

# Empirical fragility curves: The effect of uncertainty in ground motion intensity

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**Abstract:** Empirical fragility curves derived from large post-disaster databases with data aggregated at municipality-level, commonly make the assumption that the ground motion intensity level is known and is determined at the centroid of each municipality from a ground motion prediction equation. A flexible Bayesian framework is applied here to the 1980 Irpinia database to explore whether more complex statistical models that account for sources of uncertainty in the intensity can significantly change the shape of the fragility curves. Through this framework the effect of explicitly modelling the uncertainty in the intensity, the spatial correlation of its intra-event component and the uncertainty due to the scatter of the buildings in the municipality are investigated. The analyses showed that the results did not change substantively with increased model complexity or the choice of prior. Nonetheless, informed decisions should be based on the defensible modelling of the significant variability in the data between municipalities.

## 1 Introduction

Fragility is an important component of seismic risk and expresses the likelihood of damage sustained by buildings with certain characteristics in future earthquake events [1]. Fragility is commonly presented in terms of fragility curves, defined as the probability that a given building damage state will be reached or exceeded for a given ground motion intensity level, which is termed here  $X$  for simplicity. This study focuses on the empirical assessment of the fragility of buildings based on post-earthquake damage field data. The GEM Compendium database [2] identified 89 sets of empirical fragility curves for various building classes. Although two thirds of these sets determined  $X$  levels from the observed damage, the remaining and most recent curves estimate these levels from pre-selected Ground Motion Prediction Equations (GMPEs). These equations are linear statistical models associated with substantial error, which use ground motion records from past events to predict the  $X$  level at a specific site based on its local soil conditions and the characteristics of the seismic source and event. The importance of this error in the prediction of  $X$  on the seismic risk assessment of spatially distributed assets is well known (e.g., [3-8]). However, despite being extensively studied in the seismic hazard field, the error component of the GMPEs and spatial correlation of  $X$  levels has been largely ignored in the field of empirical fragility assessment of assets. Existing empirical fragility functions are typically based on large databases of observed building damage data that are often aggregated at municipality level. Such municipalities can cover a large geographical area, often with soils of significantly different properties. Yet the assumption is commonly made to represent the ground motion intensity across the municipality with a single best-estimate value of  $X$ , estimated at the centroid of the municipality. These values are estimated either by a GMPE [9] or by a ShakeMap [10]. In the latter case, the  $X$  best-estimates are determined by a GMPE whose outputs are calibrated with the earthquake ground motion records for the studied event at nearby stations. In 2014, a sensitivity study on fictitious data [11] showed that uncertainty in  $X$  can lead to significantly flatter empirical fragility curves. Moreover, the uncertainty in  $X$  levels has been explicitly

33 taken into account in the construction of empirical fragility curves of elements of electrical stations  
34 affected by successive earthquakes by Straub & Der Kiureghian [12], who developed a Bayesian frame-  
35 work to model multiple sources of uncertainties. More recently, Yazgan [13-15] highlighted the im-  
36 portance of modelling both the uncertainty in  $X$  levels and the spatial correlation of the levels in nearby  
37 sites using a Bayesian framework. Their framework combined existing analytical fragility curves for 4-  
38 storey RC buildings with data from 516 individual buildings affected by the 1999 Düzce and 2003 Bin-  
39 göl earthquakes.

40  
41 Despite recent advances, it is not well understood whether the uncertainty in the  $X$  levels, their spatial  
42 correlation or the presence of ground motion records is important in the construction of empirical fra-  
43 gility curves using large databases, which are aggregated at municipality level. The present paper ad-  
44 dresses this. A Bayesian framework is adopted here as it offers a natural and flexible way to assimilate  
45 multiple sources of uncertainty in a principled and transparent manner, as well as to combine available  
46 damage databases with prior knowledge accumulated over the past 40 years of research in the field of  
47 fragility assessment of buildings. Nonetheless, such framework requires a high degree of skill to imple-  
48 ment. Therefore, the sensitivity analysis performed here aims to explore whether the explicit modelling  
49 of sources of uncertainty typically ignored in the literature leads to a significantly different shape of the  
50 fragility curves, and assesses whether a Bayesian framework is needed. In the empirical fragility assess-  
51 ment literature, fragility is typically expressed in terms of the best-estimate fragility curve ignoring the,  
52 often substantial, uncertainty in its shape. This uncertainty, however, needs to be quantified in a defen-  
53 sible way if the curves are to be considered useful as part of an informed risk assessment. In the adopted  
54 Bayesian framework, this uncertainty can be summarized using credible intervals. Therefore, the relative  
55 contribution of modelling different sources of uncertainty around the ground motion as well as the im-  
56 pact of the presence of ground motion records is assessed here by examining how they change the cred-  
57 ible intervals of the fragility curves. Overall, five statistical models of increasing complexity are  
58 developed as part of this study. The models are then fitted to the well-studied 1980 Irpinia damage  
59 database and the constructed fragility curves are compared to existing fragility curves, which are also  
60 based on the 1980 Irpinia data.

## 61 **2 The 1980 Irpinia Earthquake Building Damage Database**

62 On 23<sup>rd</sup> November 1980, the Campania-Basilicata region was affected by a strong earthquake, with  
63 magnitude  $M_w = 6.9$ . Fig.1 highlights the 41 municipalities [16] for which post-earthquake damage data  
64 have been collected. In what follows, the building inventory, the damage scale used for the classification  
65 of the sustained damage and the ground motion intensity at each municipality are briefly presented.

66

67 *Fig.1 Map of the Campania-Basilicata region affected by the 1980 Irpinia earthquake.*

### 68 **2.1 Intensity measure**

69 The Campania – Basilicata region is located in Southern Italy along the Southern Appeninic chain,  
70 known for its high seismicity [17]. The 1980 event was the first strong event to occur since 1930. This  
71 moderately large event occurred at 19:34 local time on 23<sup>rd</sup> November 1980. The event was generated  
72 by a complex normal fault [18]. Fig.1 depicts the epicenter of the event and the projection of the fault  
73 to the surface. In an ideal world, each surveyed building should have a ground motion recording station  
74 installed so the actual ground motion intensity level at its known location could be recorded. In reality,  
75 there is a general lack of dense networks of recording stations and the buildings, especially in large  
76 databases such as the 1980 Irpinia damage database, are aggregated at municipality level. Both the lack  
77 of recordings and the data aggregation pose challenges as to how best to determine the actual ground  
78 motion intensity.

79 For the 1980 Irpinia event, the actual ground shaking caused by the main shock was recorded by 17  
80 stations scattered in the Campania-Basilicata region as depicted in Fig.1 [19]. These stations are typi-  
81 cally located in municipalities for which no damage data have been collected, with the exception of  
82 Arienzo (see Fig.1), where there is a nearby station, but this is not however included in the municipality.  
83 Given this, a popular approach is to determine the actual intensity measure level,  $x_j$ , at the geometrical  
84 centre of a given municipality,  $j$ , through a pre-selected GMPE. The use of the INGV ShakeMap is not  
85 deemed suitable in this study, as it is based on a larger scale geological map (1:100,000) than the one  
86 used in this study (1:50,000), it provides PGA estimated aggregated in bins of 0.4g and it does not  
87 differentiate between the different sources of uncertainty.

88 A typical GMPE is a function of the magnitude of the event,  $M$ , the source-to-point distance,  $R_j$ , the soil  
89 conditions,  $S_j$ , and the fault type,  $F$ . Nonetheless, the GMPE is not perfect and cannot capture the full  
90 variation in intensities, so that it is necessary to introduce a representation of the GMPE errors in order  
91 to fully reconcile the GMPE with the actual intensities. In modern GMPEs [20-22], the actual ground  
92 motion intensity is determined by explicitly accounting for an event-specific source of error and a spa-  
93 tially varying one. The event-specific error accounts for the fact that there will typically be unobserved  
94 features of an event that cause a GMPE to systematically over- or under- predict the actual intensity  
95 everywhere for a given event, although it may be unbiased “on average” over a large number of events.  
96 The spatially varying error accounts for the possibility that the precise parameterisation of the GMPE  
97 may not be appropriate for all events – for example, in a given event the decay rate of intensity with  
98 distance from the source may differ from that assumed in the GMPE due to differences of the wave path  
99 or local site conditions. In general, a GMPE determines the actual ground motion intensity level at the  
100 centroid of a municipality  $j$ ,  $x_j$ , as:

$$101 \quad \ln(x_j) = f(M, R_j, S_j, F) + \phi + \varepsilon_j \quad (1)$$

102 where  $\phi$  is the event-specific error which is typically termed inter-event error; and  $\varepsilon_j$  which is the error  
103 spatially varying within a given event and is known as the intra-event error. Both of these variables are  
104 considered normally distributed, with mean equal to 0 and variance equal to  $\sigma_{\text{inter}}^2$  and  $\sigma_{\text{intra}}^2$ , respec-  
105 tively. Existing empirical fragility assessment studies, however, do not use Eq.(1) to determine the actual  
106 intensity levels. Instead, they ignore the two error components and they assign the estimated level of  
107 intensity at the centroid of each municipality, which can be obtained by rewriting Eq.(1) as:

$$109 \quad \ln(\tilde{x}_j) = f(M, R_j, S_j, F) \quad (2)$$

110  
111 The term ‘estimated intensity’ is used wherever the intensity level is determined by Eq.(2). The focus  
112 of the present study is to examine whether the explicit modelling of the actual, rather than the estimated,  
113 ground motion intensity leads to significantly different shape of fragility curves.

114 The identification of the most appropriate GMPE is not straightforward given the years of systematic  
115 research on Italian earthquakes, which produced a plethora of GMPEs. For this reason, three recent  
116 GMPEs [23-25], which explicitly model the two sources of error, are selected and their main character-  
117 istics are presented in Table 1. All three have used the ground motion records from the 1980 Irpinia  
118 earthquake and use the Peak Ground Acceleration (PGA) as a measure of ground motion intensity. PGA  
119 is adopted here as it is considered an efficient measure to predict the response of low-rise buildings with  
120 low ductility [26], which represent the majority of the building inventory in the Campania – Basilicata  
121 region affected by the earthquake, and it is a widely used measure of intensity in empirical fragility  
122 assessment studies [2].

123 *Table 1: Main characteristics of the three GMPEs adopted in this study.*

Study	Equation	PGA range in g

Bindi et al. [23]	$\log_{10}(x_j) = F_D + F_M + F_S + F_{sof} + \phi + \varepsilon_j$ , where $\sigma_{inter} = 0.18, \sigma_{intra} = 0.28$	[0.01, 0.64]
Kotha et al. [24]	$\ln(x_j) = F_D + F_M + F_S + F_{sof} + \phi + \varepsilon_j$ , where $\sigma_{inter} = 0.35, \sigma_{intra} = 0.57$	[0.01, 0.43]
Akkar et al. [25]	$\ln(x_j) = \ln[x_{REF}(M_w, R, F)] + \ln[(S, PGA_{REF})] + \phi + \varepsilon_j$ , where $\sigma_{inter} = 0.35, \sigma_{intra} = 0.62$	[0.01, 0.44]

124

125 In Fig.2, the PGA values from the 17 ground motion records are compared to the estimated PGA values  
126 at the location of the 17 stations based on the three GMPEs in the log-log scale. It can be seen that all  
127 three GMPEs provide PGA estimates with a sizeable uncertainty. Nonetheless, the Bindi et al. [23]  
128 GMPE appears to provide a better fit as the data points seem to be symmetrically scattered around the  
129 45-degree line as opposed to the other two GMPEs [24, 25] which tend to overestimate the PGA values.  
130 Having established that Bindi et al. GMPE predicts the recorded PGA levels better than the other two,  
131 in section 3.1.1 it is further examined whether Bindi et al. [23] GMPE also fits the damage data better.  
132 In this study, the GMPE found to fit the damage data better than its alternatives would be selected to  
133 determine the PGA levels required for the fragility assessment.

134

135 *Fig.2 Recorded (Rec. PGA) PGA values from 17 stations vs estimated (Est. PGA) PGA values for the*  
136 *same locations using the GMPEs proposed by Bindi et al. [23], Kothal et al. [24] and Akkar et al.*  
137 *[25] in log-log scale.*

## 138 2.2 Building inventory

139 The database includes information from 29,661 buildings, which are considered to be a representative  
140 and unbiased sample of the total number of buildings located in the affected region. 89% of the surveyed  
141 buildings are masonry. Information regarding their vertical and horizontal construction materials is in-  
142 cluded in the database. In Table 2, it can be seen that masonry buildings are built mainly using field  
143 stone (63%), and to a lesser degree hewn stone (32%). Brick masonry buildings appear to be the least  
144 common in the affected region. It can also be noted that 47% of the surveyed masonry buildings have  
145 wooden floors, followed, in decreasing frequency, by steel (30%) and RC (13%) floors. Masonry build-  
146 ings constructed with vaults are the least common in the affected region. Reinforced concrete (RC)  
147 buildings are also present in the affected region. The RC buildings have been built either without a  
148 seismic design code or with an old seismic design code.

149 *Table 2: Classification of buildings to vulnerability classes according to their vertical and horizontal*  
150 *structure [16].*

Structure	Vertical			
	Field Stone	Hewn Stone	Brick Masonry	RC
Vaults	A (1,532)	A (617)	A (16)	-
Wood	A (8,860)	A (3,294)	C (132)	-
Steel	B (5,216)	B (2,323)	C (468)	-
RC	C (855)	C (2,060)	C (601)	C (3,383)

151

152 If the buildings are classified into 13 classes according to their vertical and horizontal structure, this  
153 results in some classes having a very small number of buildings (see Table 2). To avoid very small

154 samples, the 13 building classes are reduced to the three vulnerability classes (i.e., A, B and C) following  
 155 the re-classification approach found in Braga et al. [16] (see Table 2). The vulnerability class ‘A’ is the  
 156 best represented class in the database with overall 14,406 buildings. Class A is considered the most  
 157 vulnerable class as it includes the worst quality masonry buildings. Poor quality masonry buildings are  
 158 considered to have floors made of vaults or to have been constructed using field or hewn stone and  
 159 wooden floors (see Table 2). The damage database also includes 7,816 class B buildings. This class  
 160 includes the better quality field or hewn stone buildings, which have steel floors. Finally, Class C in-  
 161 cludes the least vulnerable buildings, having similar sample size with the latter class. The present study  
 162 concentrates on the most vulnerable (Class A) and the least vulnerable (Class C) classes of buildings to  
 163 present the results.

### 164 2.3 Damage scale

165 The damage sustained by the surveyed buildings has been classified into six discrete damage states  
 166 according to the MSK-76 scale [27]. The six damage states characterize all possible levels of damage  
 167 that a building can suffer, and are described briefly in Table 3.

168 Fig.3 shows the relationship between the estimated *PGA* level in each municipality and the percentages  
 169 of Class A and C buildings sustaining damage state  $ds_i$  or above ( $i=1, 2, 5$ ). Overall, damaged data  
 170 from 14,406 Class A and of 7,439 C buildings aggregated in 41 data points. This is substantially larger  
 171 than the minimum sample size required for the construction of meaningful fragility curves provided by  
 172 the Global Earthquake Model, empirical vulnerability assessment guidelines [30]. According to the lat-  
 173 ter, at least 200 buildings are required to be aggregated in a minimum of 10 data points. Over 80% of  
 174 the data points, (representing 70% of the building inventory), are clustered in the lower *PGA* levels, i.e.,  
 175 0.024g to 0.30g. This scarcity of data for the higher intensity measure levels is not unusual. Moreover,  
 176 the total number of recorded buildings in each municipality varies according to the building class: for  
 177 example, there are no municipalities with fewer than 50 Class A buildings, but 35 municipalities with  
 178 fewer than 50 Class C buildings.

179 *Table 3: Description of damage in each damage state [27].*

<i>DS</i>	Description:
$ds_0$	No damage
$ds_1$	Negligible or slight damage
$ds_2$	Moderate damage
$ds_3$	Substantial to heavy damage
$ds_4$	Very heavy damage
$ds_5$	Destruction

180  
 181 In Fig.3, the poor performance of class A buildings in the 1980 earthquake is highlighted, as in all 41  
 182 municipalities at least half of class A buildings sustained some level of damage (i.e.,  $DS \geq ds_1$ ) and 6%  
 183 of the total class A buildings located in over 70% municipalities had been destroyed. Overall, each  
 184 municipality appears to have recorded more damaged class A buildings with  $DS \geq ds_i$  than class C  
 185 buildings. In addition, the scatter in their data points appears to be wider than for class C buildings for  
 186 higher damage states; indicating that there is greater uncertainty in the seismic performance of class A  
 187 buildings for higher damage states. This is in line with observations in the literature regarding the high  
 188 uncertainty in the seismic performance of low quality masonry buildings [28].

189  
 190 The better seismic performance of class C buildings is also depicted in Fig.3, where in most (71%)  
 191 municipalities, less than half of the surveyed Class C buildings sustained some level of damage. The  
 192 highest scatter in the data points can be seen for  $ds_1$  and this substantially reduces for the higher damage  
 193 states. A closer examination of the data shows that the highest percentage of buildings in any given  
 194 municipality sustaining moderate damage or above (i.e.,  $DS \geq ds_2$ ) never exceeds 40%. and that in 80%

195 of the municipalities no Class C buildings have been destroyed (n.b. there are only 52 cases of collapsed  
 196 Class C buildings). Therefore, very little information is available from which to construct fragility curves  
 197 for the most severe damage states, for buildings with good seismic performance. This is a known issue  
 198 in the empirical fragility assessment literature [29] and limits the ability of empirical approaches to  
 199 determine the likelihood of collapse of buildings which perform well during earthquakes.

### 200 **3 Empirical fragility assessment**

201 The information regarding the damage, the intensity levels and building class are combined in order to  
 202 empirically assess the fragility of class A and C buildings for three damage states (i.e.  $ds_1$ ,  $ds_2$  and  $ds_5$ ).  
 203 Two simplifications, are deemed necessary to substantially reduce the amount of time required to run  
 204 each Bayesian analysis. Firstly, the fragility curves are constructed independently for each damage state  
 205 instead of exploiting the ordinal nature of the damage scale. Secondly, the fragility curves are con-  
 206 structed independently for Class A and C.

207  
 208 Past studies commonly base their empirical fragility assessment of buildings on three main assumptions  
 209 regarding the quality of the post-earthquake database. According to these assumptions, the database is  
 210 considered representative of the seismic damage in the affected area, the misclassification error in as-  
 211 signing the ‘actual’ damage states to each building is considered insignificant and the uncertainty in the  
 212  $X$  level can be ignored [30]. In what follows, a reference model based on these assumptions is developed  
 213 and fitted to the 1980 Irpinia data. Then, the importance of different sources of uncertainty in the ground  
 214 motion intensity is examined by developing and fitting four models of increasing complexity. At each  
 215 stage, the effect of accounting for additional information or uncertainties is assessed by examining the  
 216 fitted fragility curves and their credible intervals. Finally, the most realistic fragility curves are con-  
 217 structed by combining the 1980 Irpinia damage data with prior information regarding the fragility of the  
 218 Class A and C buildings.

#### 219 **3.1 Models M0-M1: Reference models**

220 Many existing studies adopt a parametric statistical model, whose systematic component is typically  
 221 expressed in terms of the cumulative lognormal distribution, and with random component following  
 222 various assumptions that are often unrealistic and whose impact on the fragility is discussed in greater  
 223 detail in [31]. The present study adopts a Generalised Linear Model (termed GLM) which is proposed  
 224 by the Global Earthquake Model (GEM) Guidelines [30]. A GLM assumes that the number of buildings,  
 225  $y_{ij}$ , which sustained damage  $DS \geq ds_i$  in municipality,  $j$ , follows a binomial distribution:  
 226

$$227 \quad y_{ij} \sim \text{Binomial}\left(n_j, \pi_i(\tilde{x}_j)\right) \quad (3)$$

228  
 229 where  $\pi_i(\tilde{x}_j)$  is the probability that a building located in municipality,  $j$ , will reach or exceed the ‘true’  
 230 damage state,  $ds_i$ , given estimated intensity level  $\tilde{x}_j$ ;  $n_j$  is the total number of buildings of the examined  
 231 building class in municipality,  $j$ . The binomial distribution is characterised by its mean:

$$232 \quad \mu_{ij} = n_j \pi_i(\tilde{x}_j) \quad (4)$$

233 which is expressed here in terms of a probit model defined in terms of  $\Phi(\cdot)$ , the cumulative distribution  
 234 function of a standard normal distribution:  
 235

$$236 \quad \Phi^{-1}\left[\pi_i(\tilde{x}_j)\right] = \eta_{ij} \quad (5)$$

237  
 238 where  $\eta_{ij}$  is the linear predictor, which can be written in the form:

$$239 \quad \eta_{ij} = \theta_{0i} + \theta_{1i} \ln(\tilde{x}_j) \quad (6)$$

241 Here,  $\theta_{1i}$ ,  $\theta_{0i}$  are the two regression coefficients, representing the slope and the intercept, respectively,  
 242 of the fragility curve corresponding to damage state  $ds_i$ . For the reference model, the ground motion  
 243 intensity level,  $\tilde{x}_j$ , is estimated at the geographical centre of municipality  $j$  from a pre-selected GMPE,  
 244 ignoring the two error components in Eq.(1). Throughout the remainder of the paper, the reference model  
 245 fitted to the data using a maximum likelihood approach is referred to as M0; the same model fitted using  
 246 a Bayesian approach is denoted M1. We next describe the two approaches, and highlight the differences  
 247 between them.  
 248

### 249 3.1.1 M0 – The maximum likelihood approach

250 In a maximum likelihood approach, the regression coefficients and their standard error are determined  
 251 from the log-likelihood function [32], as:  
 252

$$253 \quad \boldsymbol{\theta} = \arg \max L(\boldsymbol{\theta}) = \arg \max \log \left\{ \prod_{j=1}^M \left[ \binom{n_j}{y_{ij}} \mu_{ij}^{y_{ij}} (1 - \mu_{ij})^{n_j - y_{ij}} \right] \right\} \quad (7)$$

254 where  $M$  is the total number of municipalities. It should be noted that for data aggregated at municipality  
 255 level, the variability between municipalities is often greater than expected under the binomial distribu-  
 256 tion: a phenomenon known as “over-dispersion”, which can be caused due to aggregation of non-homo-  
 257 geneous data in municipalities or the failure to account for other explanatory variables (for example,  
 258 because their data are not available). Where over-dispersion occurs, standard errors for the regression  
 259 coefficients will be underestimated, which in turn leads to underestimation of the uncertainty in the  
 260 estimated fragility curves. A standard way to deal with over-dispersion in such situations is to carry out  
 261 a “quasi-binomial” GLM fit [33], which provides an empirical adjustment to the standard errors to en-  
 262 sure that they correctly reflect the estimation uncertainty [34]. M0 is fitted to the data with estimated  
 263 PGA levels from the three GMPEs. Due to the limited space in this study, the results are presented only  
 264 for the GMPE that provides the best fit to the data. However, a sensitivity analysis is presented in the  
 265 Appendix in which multiple GMPEs are used. To identify which GMPE fits the damage data best, the  
 266 maximised log-likelihood for all fitted models are compared in Table 4. The Bindi et al [23] GMPE is  
 267 found systematically to have the highest log-likelihood by a considerable margin: this means that the  
 268 PGA levels obtained by this GMPE fit the data best.

269 *Table 4: Maximized log-likelihood values for the three GMPEs.*

GMPE	$ds_1$	$ds_2$	$ds_5$
<b>Class A</b>			
Bindi et al. [23]	<b>-498.2</b>	<b>-981.5</b>	<b>-559.7</b>
Kotha et al. [24]	-612.4	-1305.5	-966.2
Akkar et al. [25]	-589.1	-1249.1	-859.7
<b>Class C</b>			
Bindi et al. [23]	<b>-428.3</b>	<b>-269.3</b>	<b>-44.6</b>
Kotha et al. [24]	-552.7	-430.3	-98.0
Akkar et al. [25]	-561.1	-435.7	-95.0

270 Fig.3 depicts the fragility curves corresponding to  $ds_1$ ,  $ds_2$  and  $ds_5$ , obtained using maximum likelihood  
 271 estimates of the regression coefficients and using the Bindi et al. [23] GMPE to determine the PGA  
 272 levels at the geographical centre of each municipality. Within the range of estimated PGA levels corre-  
 273 sponding to the municipalities for which there are available damage data, the best estimate curves rep-  
 274 resent a small part of the lognormal cumulative distribution function, rather than the full range from 0  
 275 to 1. Overall, the best-estimate fragility curves for Class A buildings appear to be systematically higher  
 276 than their Class C counterparts, highlighting the poor seismic performance of the Class A buildings. The  
 277 values of the regression coefficients are presented in Table 5.

Table 5: Regression coefficients estimates based on M0.

DS	Building Class			
	A		C	
	$\theta_0$	$\theta_1$	$\theta_0$	$\theta_1$
$ds_1$	0.16	0.25	-1.51	0.27
$ds_2$	-1.23	0.29	-3.27	0.40
$ds_5$	-4.73	0.60	-6.14	0.67

279 In Fig.3, the 90% confidence intervals for the ‘true’ fragility curves are plotted accounting for the sam-  
280 pling variation in the damage data according to the fitted “quasi-binomial” model.

### 281 3.1.2 M1 – The Bayesian approach

282 In maximum likelihood estimation, uncertainties about unknown quantities are expressed using standard  
283 errors and confidence intervals. In Bayesian inference by contrast, such uncertainties are expressed by  
284 assigning probability distributions directly to those quantities. Using Bayes’ theorem, the likelihood  
285 function is combined with prior knowledge regarding the probability distribution of the regression co-  
286 efficients in order to obtain the posterior distribution of these coefficients:

$$287 \quad p(\boldsymbol{\theta} | Y) \propto p(\boldsymbol{\theta}) L(\boldsymbol{\theta}) = p(\boldsymbol{\theta}) \prod_{j=1}^M \left[ \binom{n_j}{y_{ij}} \mu_{ij}^{y_{ij}} (1 - \mu_{ij})^{n_j - y_{ij}} \right] \quad (8)$$

288 where  $p(\boldsymbol{\theta})$  is the prior distribution of the vector of parameters  $\boldsymbol{\theta} = [\theta_{0i}, \theta_{1i}]$ ;  $L(\boldsymbol{\theta})$  is the likelihood function.  
289 In the present work, the posterior distribution of the regression coefficients, together with all other quan-  
290 tities of interest, is estimated by the Markov Chain Monte Carlo (MCMC) algorithm, using OpenBUGS  
291 [35]. All posterior distributions of interest are determined from three chains with 90,000 iterations each,  
292 ignoring the first 30,000 iterations. The simulations are fast: each lasts approximately 30 seconds. The  
293 convergence of the MCMC algorithm is assessed by the Gelman-Rubin diagnostic [36], known as Rhat  
294 statistic, which is found to be equal to 1 (to two significant digits) for all analyses, indicating the suc-  
295 cessful convergence of all chains.

296

297 The prior distribution provides a mechanism for incorporating additional information into the analysis  
298 to supplement the available post-earthquake data, if such information is available. For compatibility  
299 with model M0 however, initially we make no attempt to incorporate such information. Thus, the prior  
300 distribution for both regression coefficients (i.e.,  $\theta_{0i}$  or  $\theta_{1i}$ ) is taken to be normal, with zero mean and a  
301 very large variance:

$$302 \quad \begin{aligned} \theta_{0i} &\sim \text{Normal}(\mu_{\theta_{0i}} = 0, \sigma_{\theta_{0i}}^2 = 10^5) \\ \theta_{1i} &\sim \text{Normal}(\mu_{\theta_{1i}} = 0, \sigma_{\theta_{1i}}^2 = 10^5) \end{aligned} \quad (9)$$

303

304 where  $\mu_{\theta_{0i}}$ ,  $\mu_{\theta_{1i}}$  is the prior mean of intercept  $\theta_{0i}$  and slope  $\theta_{1i}$ , respectively;  $\sigma_{\theta_{0i}}^2$  and  $\sigma_{\theta_{1i}}^2$  is their vari-  
305 ance.

306 For model M0, a quasi-binomial fit was used to account for over-dispersion. This type of empirical  
307 adjustment is not possible in a Bayesian framework however, so an alternative approach must be sought.  
308 In model M1 therefore, over-dispersion is explicitly modelled by adding a random effect at municipality  
309 level to the linear predictor [37]. Equation (4) is therefore modified to:

$$310 \quad \eta_{ij} = \theta_{0i} + \theta_{1i} \ln(\tilde{x}_j) + \xi_j \quad (10)$$

311 )

312 where the  $\{\xi_j\}$  are random variables, realised independently for each municipality, which are considered  
 313 normally distributed with:

$$314 \quad \xi_j \sim Normal\left(\mu_{\xi_j} = 0, \tau^2\right) \quad (11)$$

315 with  $\tau^2$  is the variance. The size of this variance determines the size of the over-dispersion [37]. For  
 316 example, when  $\tau^2=0$ , the model reduces to the binomial, otherwise the over-dispersion is taken into  
 317 account. In OpenBUGS [35], the normal distribution is modelled in terms of its inverse variance instead  
 318 of its variance. The inverse variance, termed precision, is here assigned a non-informative prior distri-  
 319 bution in the form of a gamma distribution with mean 1 and variance equal to 100.

320 In Fig.3, the best estimate fragility curves obtained from the Bayesian approach are compared to their  
 321 counterparts obtained by the maximum likelihood approach. The 90% credible intervals around the best  
 322 estimates are also plotted. These credible intervals are much wider than the corresponding confidence intervals  
 323 from the maximum likelihood method. This is predominantly due to the slightly different model formulations in  
 324 the two methods. In model M0, a single fixed fragility curve is assumed for all municipalities and the scatter of  
 325 observations is accounted for via an empirical adjustment for overdispersion: the confidence intervals for this  
 326 model represent uncertainty about the single fixed curve. In model M1 however, the scatter of observations is  
 327 attributed to municipality-specific fragility curves defined via the random effects in Eq.(10): the credible intervals  
 328 here represent uncertainty about the fragility curve for an individual municipality. The differences are most  
 329 notable for the curves corresponding to  $ds_2$  for Class A and  $ds_1$  for Class C, which are associated with  
 330 the highest scatter in the data points. It should be noted that a smaller sample size would increase the  
 331 uncertainty around the fragility curves leading to wider credible intervals. That would reduce the differ-  
 332 ences between the models.

333

334 *Fig.3 The data points represent the proportion of buildings of a given class (A or C) in each municipal-*  
 335 *ity, which sustained damage greater or equal to a given damage state  $ds_i$ . The size of each data point*  
 336 *varies according to the total number of buildings of a given class located in a municipality. Best estimate*  
 337 *fragility curves and their corresponding 90% confidence and the 90% credible intervals comparing M0*  
 338 *vs M1 are also presented.*

### 339 3.2 Exploring the importance of the uncertainty in X

340 A sensitivity analysis is performed in order to examine whether the shape of the fragility curves is in-  
 341 fluenced by explicitly accounting for the error component in the GMPE, the spatial correlation in the  
 342 intra-event component, the uncertainty due to the spread of the buildings in each municipality and the  
 343 presence of ground motion records. To achieve that, four models (termed M2-M) are constructed here  
 344 which explicitly account for the additional sources of uncertainty, the spatial structure of the data or the  
 345 presence of the ground motion records. The models increase in complexity as depicted in Table 6.

346 *Table 6: Summary of the five models used in this study.*

Model	Over-dis- persion	Uncer- tainty in X	Spatial Correla- tion in intra event component	Uncertainty due to the spread of buildings in each municipality	Presence of ground motion records.
M1	x	-	-	-	-
M2	x	x	-	-	-
M3	x	x	x	-	-
M4	x	x	x	x	-
M5	x	x	x	x	x

347

348 The fits of these models to the 1980 Irpinia data using the Bayesian approach are then compared to each  
 349 other and to the reference model, M1. The fit is compared in terms of the best-estimate fragility curve

350 as well as the 90% credible intervals. The conclusions were found to be the same if alternative credible  
 351 intervals levels (e.g., 75% or 95%) were preferred. In order for the results to be directly comparable,  
 352 non-informative prior distributions are assigned to the two regression coefficients: the effect of prior  
 353 choice is addressed later. For these models, the posterior distributions of the probability that a damage  
 354 state will be reached or exceeded by the buildings of a given class for a range of PGA levels are deter-  
 355 mined by three MCMC chains with 150,000 iterations each, ignoring the first 30,000 iterations. Each  
 356 analysis lasts approximately 12 minutes. The convergence of the MCMC algorithm is assessed by the  
 357 Rhat convergence statistic, which is found to be approximately equal to 1 for all analyses, indicating the  
 358 successful convergence of the three chains.

### 359 3.2.1 M2 – Accounting for the error components in GMPE

360 A new model M2 is constructed here, which shares Eq.(2) to Eq.(6) with M1, but considers the actual  
 361 ground motion intensity,  $x_j$ , at the center of municipality  $j$  by explicitly modelling the two error terms in  
 362 Eq.(1). The inter-event error  $\phi$  is common to all municipalities. As a first attempt to account for the  
 363 intra-event errors  $\{\varepsilon_j\}$ , they are considered to be mutually independent in model M2 and to follow iden-  
 364 tical normal distributions:

$$366 \begin{aligned} \phi &\sim N(\mu_\phi, \sigma_\phi^2) \\ \varepsilon_j &\sim N(\mu_{\varepsilon_j}, \sigma_{\varepsilon_j}^2) \end{aligned} \quad (12)$$

367 where  $\mu_\eta, \mu_{\varepsilon_j}$  are the mean, which are considered equal to zero;  $\sigma_\eta^2, \sigma_{\varepsilon_j}^2$  are the variance of the residuals.  
 368 The average values of the variances are provided by the adopted GMPE and for this reason they are  
 369 assigned informed prior distributions. Following standard practice, gamma distributions are assigned to  
 370 the corresponding precision parameters, with mean and variance chosen to represent a judgement that  
 371 90% of the individual standard deviations are likely to lie within 20% of the provided values:  
 372

$$374 \begin{aligned} 1/\sigma_\phi^2 &\sim \text{Gamma}(\text{mean} = 1/0.18^2, \text{Variance} = 65.92) \\ 1/\sigma_{\varepsilon_j}^2 &\sim \text{Gamma}(\text{mean} = 1/0.28^2, \text{Variance} = 12.11) \end{aligned} \quad (13)$$

375 For more information regarding the prior distributions and their parameters, the reader is referred to the  
 376 comments in the file ‘M5.R’ uploaded as supplementary material accompanying this article.  
 377

378 In Fig.4, the best estimate fragility curves and their 90% credible intervals obtained by fitting the model  
 379 M1 using the Bayesian approach are compared to their counterparts obtained by fitting M2. It can be  
 380 seen that there is practically no difference in the best-estimate fragility curve between the two models.  
 381 The credible intervals of M2 tend to be close and somewhat narrower than for M1. The differences  
 382 appear to be notable but not significant for  $ds_5$  for both building classes.  
 383

384  
 385 *Fig.4 The data points represent the proportion of buildings of a given class (A or C) in each municipal-*  
 386 *ity, which sustained damage greater or equal to a given damage state  $ds_i$ . The size of each data point*  
 387 *varies according to the total number of buildings of a given class located in a municipality. Best-estimate*  
 388 *fragility curves and their corresponding 90% credible interval comparing M1 vs M2 are plotted.*

### 389 3.2.2 M3 – Accounting for the error components in GMPE and spatial correlation

390 In model M2, the intra-event errors  $\{\varepsilon_j\}$  were considered to be independent at each municipality. In  
 391 reality however, if a GMPE over / underpredicts the ground motion intensity in one municipality for an  
 392 event, it is conceivable that there will be a tendency to over / underpredict in neighbouring municipalities  
 393 as well: the independence assumption is questionable, therefore. To allow for such dependence requires

394 a more complex statistical model, but it is also potentially beneficial because it allows the possibility for  
 395 information to flow between municipalities: this can be particularly helpful when data from some mu-  
 396 nicipalities are sparse, since the characteristics of the GMPE errors there can be inferred (with appropri-  
 397 ate consideration of uncertainty, via the Bayesian approach to inference) from more data-rich locations  
 398 nearby. Model M3 therefore removes the restriction that the intra-event errors are independent.  
 399 The significance of the intra-event spatial correlation in seismic risk assessment has generated an exten-  
 400 sive literature aiming to determine the spatial correlation structure at given sites. Published studies ex-  
 401 clusively consider that the natural logarithm of  $X$  levels in multiple sites follow a multivariate normal  
 402 distribution [38]. The mean of this distribution is provided by Eq.(1) ignoring the two random effects,  
 403 and the covariance matrix is determined as:

$$404 \quad \Sigma = \sigma_{inter}^2 \begin{bmatrix} 1 & 1 & \cdots & 1 \\ 1 & 1 & & \vdots \\ \vdots & & \ddots & \\ 1 & 1 & \cdots & 1 \end{bmatrix} + \sigma_{intra}^2 \begin{bmatrix} 1 & \rho(h_{12}) & \cdots & \rho(h_{1m}) \\ & 1 & & \vdots \\ & & \ddots & \\ sym & & \cdots & 1 \end{bmatrix}$$

405 (14)

406 where  $\rho(h_{jk})$  is the spatial correlation coefficient which is a function of the distance  $h_{jk}$  between the  
 407 centroids of municipalities  $j$  and  $k$ , and is expected to decay with increasing distance. In a Bayesian  
 408 context however, the use of correlation-based dependence models can be computationally expensive,  
 409 because the intra-site correlation matrix must be inverted at each iteration in order to calculate the like-  
 410 lihood contribution to the posterior distribution [39]. With  $m$  municipalities in total, the computational  
 411 cost of inverting a covariance matrix via any standard algorithm is roughly proportional to  $m^3$ : to do this  
 412 at each MCMC iteration (we use 150,000 iterations per model for the results reported below, which is  
 413 not an unusually high number, and is considered necessary in order to get a large effective sample size  
 414 for the more complex models considered here) is simply not feasible for moderate or large numbers of  
 415 locations. For this reason, MCMC-based Bayesian inference for spatial datasets is usually done using  
 416 conditional autoregressive (CAR) representations of dependence, in which the distribution of the quan-  
 417 tity of interest at each spatial location is specified conditional on the values at neighbouring locations.  
 418 The CAR approach has gained wide acceptance in other fields (e.g., ecological studies and disease map-  
 419 ping [40]).  
 420

421 In M3, the intrinsic CAR model [41] (i.e., the simplest form of a CAR model) is used to capture the  
 422 spatial correlation of the intra-event component of the uncertainty in the ground motion intensity. Ac-  
 423 cording to this model, the error  $\varepsilon_j$  in municipality  $j$  depends on the values of the errors in the neighboring  
 424 municipalities, (defined here as those with which municipality  $j$  shares a border), and is modelled as a  
 425 normal distribution:

$$426 \quad \varepsilon_j | \varepsilon_{i, i \neq j} \sim Normal \left( \frac{\sum w_{ji} \varepsilon_i}{\sum w_{ji}}, \frac{\sigma_{CAR}^2}{\sum w_{ji}} \right) \quad (15)$$

427 where the  $\sigma_{CAR}^2$  is the unknown variance parameter; and  $w_{ji}$  are weights which account for the proximity  
 428 of two municipalities, and can be written in the form:

$$w_{jk} = \begin{cases} 1 & \text{If } k \text{ and } j \text{ are neighbour municipalities} \\ 0 & \text{If } k \text{ and } j \text{ are not neighbour municipalities} \end{cases} \quad (16)$$

The variance of the CAR model,  $\sigma_{CAR}^2 / \sum w_{ji}$  (see Eq.(15)) controls the variability of the effect in municipality  $j$  conditional on the effects of neighbour municipalities, and also depends on the number of these municipalities [42]. The intuition here is that the magnitude of the error in municipality  $j$  can be determined more precisely if the errors in a large number of neighbours are already known, than if there is little neighbourhood information. Given the lack of prior information regarding the variance of the spatially distributed effects, an uninformative prior distribution is assigned to the inverse of  $\sigma_{CAR}^2$ , in the form of a gamma distribution which is assumed to have mean equal to 1 and variance equal to 100. It should be noted that an informative prior based on existing spatial models (e.g., [38]) is not feasible as the CAR dependence structure cannot be directly related to a model for inter-station correlations.

In Fig.5, the best-estimate fragility curves corresponding to  $ds_1$ ,  $ds_2$  and  $ds_5$  and their 90% credible intervals obtained by fitting M3 and M1 to the 1980 Irpinia data for class A and C are depicted. The best-estimate fragility curves for M3 appear to be identical to those for M1. The differences between the credible intervals of the two models also appear to be negligible irrespective of damage state or class.

*Fig.5 The data points represent the proportion of buildings of a given class (A or C) in each municipality, which sustained damage greater or equal to a given damage state  $ds_i$ . The size of each data point varies according to the total number of buildings of a given class located in a municipality. Best estimate fragility curves and their corresponding 90% credible interval comparing M1 vs M3 are also plotted.*

### 3.2.3 M4 – Accounting for the error components in GMPE, spatial correlation and uncertainty in IMLs due to the scatter of buildings in the municipality

In the empirical fragility assessment of aggregated post-disaster data, it is commonly assumed that the ground motion level is estimated at the geometrical centre of each municipality. For the Irpinia database, this means that municipalities with hundreds or thousands of buildings, are all assigned the same ground motion level. This is an unrealistic assumption as buildings can be far away from the geometrical centre of the municipality or be sited on soils with very different properties. The within-municipality variation is expected to decrease with distance from the fault (due to an exponential decay in ground motion with distance from the fault). Model M4 is designed to represent this variation in a simplified manner, and hence to test the sensitivity of the estimated fragility curves to the common assumption that all buildings within a municipality experience the same ground motion. To represent the variation, the area in every municipality is subdivided into a regular grid with cell size 1km x 1km. The ground motion intensity level at each centre is estimated by Eq.(2). The variation of these estimates is then calculated in order to determine an index of variation for that municipality. This approach essentially allows greater variation of the intra-event errors for those municipalities where the ground motion is more variable, thus making some allowance for the fact that the precise building locations are unknown.

In M4, the uncertainty due to the spatial distribution of the buildings in each municipality is modelled by adding a municipality-level random effect component at Eq.(1) in the form:

$$\ln(x_j) = f(M, R_j, S_j, F) + \phi + \varepsilon_j + w_j \quad (17)$$

where  $w_j$  is assumed to follow a normal distribution with:

472  $w_j \sim N(\mu = 0, \text{var}_{w_j})$  (18)

473 The inverse variance is also assigned an informative gamma distribution prior concentrated around the  
 474 inverse sample variance of the ground motions across the municipality. It should be noted that unlike  $\epsilon_j$ ,  
 475  $w_j$  is not spatially correlated and for this reason, the two variables are modelled separately.  
 476

477 In Fig.6, the best estimate fragility curves and their 90% credible intervals for models M4 and M1 appear  
 478 to be almost identical. Compared to the fit of M3 (see Fig.5), the addition of an extra random component  
 479 in the estimation of the ground motion intensity in M4 leads to small and non-systematic differences.  
 480 The fit of M4 appears to have a negligible effect on the width of the credible intervals for the curves  
 481 corresponding to  $ds_1$ ,  $ds_2$  and  $ds_5$  for Class A. The width of the intervals corresponding to  $ds_2$  and  $ds_5$   
 482 for Class C are reduced, whilst the width of the intervals corresponding to  $ds_1$  for Class C remains  
 483 unchanged.  
 484

485 *Fig.6 The data points represent the proportion of buildings of a given class (A or C) in each municipal-*  
 486 *ity, which sustained damage greater or equal to a given damage state  $ds_i$ . The size of each data point*  
 487 *varies according to the total number of buildings of a given class located in a municipality. Best-estimate*  
 488 *fragility curves and their corresponding 90% credible interval comparing M1 vs M4 are also plotted.*

489 **3.2.4 M5 – Accounting for the error components in GMPE, spatial correlation, uncertainty in IMLs**  
 490 *due to the scatter of buildings in the municipality and known IMLs*

491 The models proposed so far have ignored the presence of observed ground motion records from the  
 492 studied earthquake. This, however, is not realistic as there are often multiple records, which can be used  
 493 to constrain the uncertainty in the  $X$  levels. M5 is the same as M4, the only difference between the two  
 494 models is that in M5 the PGA level in the 17 municipalities for which there are ground motion records,  
 495 is determined by these records. The PGA level at the remaining municipalities is estimated from the  
 496 Bindi et al. [23] GMPE, by explicitly accounting for the two error components, the spatial correlation  
 497 of the intra-event component and the uncertainty due to the spatial variation of the building inventory  
 498 in each municipality.  
 499

500 In Fig.7, the best estimate fragility curves and their 90% credible intervals obtained by fitting M5 and  
 501 M1 to the 1980 Irpinia data can be compared. The best-estimate curves and their 90% credible intervals  
 502 appear to be identical for  $ds_1$  and  $ds_2$  for both building classes. The differences in the two models appear  
 503 to be notable for  $ds_5$ , where the credible intervals appear to be reduced for M5. The fit of M5 is then  
 504 compared to the fit of M4. The differences appear to be small, which is in line with similar observations  
 505 made in the literature [7, 11] regarding the small impact of a few ground motion stations in the estimation  
 506 of the likelihood of damage and highlight once more the need for a denser network of ground motion  
 507 stations.  
 508

509 *Fig.7 The data points represent the proportion of buildings of a given class (A or C) in each municipal-*  
 510 *ity, which sustained damage greater or equal to a given damage state  $ds_i$ . The size of each data point*  
 511 *varies according to the total number of buildings of a given class located in a municipality. Best estimate*  
 512 *fragility curves and their corresponding 90% credible intervals comparing M1 vs M5 are also plotted.*

513 **3.3 Exploring the impact of informative priors**

514 In models M1 to M5, the uninformative priors of the regression coefficients ignore the wealth of research  
 515 regarding the fragility of the Italian building inventory. A search in the GEM compendium [43] identi-  
 516 fied twelve studies [9, 10, 16, 29, 44-50] that can be used to determine the fragility of Class A and C

517 Italian buildings. These include five empirical studies, six analytical and one heuristic fragility assess-  
 518 ment study. It should be noted that the 1980 Irpinia earthquake is a well-studied event and its post-  
 519 disaster data has been used by all the empirical fragility studies chosen [9, 10, 16, 29, 44]. Therefore,  
 520 the 5 empirical fragility functions are excluded as sources of prior information regarding the regression  
 521 coefficients, as they do not add new information regarding the shape of the fragility curves. Instead, the  
 522 sets of fragility curves found in the six remaining analytical [45-49] and heuristic [50] studies are used  
 523 here to determine the prior distributions.

524  
 525 In Fig.8, the plots of the slope against the intercept of the existing curves for the three damage states and  
 526 the two building classes are depicted. Overall, the variation in the values of the slope and intercept is  
 527 dominated by the variation between studies, which is substantially larger than the variation for individual  
 528 studies that have constructed multiple fragility curves. It can also be noted that the intercept appears to  
 529 be positively correlated to the slope. Nonetheless, this correlation can be attributed to the variation be-  
 530 tween studies. For individual studies which constructed multiple fragility curves there is little evidence  
 531 of such correlation and for this reason, the correlation between the two coefficients is ignored.

532  
 533 In using this information to set informed priors for the two coefficients, the intercept is assigned a normal  
 534 distribution as it can take both positive and negative values and the slope is considered to follow a  
 535 gamma distribution, which accounts for the expectation that the increase in the ground motion intensity  
 536 will increase the probability of a building to be damaged. The informative prior distributions for the two  
 537 regression coefficients can be written as:

$$538 \quad \begin{aligned} \theta_{0i} &\sim Normal(\mu_{\theta_{0i}}, \sigma_{\theta_{0i}}^2) \\ \theta_{1i} &\sim Gamma(\mu_{\theta_{1i}}, \sigma_{\theta_{1i}}^2) \end{aligned} \quad (19)$$

539 The mean and the variance of these prior distributions are determined from the existing fragility curves.  
 540 In particular, the prior mean intercept and slope (i.e.,  $\mu_{\theta_{0i}}$  and  $\mu_{\theta_{1i}}$ ) are set to the means of the corre-  
 541 sponding values from the existing fragility curves. In setting the prior variances however, it is prudent  
 542 to allow for a larger range of coefficient values than is present in the small number of existing fragility  
 543 curves. The prior variances in equation (19) are therefore set at 16 times the sample variance of the exist-  
 544 ing intercepts and slopes.

545  
 546 *Fig.8 Plots of slopes against the intercept for existing fragility curves corresponding to 3 damage*  
 547 *states used as priors for class A and C.*

548 In Fig.9, the fragility curves obtained by fitting model M5 to the data using informative (M5-Info) and  
 549 non-informative (M5-Uninfo) priors are plotted. The differences in the best-estimate curves as well as  
 550 in their 90% credible intervals are not consistent but depend on the building class and damage state.  
 551 Overall, the differences can be considered negligible or small with the exception of the collapse fragility  
 552 curve (i.e.,  $ds_5$ ) for Class C buildings, which is associated with very small probabilities of collapse. For  
 553 this case, the M5-Info leads to flatter best-estimate fragility curves and notably narrower credible inter-  
 554 vals. These observations can be attributed to the relatively large sample sizes of Class A and C buildings  
 555 in the 1980 Irpinia database, which ensure that the observations are highly informative and dominate  
 556 any effect of the prior specification.

557  
 558 The existing fragility curves from which the priors were derived are also depicted in Fig.9. It can be  
 559 noted that the analytical curves appear to be notably steeper than the best estimate fragility curves irre-  
 560 spective of whether informative or non-informative priors have been adopted. By contrast, the heuristic  
 561 ones are more in line with the empirical ones, although this is not systematic. The systematic difference

562 in steepness between the analytical and empirical curves could be attributed to the nature of the analyt-  
563 ical studies which are typically based on a single well defined building exposed to known ground motion  
564 excitations. For this reason, they tend to result in steep fragility curves. By contrast, the empirical curves  
565 are based on large databases that include large variations in the performance and geometric characteris-  
566 tics of buildings in the same class as well as the variability in the ground motion excitation whose char-  
567 acteristics are generally not known.  
568

569 *Fig.9 Prior fragility curves corresponding to 3 damage states for class A and C as well as the best es-*  
570 *timate fragility curves and their 90% credible intervals based on M5 assuming informative (M5-Info)*  
571 *and non-informative (M5-Uninfo) priors.*

572 Fig.10 shows our estimated fragility curves based on M5-Info together with their counterparts based on  
573 M1 with uninformative priors. The differences in the credible intervals for the two models appear to be  
574 small, with the exception of the collapse fragility curves for Class C buildings. In this latter case, the  
575 model M5-info yields significantly narrower credible intervals than model M1. Fig.10 also depicts the  
576 curves constructed by the five [9, 10, 16, 44] other existing empirical studies that adopted the 1980  
577 Irpinia damage database for class A and C buildings either on its own or among other databases from  
578 Italy or worldwide. Overall, the results show a significant variation in the fragility curves. This is most  
579 likely due to differences in data included in the studies (many studies include data sets from several  
580 earthquakes), how the data is manipulated for use in the construction of the fragility functions (e.g.  
581 whether the data is complete, biased etc.), differences in ground motion intensity estimation approach  
582 and due to differences in the statistical model used for their development. Such variations in empirical  
583 fragility functions developed from same/similar data is not uncommon, as seen in [51]. Interestingly,  
584 the variation is large both for Class A buildings, (which are known for their poor performance), and  
585 Class C buildings, (which are expected to perform better).  
586

587 *Fig.10 Plots of best-estimate fragility curves and their 90% credible intervals based on M5 with*  
588 *informative priors and M1 with uninformative priors. Fragility curves from five studies which also used*  
589 *the 1980 Irpinia damage database are also included.*

### 590 **3.4 Prediction of collapsed buildings**

591 So far, this paper has focused on the construction of fragility curves. Despite the importance of such  
592 curves in the seismic risk assessment of the buildings inventory, decision makers often need answers to  
593 questions such as how many buildings are expected to collapse in a future event. The adopted Bayesian  
594 framework can be used to make these predictions, quantifying the uncertainty involved in the expected  
595 number of collapsed buildings. In general, predictions within as well as beyond the range of the data  
596 are possible. However, due to the limited information which produced fragility curves being only part  
597 of the lognormal cumulative distribution function, rather than its full range from 0 to 1, the credible  
598 intervals outside the provided range of data should be used for a qualitative assessment of the fragility.  
599 Fig.11 depicts the posterior distributions of the number of Class A and C buildings expected to collapse  
600 in three municipalities in a future repetition of the 1980 Irpinia earthquake. The predictions concern  
601 three municipalities (see Fig.1) associated with low, medium and high estimated PGA levels. It can be  
602 seen that there is higher uncertainty in predicting the collapsed Class A buildings for all three  
603 municipalities. By contrast, the predictions of collapsed Class C buildings are associated with smaller  
604 uncertainty, and the collapses of multiple buildings are expected only for the municipality very close to  
605 the epicentre.  
606

607 *Fig.11 Histogram of the posterior distribution of the number of buildings expected to be destroyed (i.e.,*  
608 *to sustain damage  $DS=ds_5$ ) in a future earthquake in three municipalities which are expected to be*

609 affected by very low (0.03g), medium (0.09g) and high intensity (0.64g) levels (based on fitting the M1  
 610 model with uninformative priors of regression coefficients).

611  
 612 In the preceding sections, the differences between the models presented in this paper have been studied  
 613 by visual inspecting the best-estimate fragility curves and the length of the corresponding 90% credible  
 614 intervals. Notwithstanding the ease of interpretation of the results of such a qualitative approach, the  
 615 strength of the conclusions is reinforced here by quantifying the differences between the models in  
 616 predicting the number of buildings likely to suffer a given damage state. The focus is on the state of  
 617 collapse, as the differences between the models were found to be more pronounced at this damage state.  
 618 Table 7 depicts the relative change in the predictions of the number of Class A or C buildings likely to  
 619 collapse in the municipality with the largest PGA value, based on models M2-M5 for uninformative  
 620 priors and M5 for informative priors compared to model M1. The relative change in the best estimate  
 621 and the length of the 90% credible intervals are both recorded. For this extreme case, the differences can  
 622 be notable for Class A buildings for both the best estimate and the length of the credible intervals. The  
 623 largest relative change is noted for the most complex M5 model with informative priors. For this model,  
 624 the expected number of collapsed buildings is 14% lower than for M1 and the credible intervals are 20%  
 625 narrower than for M1. The differences between the models are much higher for Class C buildings. In  
 626 particular, for M5-info, 46% fewer buildings are expected to collapse than for M1 and the 90% credible  
 627 intervals appear 59% narrower than for M1. These observations highlight that the more complex model  
 628 has a substantial impact only for the probability of collapse of Class C buildings, where the probability  
 629 of collapse is low.

630 *Table 7: Predicted numbers of collapsed Class A and C buildings in Lioni, a municipality with a total*  
 631 *of 356 Class A and 604 Class C buildings exposed to PGA=0.64g as well as the relative change of the*  
 632 *predictions based on M2-M5 using uninformative priors and M5 using informative priors compared to*  
 633 *M1.*

Class	Model	Values Best Estimate (95%, 5%)	Interval length	Relative change com- pared to M1	
				Best Estimate	Interval length
A	M1	53 (159, 3)	156		
	M2	54 (139, 4)	135	-1%	13%
	M3	50 (146, 2)	144	6%	8%
	M4	50 (143, 3)	140	7%	10%
	M5	49 (131, 4)	127	9%	19%
	M5_Info	46 (127, 2)	125	14%	20%
C	M1	28 (116, 0)	116		
	M2	24 (95, 0)	95	13%	18%
	M3	24 (108, 0)	108	14%	7%
	M4	21 (83, 0)	83	24%	28%
	M5	21 (69, 0)	69	23%	41%
	M5_Info	15 (47, 0)	47	46%	59%

634

## 635 **4 Conclusions**

636 A Bayesian framework is used in this study in order to examine the importance of the uncertainty in the  
637 ground motion intensity in the shape of fragility curves based on post-disaster data aggregated at mu-  
638 nicipality level. The advantage of such framework is its ability to combine prior information regarding  
639 the shape of the fragility curves with post-disaster data and its flexibility in modelling additional sources  
640 of uncertainty. The novelty of the framework includes the use of a CAR model to model the spatial  
641 correlation in the intra-event component and the modelling of the uncertainty due the scatter of the  
642 buildings in the municipality.

643  
644 The framework was applied to the 1980 Irpinia earthquake building damage database, which includes  
645 damage data from 21,845 Class A and C buildings aggregated in 41 municipalities and the ground mo-  
646 tion intensity is estimated by a GMPE. Five models of increasing complexity were constructed in order  
647 to account for the uncertainty in the ground motion, the spatial correlation of its intra-event component  
648 and the uncertainty due to the scatter of the buildings in the municipality as well as to account for the  
649 known ground motion intensity records. The fit of these models to the data was compared to the fragility  
650 curves constructed by fitting a reference model using maximum likelihood analysis to determine the  
651 regression coefficients.

652  
653 The analyses show that more complex models (e.g. M2-M5) yield almost identical results to those ob-  
654 tained from the reference model M1 that uses the estimated, instead of the actual, ground motion inten-  
655 sity and ignores the sources of uncertainty associated with the ground motion intensity or the presence  
656 of ground motion records. This suggests that the studies with aggregated post-disaster data did not in-  
657 troduce an error to the shape of the fragility curves by ignoring the uncertainty in the ground motion  
658 intensity. It was also noted that due to the large number of post-disaster data, the prior information was  
659 found to have a negligible impact on the shape of the fragility curves constructed here with the exception  
660 of the collapse fragility curves for Class C buildings, associated with low probability of exceedance.  
661 Finally, the analyses also highlight the need to appropriately model the significant over-dispersion in  
662 the data (i.e., the variation between the municipalities), which is typically ignored in the literature.  
663 Hence, the use of the reference model M1 can appropriately capture the uncertainty in the damage data  
664 and provide informed predictions regarding the number of buildings likely to suffer damage in a future  
665 earthquake. This has important implications for the seismic risk assessment of the building inventory as  
666 well as for decision makers interested in informed predictions of the vulnerability of the inventory in  
667 future events.

## 668 **Acknowledgement**

669 The time of Dr Ioanna Ioannou and Professor Tiziana Rossetto on this research work was supported by  
670 the European Research Council URBANWAVES grant (ERC Starting Grant 336084; awarded to Pro-  
671 fessor Tiziana Rossetto).

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806

## 807 **Appendix – Ground motion intensity based on Multiple GMPEs**

808 In the main article, the results were based on selecting a single GMPE (i.e. Bindi et al [23]) to estimate  
809 the ground motion intensities of interest which was found to fit the ground motion records for the 1980  
810 Irpinai earthquake better and was found to fit the damage data substantially better than the two  
811 alternatives. A sensitivity analysis is performed here in which all three GMPEs are used to produce  
812 combined assessments of interest, under the simplifying assumption that each of them is equally credible  
813 a priori. Given the overwhelming differences between the fit of the three GMPEs, as measured by their  
814 log-likelihoods in Table 4, this sensitivity analysis can be regarded as extremely conservative in the  
815 sense that it encompasses a much broader range of scenarios than is supported by the available evidence.

816 The aim of this note is to determine how the combined information from the three GMPEs can be used  
817 within our analysis framework. Some notational changes are deemed necessary in Eq.(1) and Eq.(2) in  
818 the article because each GMPE has its own function  $f(\cdot)$ , its own event-specific error  $\phi$  and its own set  
819 of residual errors  $\{\varepsilon_j\}$ . Therefore, a subscript  $g$  is used to denote the values of these quantities from the  
820  $g$ th GMPE. Eq.(1) thus becomes, for  $g=1,2,3$ :

$$821 \quad \ln(x_j) = f_g(M, R_j, S_j, F) + \phi_g + \varepsilon_{jg} \quad (\text{A.1})$$

822 and Eq. (2) becomes

$$823 \quad \ln(\tilde{x}_{jg}) = f_g(M, R_j, S_j, F) \quad . \quad (\text{A.2})$$

824 The absence of a  $g$  subscript on the left-hand side of Eq. (A.1) above is correct:  $x_j$  is the actual ground  
 825 motion, which is the same regardless of which GMPE is used. Also in this equation, the quantities  $\varphi_g$   
 826 and  $\varepsilon_{jg}$  have their own GMPE-specific variances,  $\sigma_{inter_g}^2$  and  $\sigma_{intra_g}^2$  say.

827 According to equations (A.1) and (A.2), if the  $g^{\text{th}}$  GMPE is correct then  $\ln x_j$  has a normal distribution  
 828 with expected value  $\ln \tilde{x}_{jg}$  and variance  $\sigma_{inter_g}^2 + \sigma_{intra_g}^2$ . Moreover, under this GMPE, and under the  
 829 assumption used in models M0 to M2 that the errors  $\{\varepsilon_{.}\}$  are uncorrelated between locations, the co-  
 830 variance between  $\ln x_j$  and  $\ln x_k$  is  $\sigma_{inter_g}^2$ . Formally, we can write  $E(\ln x_j | g) = \ln \tilde{x}_{jg}$ ;  $\text{Var}(\ln x_j | g) =$   
 831  $\sigma_{inter_g}^2 + \sigma_{intra_g}^2$ ; and  $\text{Cov}(\ln x_j, \ln x_k | g) = \sigma_{inter_g}^2$ , where the notation  $\cdot | g$  denotes a property of a proba-  
 832 bility distribution conditional on the  $g^{\text{th}}$  GMPE being correct.

833 Now: assuming that all three GMPEs are considered equally credible a priori, then a probability of 1/3  
 834 is assigned to each of them. In this case, the laws of iterated expectation and variance are applied to  
 835 combine the information from all three GMPEs. In particular, the expected actual ground motion inten-  
 836 sity is:

$$837 \quad E(\ln(x_j)) = E_g \left\{ E(\ln(x_j) | g) \right\} = \sum_{g=1}^3 E(\ln(x_j) | g) P(g) = \frac{1}{3} \sum_{g=1}^3 \ln(\tilde{x}_{jg}) \quad (\text{A.3})$$

838 The variance and covariance are, respectively:

$$839 \quad \begin{aligned} \text{Var}(\ln(x_j)) &= E_g \left\{ \text{Var}(\ln(x_j) | g) \right\} + \text{Var}_g \left\{ E(\ln(x_j) | g) \right\} = \\ &= \frac{1}{3} \sum_{g=1}^3 (\sigma_{inter_g}^2 + \sigma_{intra_g}^2) + \frac{1}{3} \sum_{g=1}^3 (\ln(\tilde{x}_{jg}) - E(\ln(x_j)))^2 \end{aligned} \quad (\text{A.4})$$

840 and

$$841 \quad \begin{aligned} \text{Cov}(\ln(x_j), \ln(x_k)) &= E_g \left\{ \text{Cov}(\ln(x_j), \ln(x_k) | g) \right\} + \text{Cov}_g \left\{ E(\ln(x_j) | g), E(\ln(x_k) | g) \right\} = \\ &= \frac{1}{3} \sum_{g=1}^3 \sigma_{inter_g}^2 + \frac{1}{3} \sum_{g=1}^3 [\ln(\tilde{x}_{jg}) - E(\ln(x_j))] [\ln(\tilde{x}_{kg}) - E(\ln(x_k))] \end{aligned} \quad (\text{A.5})$$

843 To apply the framework of the main paper to this ‘multi-GMPE’ setting, it is necessary to identify ‘ag-  
 844 gregate’ quantities  $\sigma_{inter.}^2$  and  $\sigma_{intra.}^2$  that can be interpreted as combined estimated of inter- and intra-  
 845 event variation corresponding to quantities  $\sigma_{\phi}^2$  and  $\sigma_{\varepsilon_j}^2$ , respectively in Eq. (12). In this case, the value  
 846 of Eq.(A.4) must correspond to  $\sigma_{inter.}^2 + \sigma_{intra.}^2$  and Eq.(A.5) to  $\sigma_{inter.}^2$ . Unfortunately, the desired quanti-  
 847 ties do not exist in general because the values of (A.4) and (A.5) vary between sites (they depend on the  
 848 values of  $j$  and  $k$ ). Nonetheless, it is not necessary to be too precise about the values of  $\sigma_{inter.}^2$  and  $\sigma_{intra.}^2$ .  
 849 There are two reasons for this. First, the focus of this sensitivity analysis is on ‘very conservative’ as-  
 850 sumptions as noted above, a rough approximation will suffice. Secondly the estimates of the inter- and  
 851 intra- variations are used to determine the parameters of the respective prior distributions (see Eq.12) so  
 852 that indicative values will suffice. In view of this,  $\sigma_{inter.}^2$  is determined as the average value of expres-  
 853 sion.(A.5) over all sites, and  $\sigma_{inter.}^2 + \sigma_{intra.}^2$  as the average value of expression.(A.4) over all sites.

854 Using the mean, variance and covariance of the intensity levels based on the combined three GMPEs,  
 855 the reference models M0-M1 (as defined in section 3.1) are fitted to the damage data and fragility curves  
 856 corresponding to  $ds_1$ ,  $ds_2$  and  $ds_5$  for Building Class A and C are constructed. Fig.A.1 depicts the best

857 estimate fragility curves and the 90% credible intervals obtained by fitting M1 to damage data and in-  
858 tensity levels estimated by a single GMPE [23] and the combined GMPEs [23-25]. Overall, the intensity  
859 level at the centroid of each municipality is smaller when estimated by the combined GMPEs. This leads  
860 to the best-estimate fragility curves being systematically higher than the ones based only on Bindi et al.  
861 [23]. This suggests that the combined GMPEs leads to more conservative results with both examined  
862 building classes being more vulnerable to earthquakes than the curves based on the best-fitted GMPE.  
863 It can also be noted that the differences in the width of the credible intervals for the two tested assump-  
864 tions are not systematic. They appear to vary according to the damage state and building class.  
865

866 *Fig.A.1 The data points represent the proportion of buildings of a given class (A or C) in each munici-  
867 pality, which sustained damage greater or equal to a given damage state  $ds_i$ . The size of each data point  
868 varies according to the total number of buildings of a given class located in a municipality. Best estimate  
869 fragility curves and their corresponding 90% credible intervals for M1 for intensity levels based on the  
870 best-fitted Bindi et al. [23] GMPE and on combining the three selected GMPEs [23-25].*

871 *Table A.1: Summary of the three models used for this sensitivity study.*

Model	Over-dis- persion	Uncertainty in X	Uncertainty due to the spread of buildings in each municipality
M1	x	-	-
M2	x	x	-
M3	x	x	x

872 The inter-model variability on the shape of the fragility curves is examined next by explicitly accounting  
873 for the error component in the combined GMPEs as well as the uncertainty due to the spread of the  
874 buildings in each municipality. It should be noted that the most complex models used in this sensitivity  
875 analysis ignores the spatial correlation. In principle, it would be possible to relax the assumption that  
876 the intra-event errors are uncorrelated between locations for each GMPE and to account for the spatial  
877 correlation. Nonetheless, that would result in substantially more complicated expressions and, given the  
878 arguments in the preceding paragraph, it is not clear that the additional complexity is justified. A sum-  
879 mary of the main characteristics of the three models used in this sensitivity analysis can be found in  
880 Tabel.A.1. A visual inspection of the fit on the reference model M1 with the more complex models M2  
881 and M3\* depicted in Fig.A.2 and Fig.A.3 show that neither the best-estimate fragility curves or their  
882 90% credible intervals change significantly for M2 or M3 compared to M1.

883 The sensitivity analysis presented in this appendix highlighted that intensity levels based on the ex-  
884 tremely conservative assumption which combined multiple GMPEs, leads to significant differences  
885 when compared to the curves based on the assumption of the best-fitted GMPE. It was also shown that  
886 with regard to the inter-model differences, in neither case do the best-estimate fragility curves or 90%  
887 credible intervals change significantly for M2 or M3 compared to M1 if the multiple GMPEs were used  
888 to estimate the intensity levels.

889  
890 *Fig.A.2 The data points represent the proportion of buildings of a given class (A or C) in each munici-  
891 pality, which sustained damage greater or equal to a given damage state  $ds_i$ . The intensity levels are  
892 estimated by combining the three selected GMPEs. The size of each data point varies according to the  
893 total number of buildings of a given class located in a municipality. Best estimate fragility curves and  
894 their corresponding 90% credible intervals comparing M1 vs M2 are also presented.*

895  
896 *Fig.A.3 The data points represent the proportion of buildings of a given class (A or C) in each munici-  
897 pality, which sustained damage greater or equal to a given damage state  $ds_i$ . The intensity levels are  
898 estimated by combining the three selected GMPEs. The size of each data point varies according to the*

899 *total number of buildings of a given class located in a municipality. Best estimate fragility curves and*  
900 *their corresponding 90% credible intervals comparing M1 vs M3 are also presented.*  
901

# 1980 Irpinia Earthquake



























