the S/P ratio towards the  
673 CMB. The inference that pPv is present everywhere close to the CMB, also  
674 inside the LLVPs, should not be ignored as a possibility in future studies.  
675 In addition, our study indicates the potential for constraining the Clapeyron  
676 slope of the brg-pPv phase transition using global tomography, especially if  
677 future studies incorporate a denser depth parameterisation in the lowermost  
678 mantle.

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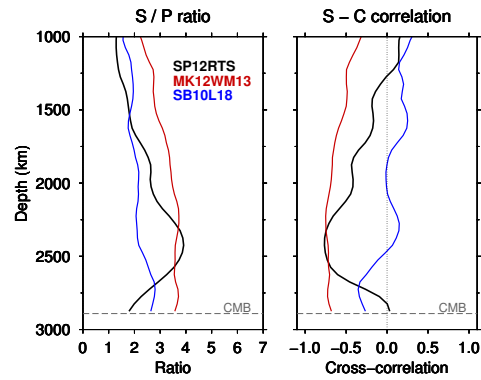
850 **Figures**

Figure 1: Characteristics of global tomography showing the S/P ratio (left) and S-C correlation (right) for some extreme cases: body-wave model MK12WM13 of Su and Dziewonski (1997) (red), long-period model SB10L18 of Masters et al. (2000) (blue) and mixed-data model SP12RTS of Koelemeijer et al. (2016) (black).

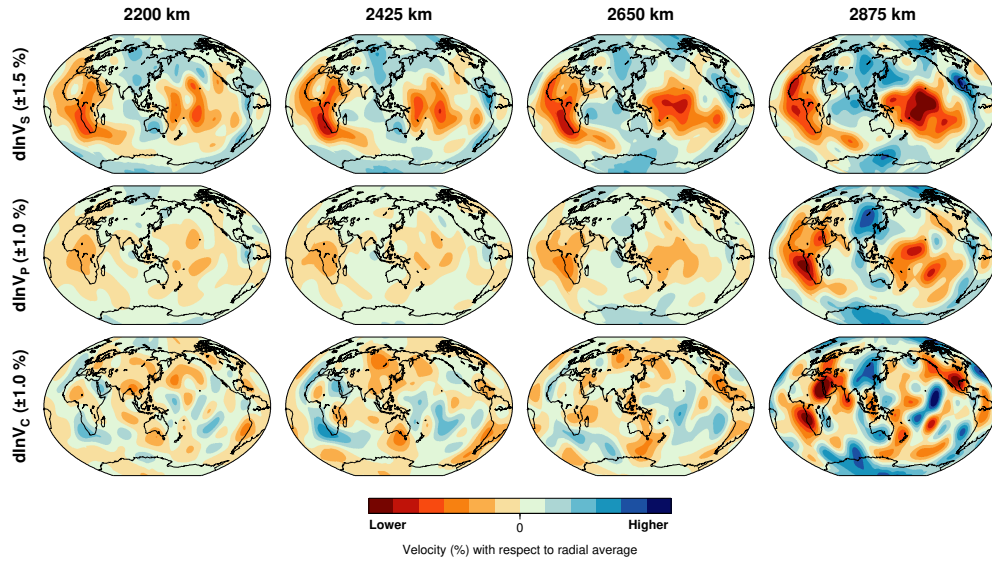


Figure 2: Variations in shear-wave velocity  $d\ln V_S$  (top), compressional-wave velocity  $d\ln V_P$  (middle) and bulk-sound velocity  $d\ln V_C$  (bottom) according to model SP12RTS at different depths in the mantle. Velocity is higher (lower) than the radial average at each depth in blue (red) regions and the colour intensity is proportional to the velocity amplitude up to a maximum of 1.5 % for  $d\ln V_S$  and 1.0 % for  $d\ln V_P$  and  $d\ln V_C$ , respectively. Note that  $d\ln V_C$  are constructed using  $d\ln V_S$  and  $d\ln V_P$ , thus giving rise to small-scale artefacts that should not be interpreted.



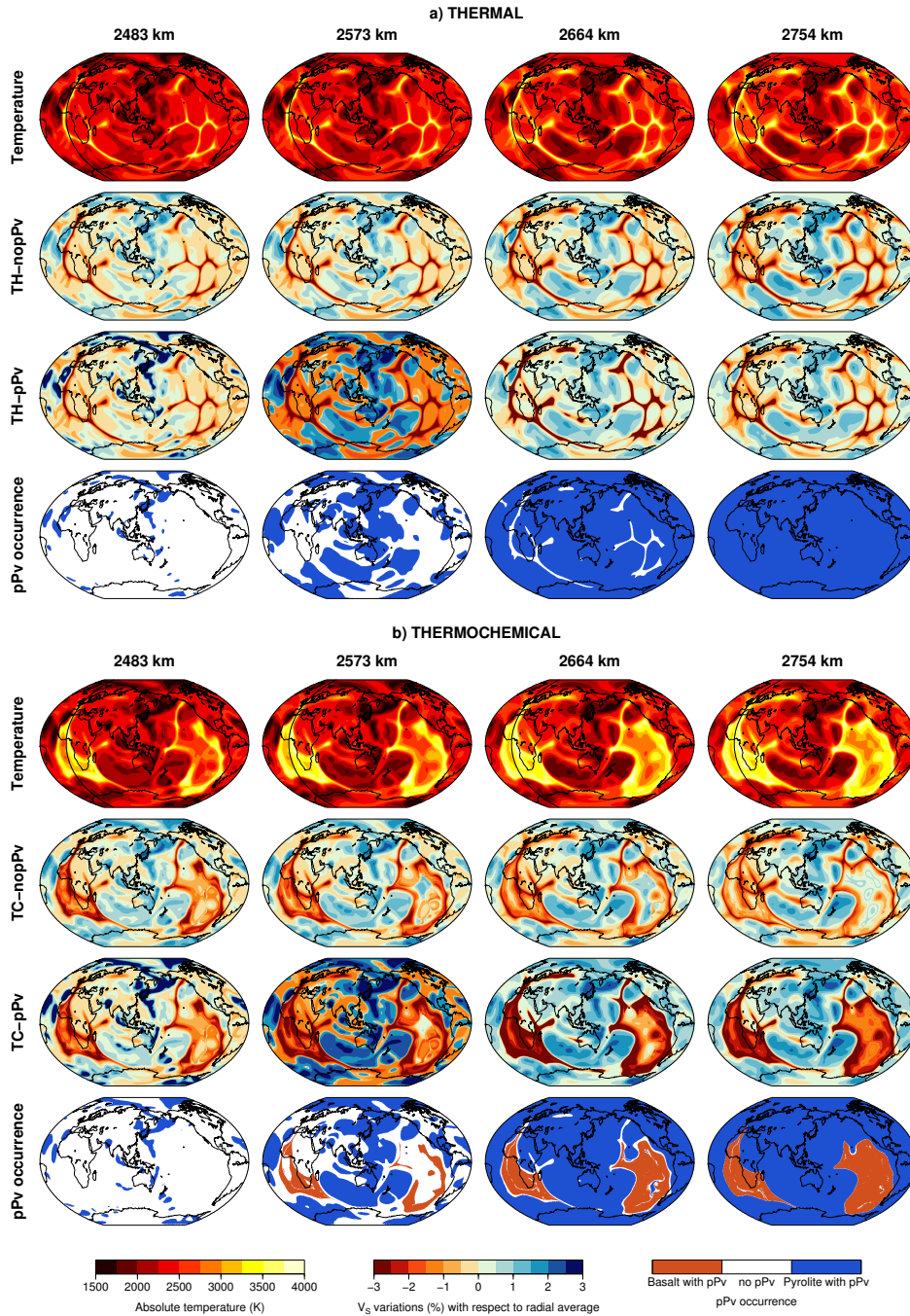


Figure 3: Temperature, shear-wave velocity variations and pPv occurrence maps for (a) thermal (TH) models and (b) thermochemical (TC) models at different depths in the low-  
 41  
 ermost mantle. In each case, the top row shows the absolute temperature field (generated by the geodynamic modelling), the middle rows show the  $V_S$  structure (based on the mineral physics conversion) without and with pPv present, respectively, and the bottom row shows the lateral variations in pPv occurrence. For the shear-wave velocity variations, we remove the radial average at each depth.

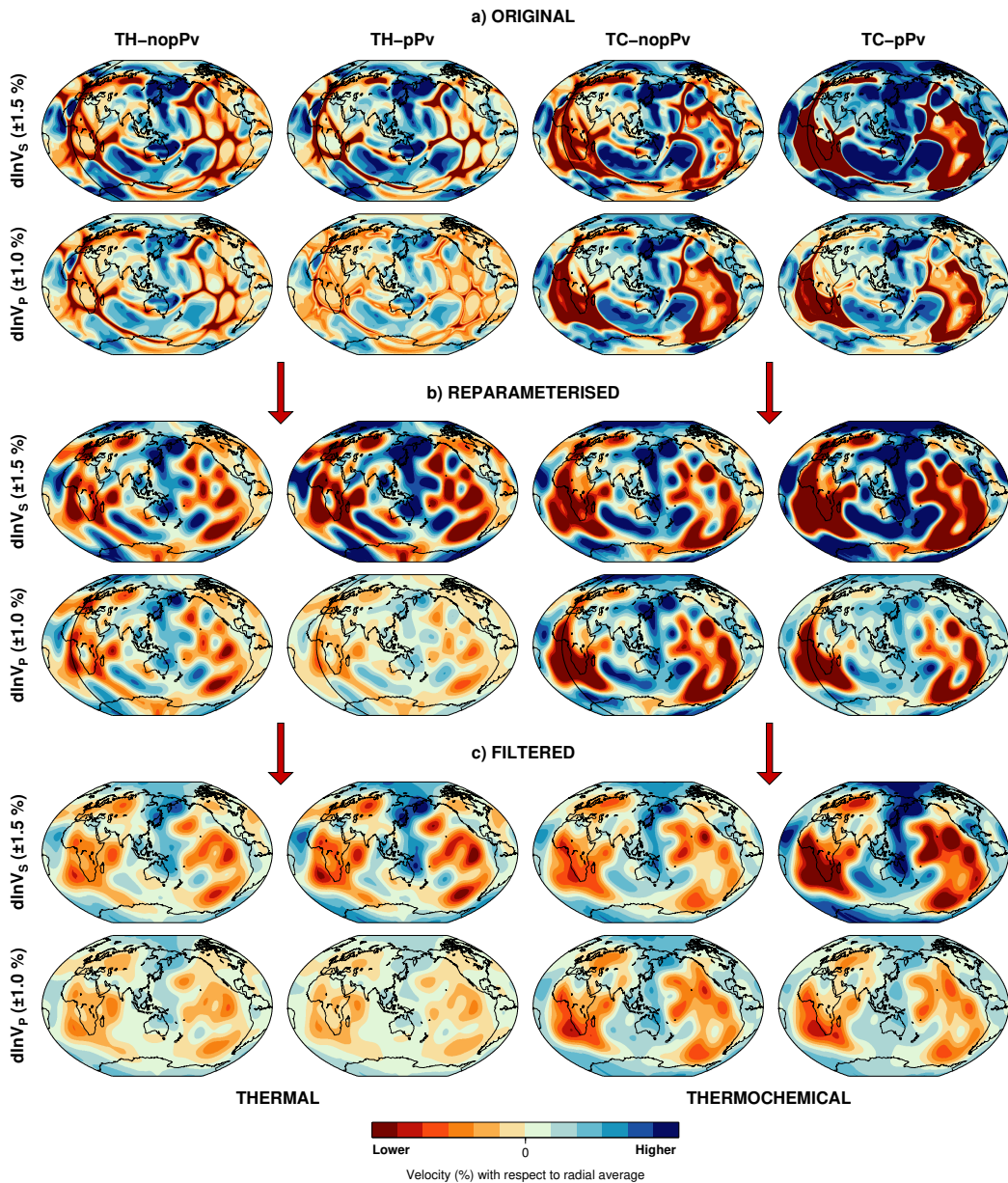


Figure 4:  $d\ln V_S$  (top) and  $d\ln V_P$  (bottom) at 2650 km depth for (a) the original high-resolution geodynamic models, (b) the reparameterised geodynamic models and (c) the tomographically filtered geodynamic models. The colour scale is the same as in Fig. 2 with a maximum amplitude of 1.5 % for  $d\ln V_S$  and 1.0 % for  $d\ln V_P$ . The reparameterisation affects  $d\ln V_S$  and  $d\ln V_P$  structures in a similar way. Subsequently, the multiplication with  $\mathcal{R}$  decreases both fast and slow anomalies by  $\sim 35\text{-}50\%$ , consistent with findings by (Zaroli et al., 2017). The effect of pPv remains evident after filtering, with models including pPv showing larger amplitudes for  $d\ln V_S$  and lower amplitudes for  $d\ln V_P$ .

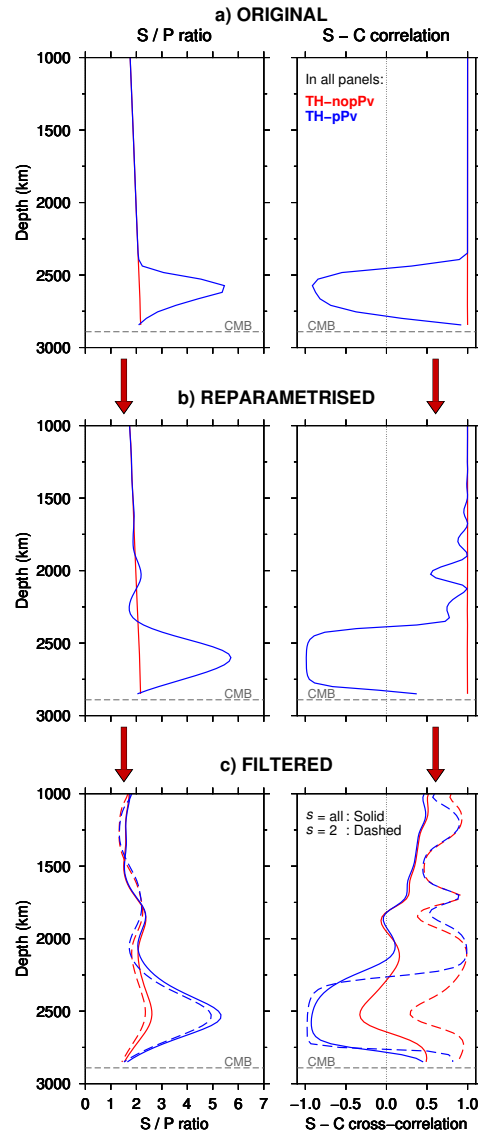


Figure 5: Effects of reparameterisation and tomographic filtering on the S/P ratio (left) and S-C correlation (right) for thermal (TH) models. (a) Original high-resolution geodynamic models, (b) reparameterised geodynamic models and (c) tomographically filtered geodynamic models. Red and blue lines show thermal models without pPv (TH-nopPv) and with pPv (TH-pPv), respectively, with dashed lines in (c) indicating the degree 2 component only.

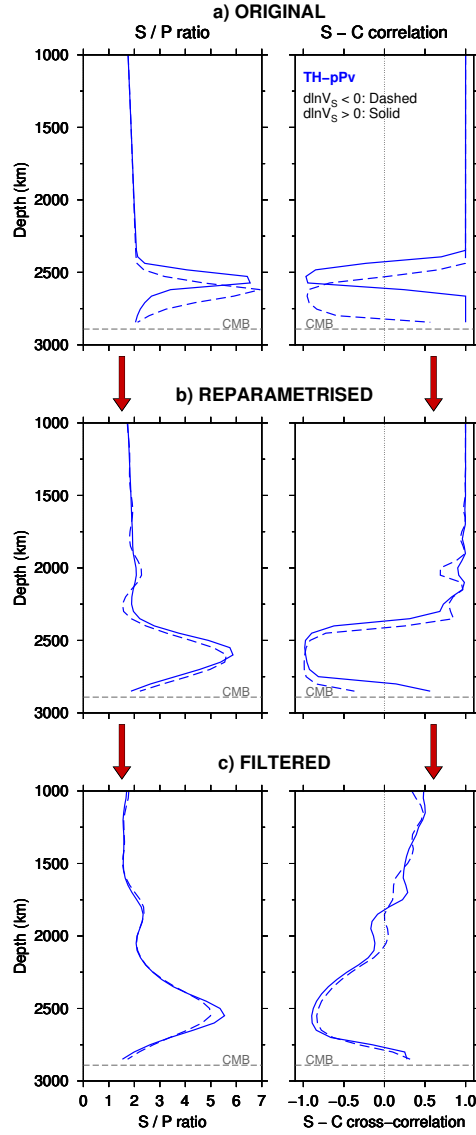


Figure 6: The S/P ratio (left) and S-C correlation (right) in thermal model TH-pPv with post-perovskite present, separated into regions of fast (solid) and slow (dashed) shear-wave velocity variations. (a) Original high-resolution, (b) reparameterised, and (c) tomographically filtered geodynamic models.

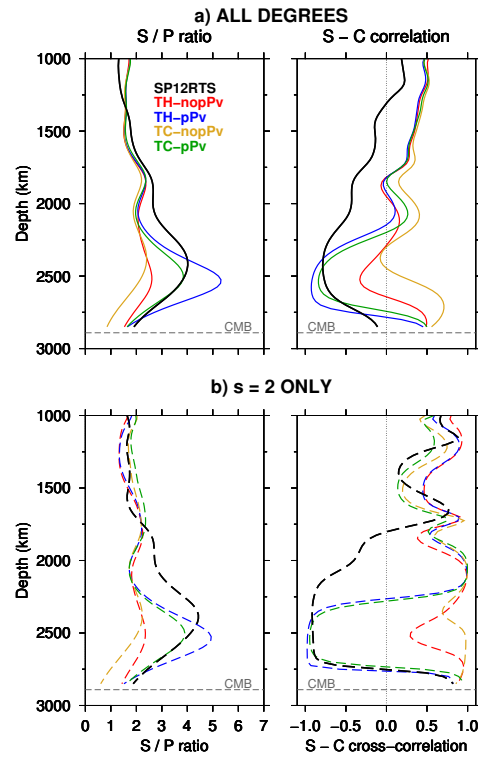


Figure 7: Comparison of the S/P ratio (left) and S-C correlation (right) between the geodynamic models and SP12RTS for (a) all spherical harmonic degrees up to  $s = 12$  and (b) degree  $s = 2$  only (dashed lines). Black lines show the characteristics of SP12RTS, whereas different colours represent the geodynamic models, as indicated in the figure.

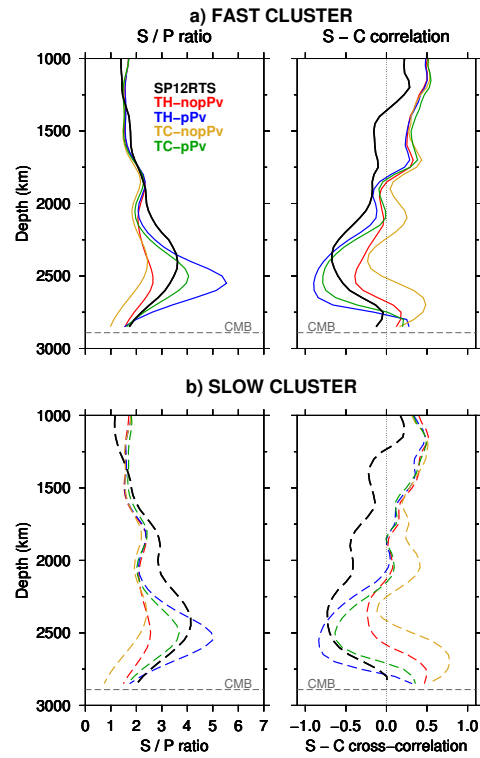


Figure 8: Comparison of the S/P ratio (left) and S-C correlation (right) calculated for (a) the fast cluster and (b) the slow cluster for all geodynamic models and SP12RTS. Colours are the same as in Fig. 7.

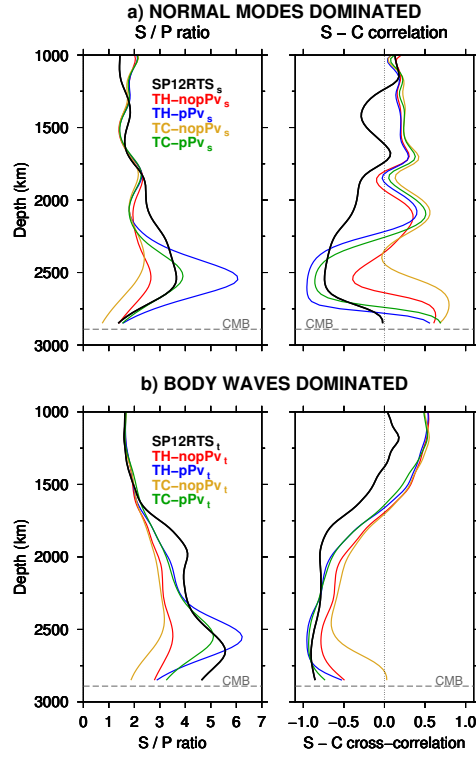


Figure 9: Comparison of the S/P ratio (left) and S-C correlation (right) between geodynamic models and tomographic models obtained with different data weighting (i.e. SP12RTS<sub>s</sub> and SP12RTS<sub>t</sub> for inversions dominated by normal-mode and body-wave data, respectively), calculated for all spherical harmonic degrees. (a) Normal-mode data dominated inversion. (b) Body-wave data dominated inversion. The same colours as in Fig. 7 represent the geodynamic models, but we now filter them using either (a)  $\mathcal{R}_s$  or (b)  $\mathcal{R}_t$ .



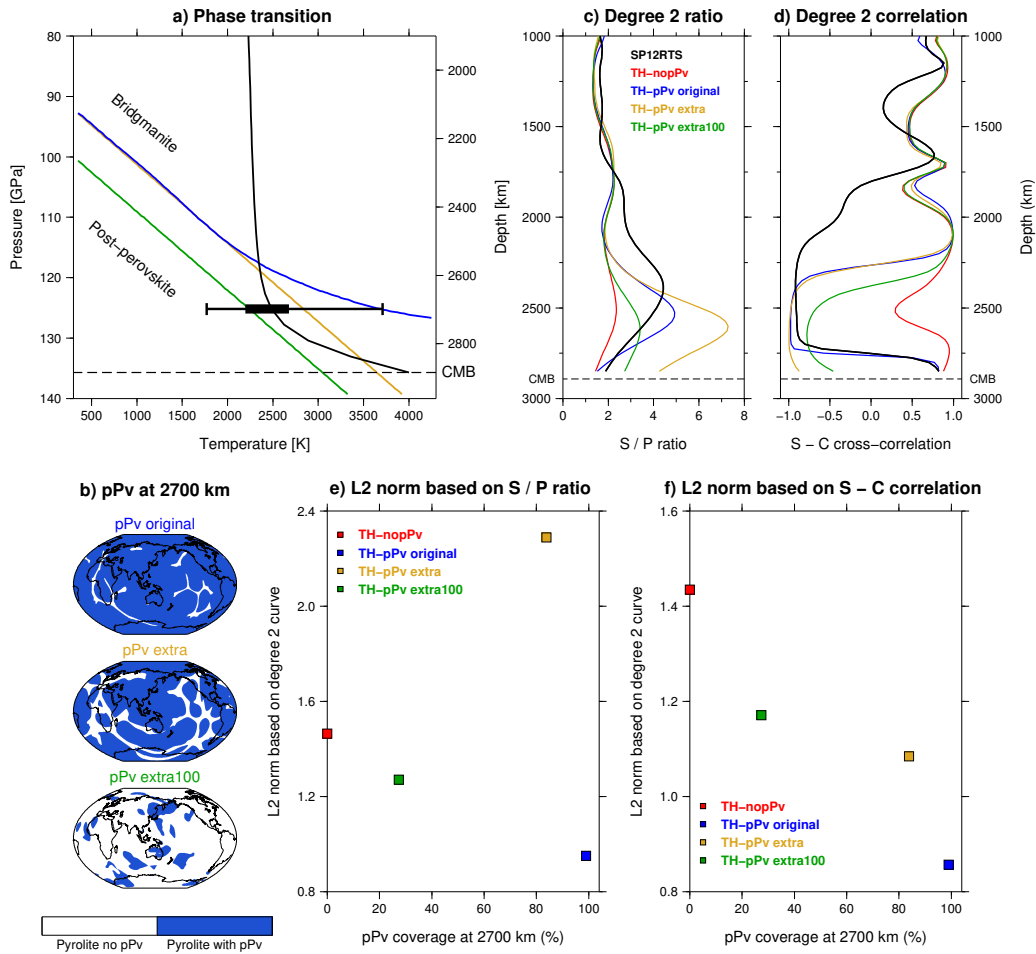


Figure 10: Effect of (a) different Clapeyron slopes of the phase transition in pyrolite on (b) the amount of pPv in the lower mantle, (c) the S/P ratio and (d) the S-C correlation. (e) and (f) show the L2 norm between SP12RTS and the geodynamic models, based on the degree-2 curves of either (e) the S/P ratio or (f) the S-C correlation. The black line in (a) gives the geotherm of the TH model and the boxcar indicates the 1, 25, 75 and 99 % percentiles of the temperature distribution at 2700 km depth. The resulting pPv occurrence maps in (b) contain either pPv everywhere at the CMB for the original mineral physics table (blue) or contain pPv lenses in the colder regions for the extrapolated tables “extra” (yellow) and “extra100” (green). The patterns in the S/P ratio (c) and S-C correlation (d) curves for degree 2 of SP12RTS (black) are matched best by the original mineral physics table (blue).