Spontaneous Rotation of Ferrimagnetism Driven by Antiferromagnetic Spin Canting

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Spin-reorientation phase transitions that involve the rotation of a crystal's magnetization have been well characterized in distorted-perovskite oxides such as orthoferrites. In these systems spin reorientation occurs due to competing rare-earth and transition metal anisotropies coupled via f-d exchange. Here, we demonstrate an alternative paradigm for spin reorientation in distorted perovskites. We show that the R_2 CuMnMn₄O₁₂ (R = Y or Dy) triple A-site columnar-ordered quadruple perovskites have three ordered magnetic phases and up to two spin-reorientation phase transitions. Unlike the spin-reorientation phenomena in other distorted perovskites, these transitions are independent of rare-earth magnetism, but are instead driven by an instability towards antiferromagnetic spin canting likely originating in frustrated Heisenberg exchange interactions, and the competition between Dzyaloshinskii-Moriya and single-ion anisotropies.

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Temperature-induced spin-reorientation (SR) phase transitions occur between two long-range ordered magnetic phases [1–3], and can involve the rotation of the staggered magnetization in antiferromagnets [4–7], the net magnetization in ferromagnets and ferrimagnets [8,9], or both coupled together [10]. The discovery of SR transitions and the establishment of their microscopic origin has attracted substantial attention within the condensed matter physics community both in the fundamental study of order and dynamics in quantum magnetism, and in more applied directions where magnetization switching is an essential ingredient for realizing nanoscale components that form the building blocks of spintronic-based technology [11], such as those used in spin-torque devices [12].

SR-based devices lend themselves to operating in the ultrafast regime when there exist two antialigned magnetic sublattices in, for example, antiferromagnets or ferrimagnets [13], which is critical to achieving operational speeds that are comparable to those of charge-based devices [14]. The rare-earth (RE) orthoferrite [15,16] distortedperovskite oxides (generic chemical formula ABO_3 , A = REand B = Fe) are archetypal examples of materials that host ultrafast SR phase transitions [17]. Antiferromagnetic (AFM) order resides on the transition metal (TM) sublattice at all temperatures below T_N , and in certain symmetries a weak ferromagnetic (FM) moment appears through spin canting, which is coupled to the primary AFM order via the Dzyaloshinskii-Moriya interaction [18]. For compounds with a magnetic RE species, f-d exchange interactions have been found to couple either the weak FM moment or the staggered magnetization of the TM sublattice to the RE sublattice. A temperature-induced SR transition can then result if the RE and TM ions have competing magnetic anisotropies [19].

A SR phase transition driven by the same mechanism of f-d coupled competing magnetic anisotropies was recently observed in the triple A-site columnar-ordered quadruple perovskite manganite TmMn₃O₆ [20] (generic chemical formula $A_2A'A''B_4O_{12}$, A = Tm and A', A'', B = Mn). This material belongs to a relatively understudied family of distorted perovskites related to the orthoferrites, but with a different octahedral tilt pattern of $a^+a^+c^-$ instead of $a^{-}a^{-}c^{+}$ (in Glazer notation [21]), which affords a complex ordering of A, A', and A'' cations [22]. TmMn₃O₆ adopts a ferrimagnetic (FIM) structure and boasts an uncompensated magnetization of approximately $1\mu_{\rm B}$ per TM [20], as opposed to the weak FM canting of typically $\leq 0.1 \ \mu_B$ per TM found in the orthoferrites [23]. Hence, a much larger magnetization rotates at the SR transition in $TmMn_3O_6$, giving, for example, the potential for a stronger exchange bias in device heterostructures while maintaining ultrafast switching potential.

In this Letter, we demonstrate a new paradigm for SR transitions in distorted perovskites. We show that both Y₂CuMnMn₄O₁₂ (YCMO) and Dy₂CuMnMn₄O₁₂ (DCMO) columnar-ordered quadruple perovskites adopt a canted FIM structure (m||b) below $T_1 = 175$ K and 159 K, and undergo a SR transition to a collinear FIM (m||c) at $T_2 = 115$ K and 125 K, respectively. Both materials undergo another phase transition at $T_3 = 17$ K, to a canted FIM ground state with a doubled magnetic unit cell. In YCMO, this transition is accompanied by a rotation

of the magnetization back to m||b. In DCMO SR does not occur at T_3 , owing to an additional Ising-like anisotropy of the polarized Dy³⁺ crystal electric field ground state. We show that, unlike other distorted perovskites, the observed SR phenomena in YCMO and DCMO is independent of RE magnetism, but can instead be driven by an instability towards AFM spin canting combined with Dzyaloshinskii-Moriya and single-ion anisotropies.

A 2.06 g polycrystalline sample of YCMO was prepared from a stoichiometric mixture of h-YMnO₃, Mn₂O₃, CuO, and MnO_{1.839}. The mixture was annealed in small batches at 6 GPa and ~1670 K for 2 h in Pt capsules in a belt-type high-pressure apparatus, before the mixture was quenched to room temperature. A 1.32 g polycrystalline sample of DCMO was prepared in the same way, using Dy₂O₃ instead of the h-YMnO₃ precursor [22]. Measurements using dc magnetization were performed using a SQUID magnetometer (Quantum Design, MPMS-XL-7T) between 2 and 400 K under both zero-field-cooled (ZFC) and field-cooled on cooling (FCC) conditions. Time of flight neutron diffraction measurements were performed using WISH at ISIS [24]. Both samples were cooled to 1.5 K and neutron diffraction data were collected on warming through all magnetic phases in 5 K steps (2 K steps were used close to T_1 and also close to T_3 for YCMO). In addition, data were collected with high counting statistics at temperatures representative of each magnetic phase. The crystal structure for both samples was refined against data collected in the paramagnetic phase using the published Pmmn structure [22] [full details are given in the Supplemental Material (SM) Secs. S1 and S2 [25]]. The two A sites (labeled R1 and R2) were found to be fully occupied by Y^{3+} and Dy^{3+} in each of the samples. The A' sites (labeled Cu1) were occupied by 79% Cu^{2+} and 21% Mn^{3+} in YCMO, and 70% Cu^{2+} and 30% Mn^{3+} in DCMO. The A" sites (labeled Mn2) were occupied by 74% Mn^{2+} and 26% Y^{3+} in YCMO, and 78% Mn²⁺ and 22% Dy³⁺ in DCMO. The two symmetry inequivalent B sites form layers stacked alternately along c, labeled Mn3 and Mn4. The Mn3 layers were fully occupied by Mn³⁺ in YCMO, but had a 9% occupation of Cu^{2+} in DCMO. The Mn4 layers were fully occupied by Mn⁴⁺ in both samples. In the following we present neutron powder diffraction data analyzed in terms of symmetry-adapted magnetic modes, F_i , A_i , X_i , and Y_i (defined in the SM [25] for the A and B sublattices), where i represents the direction of the moment components in the basis x||a, y||b, z||c.

At $T_1 = 175$ K new Γ -point intensities appeared in the diffraction pattern for YCMO (Fig. S4 [25]) that occurred concomitantly with a rapid increase in the dc magnetic susceptibility shown in Fig. 1(a), which together indicate the development of long-range FM sublattices. Rietveld refinement of the diffraction data showed that in this first magnetic phase (labeled CFI') Mn2 and Mn4 sites order with F_y modes, and the Mn3 sites order with A_x , F_y , Y_z

modes [Fig. 2(c)]. Key features of the magnetic structure can be directly observed in the diffraction pattern. For example, the $\{200\}$ family of magnetic reflections, Figs. 3(a)-3(c), originate in scattering from A- and B-site F_i modes only, and their relative intensities provide a direct measure of the direction i of the respective moments. Zero magnetic intensity at (020) and equal magnetic intensities at (200) and (002), as shown in Fig. 3(a), is uniquely consistent with F_v modes. The {110} family of magnetic intensities shown in Figs. 3(d)–3(f) are also sensitive to F_i modes at the A sites, and AFM A_i, X_i, Y_i modes (instead of F_i modes) at the B sites. In this phase zero magnetic intensity at (110), and equal magnetic intensities at (011)and (101), Fig. 3(d), can only be accounted for by the presence of A_x , Y_z modes on Mn3 layers in addition to the Mn2 F_v mode. The F_v modes combine to give a FIM structure with a net magnetization parallel to y, and the A_x and Y_{τ} modes give rise to spin canting of the Mn3 layers with the same amplitude in every Mn3 layer. The temperature dependence of the net magnetization arising from the F_{v} modes, and the perpendicular moment magnitude of the A_x and Y_z canting are given in Figs. 1(c) and 1(e), respectively. As the temperature is lowered the magnetization increases, in agreement with the temperature dependence of all symmetry inequivalent magnetic moments (Fig. S4 [25]).

At $T_2 = 115$ K the shift of magnetic intensity from the (002) to the (020) reflection, while the (200) intensity remains the same [Fig. 3(b)], indicates that the F_i mode, and therefore the net magnetization, rotated from the *b* axis to the *c* axis. This SR transition is also apparent in magnetometry measurements shown in Fig. 1(a), that



FIG. 1. Temperature dependence of (a),(b) ZFC and FCC magnetization measurements under an applied dc field of 100 Oe (c),(d) the net magnetization per TM. The net magnetization was calculated by taking the sum over all magnetic sites in the unit cell (Cu1 had a contribution of zero to the net magnetization) and (e),(f) the Mn3 moment magnitudes for each AFM spin canting mode.



FIG. 2. The refined magnetic structures, separated into the *A* and *B* sites, of (a)–(c) YCMO and (d)–(f) DCMO at temperatures of 1.5 K, 40 K, and 140 K. For the *A* sites, *R*1 is shown in blue, *R*2 in green, Cu1 in black, and Mn2 in red. For the *B* sites Mn3 is shown in blue and Mn4 in black. The crystallographic unit cell is drawn in black. Note that at 1.5 K the propagation vector of the spin canting is $(0,0,\frac{1}{2})$ and thus (a) and (d) should be doubled along *c* to represent the full magnetic unit cell.

feature a characteristic cusplike increase in the magnetization [20]. Rietveld refinement of data measured at 40 K showed that this second magnetic phase (labeled FI) has a collinear FIM structure where the Mn2, Mn3, and Mn4 sublattices order with F_z modes [Fig. 2(b)]. The SR transition at T_2 was found to occur over a 20 K interval, as shown in Figs. 1(a) and 1(c). The collinear phase then persists on cooling to a second SR transition at $T_3 = 17$ K.

Below T_3 , two significant changes to the diffraction pattern were observed. First, eight new magnetic peaks appeared that could be indexed with a $\mathbf{k} = (0, 0, 0.5)$ propagation vector (Z point). Second, the intensity shifted from the (020) to the (002) reflection, showing that the F_i modes rotated back to the *b* axis. In this third magnetic phase (labeled CFI), Mn2, Mn3, and Mn4 F_y modes accounted for all Γ -point magnetic intensities apart from a small intensity at (011) that is likely due to the presence of an unidentified magnetic impurity. The magnetic peaks at the Z point were fitted with Y_x , A_z AFM canting modes on the Mn3 layers, the amplitude of which changes sign from one Mn3 layer to the next [Fig. 2(a)]. We note that in all magnetic phases our analysis indicated zero moment on the Cu1 sites, despite strong exchange coupling of Cu demonstrated by ESR measurements (Fig. S5 [25]). This effect could occur if the minority Mn^{3+} and majority Cu^{2+} ions, randomly located on the Cu1 site, had antiparallel moments, giving an average moment lower than the sensitivity of our experiment [34].

In DCMO, the first two magnetic phases, CFI' and FI [Figs. 2(f) and 2(e)], were found to be identical to YCMO, except that in the FI phase an additional polarized moment developed on the Dy1 and Dy2 sublattices with m || c [25]. Crystal electric field calculations (Sec. S5 [25]) showed that the lowest lying Kramers doublet of both Dy1 and Dy2 is well separated from excited states, and has a strong Isinglike *g*-tensor anisotropy ||z|, which is consistent with the onset of a Dy1 and Dy2 moment only below the SR transition at $T_2 = 125$ K. Evidence for the polarized Dy1 and Dy2 moments was found at the (011) and (101) reflections [Fig. 3(k)], which are expected to be of equal intensity in the absence of a moment on the RE sites, as was the case for the YCMO magnetic structure refined at 40 K [Fig. 3(e)], but instead had unequal intensities consistent with a finite moment on the Dy sublattices. By comparison with YCMO, it is apparent that the additional Dy magnetism had two significant effects on the behavior of the system. First, the SR transition between CFI' and FI became sharper, Figs. 1(b) and 1(d), and second, at $T_3 =$ 17 K it prevented the SR between phases FI and CFI [as indicated by the absence of any changes at the $\{200\}$ family of reflections, Fig. 3(i), and the absence of a cusp in the magnetic susceptibility, Fig. 1(b)]. Instead, the CFI phase of DCMO had Γ -point F_{τ} modes across all sites that maintained the FIM structure with magnetization ||c|[Fig. 2(d)]. A Z-point peak also appeared in the CFI phase, which could be fit by a single AFM canting mode on the Mn3 layer (either A_x or A_y).

Spin canting typically arises when the Dzyaloshinskii-Moriya (DM) interaction is allowed by symmetry (e.g., in orthoferrite YFeO₃ DM exchange induces a $\sim 0.3^{\circ}$ canting of Fe spins [35], which is small due to the DM interaction being approximately thirty times weaker than Heisenberg exchange [36]). By comparison, Mn3 spins in R_2 CuMnMn₄O₁₂ exhibit canting angles of up to ~30° (Fig. S4 [25]), which are improbably large for DM-induced spin canting. Furthermore, the symmetry of spin canting found in the CFI phase of DCMO is incompatible with DM exchange, as explained in the next paragraph. Instead, large spin canting in R_2 CuMnMn₄O₁₂ can be established by the competition between effective FM (Mn3-O-A-O-Mn3) and AFM (Mn3-O-Mn3) isotropic Heisenberg exchange between nearest-neighbor Mn3 spins in a given layer, as described in Ref. [20]. The former interactions favor F_i modes, whereas the latter primarily favor an A_i mode,



FIG. 3. Neutron powder diffraction data taken on WISH; (a),(d),(g),(j) were collected at 140 K; (b),(e),(h),(k) at 40 K and (c),(f),(i),(l) at 1.5 K. (a)–(c) {200} and (d)–(f) {110} reflections from YCMO, and (g)–(i) {200} and (j)–(l) {110} reflections from DCMO. The data are shown by the red circles, the fit by the solid black line and the blue shading represents the nuclear contribution to scattered intensity, including an impurity phase for DCMO. The green tick marks indicate, from top to bottom, the nuclear and magnetic reflections.

which can be augmented by X_i or Y_i modes in the case of inequivalent exchange along x and y. In the mean field approximation one can show that this competition leads to two separate orders for the Mn3 sublattice; collinear FM or canted FM, which can be selected by tuning the ratio of the effective FM and AFM interaction strengths. This tuning is apparent when comparing the magnetic structures of R_2 CuMnMn₄O₁₂ and TmMn₃O₆ [20]. In TmMn₃O₆ every A' site was occupied by Mn³⁺ and spin canting was not observed [20]. In R_2 CuMnMn₄O₁₂ the magnetic moment on the A' sites was considerably reduced by the substitution of Mn³⁺ for Cu²⁺, giving a smaller effective FM exchange and prevalent spin canting.

While competing Heisenberg exchange can establish spin canting, it cannot alone determine the orientation of the magnetic moments with respect to the crystal structure. However, once the canted structure exists, DM interactions can play a dominant role in determining the spin anisotropy, as they will be optimized when the moment components of the primary magnetic modes (F_i, A_i, Y_i) are placed along specific crystallographic directions [37,38]. Formally, DM interactions couple orthogonal moment components from two modes of different types (e.g., A_x , F_{y}), both of which must transform by the same irreducible representation of the paramagnetic space group such that a bilinear free energy invariant exists [39]. In the SM (Table S5) [25] we tabulate linear combinations of modes categorized by their symmetry. It is apparent that the A_x , F_y , and Y_z combination (Γ_4^+ irrep), as found in the CFI' phase of both YCMO and DCMO, presents a unique combination of all three primary modes mutually coupled by DM interactions. In the CFI phase of YCMO, symmetry prohibits DM interactions between the Γ -point F_{v} and the Z-point A_i , Y_i modes. However, the latter modes can couple via DM exchange in two symmetries: the Z_1^+ irrep (Y_x, A_z) and the Z_4^+ irrep (A_x, Y_z) (Table S5 [25]). Symmetry alone cannot determine which scenario is realized (the former was observed), but both involve moment components along x and z meaning that the net magnetization from the Γ -point F_i mode will be placed parallel to b(y) to establish a constant moment ground state. To the contrary, in the CFI phase of DCMO the net magnetization lies parallel to c (F_z modes). For A_i or Y_i modes to be included in a constant moment ground state they must have moment components perpendicular to z. However, there is no single irrep that transforms (couples) A_x , Y_y or Y_x , A_y . Accordingly, the canted ground state of DCMO does not optimize antisymmetric exchange but is instead predominantly selected by the dominant, Ising-like anisotropy of Dy³⁺. The intermediate FI phase of both YCMO and DCMO has an approximately collinear magnetic structure (within the sensitivity of the experiment), which drastically reduces the DM interactions. The F_i modes then follow the weak easy axis single-ion-anisotropy of Mn^{3+} , which is parallel to the *c* axis on average [40].

In summary, Y₂CuMnMn₄O₁₂ and Dy₂CuMnMn₄O₁₂ host magnetic phase transitions between canted and collinear structures that are accompanied by spin reorientation from m||b (favored by DM in the canted phases) to m||c (favored by single ion anisotropy in the collinear phase), with the exception of the Dy₂CuMnMn₄O₁₂ canted ground state where Dy³⁺ Ising-like anisotropy imposes m||c. Our results are in complete contrast to well established SR phenomena in other distorted perovskites, but instead

demonstrate a mechanism for spin reorientation originating in spin canting instabilities. Importantly, these triple A-site columnar-ordered quadruple perovskites have the potential to host ultrafast spin-reorientation transitions while boasting a large 1 μB moment per TM, making them candidate materials to realize novel spin-based technology. In future studies it would be interesting to investigate the modification of the SR phenomena through further chemical substitution and doping on this triple A-site columnarordered perovskite framework.

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- [1] H. Horner and C. M. Varma, Phys. Rev. Lett. **20**, 845 (1968).
- [2] K. P. Belov, A. K. Zvezdin, A. M. Kadomtseva, and R. Z. Levitin, Sov. Phys. Usp. 19, 574 (1976).
- [3] S. Chikazumi, *Physics of Ferromagnetism*, International Series of Monographs on Physics (Clarendon Press, Oxford, 1997).
- [4] A. Marcinkova, T. C. Hansen, C. Curfs, S. Margadonna, and J. W. G. Bos, Phys. Rev. B 82, 174438 (2010).
- [5] S. A. J. Kimber, A. H. Hill, Y.-Z. Zhang, H. O. Jeschke, R. Valentí, C. Ritter, I. Schellenberg, W. Hermes, R. Pöttgen, and D. N. Argyriou, Phys. Rev. B 82, 100412(R) (2010).
- [6] A. J. Corkett, D. G. Free, and S. J. Clarke, Inorg. Chem. 54, 1178 (2015).
- [7] Q. Zhang, W. Tian, S. G. Peterson, K. W. Dennis, and D. Vaknin, Phys. Rev. B 91, 064418 (2015).
- [8] Z. Tie-song, J. Han-min, G. Guang-hua, H. Xiu-feng, and C. Hong, Phys. Rev. B 43, 8593 (1991).
- [9] R. W. Houghton and W. Weyhmann, Phys. Rev. Lett. 20, 842 (1968).
- [10] J. P. Bolletta, F. Pomiro, R. D. Sánchez, V. Pomjakushin, G. Aurelio, A. Maignan, C. Martin, and R. E. Carbonio, Phys. Rev. B 98, 134417 (2018).
- [11] I. Fita, A. Wisniewski, R. Puzniak, E. E. Zubov, V. Markovich, and G. Gorodetsky, Phys. Rev. B 98, 094421 (2018).
- [12] N. Locatelli, V. Cros, and J. Grollier, Nat. Mater. 13, 11 (2014).
- [13] A. V. Kimel, B. A. Ivanov, R. V. Pisarev, P. A. Usachev, A. Kirilyuk, and T. Rasing, Nat. Phys. 5, 727 (2009).
- [14] Y. Yang, R. B. Wilson, J. Gorchon, C.-H. Lambert, S. Salahuddin, and J. Bokor, Sci. Adv. 3, e1603117 (2017).
- [15] S. Geller, J. Chem. Phys. 24, 1236 (1956).
- [16] W. C. Koehler, E. O. Wollan, and M. K. Wilkinson, Phys. Rev. 118, 58 (1960).

- [17] A. V. Kimel, A. Kirilyuk, A. Tsvetkov, R. V. Pisarev, and T. Rasing, Nature (London) 429, 850 (2004).
- [18] D. Treves, Phys. Rev. 125, 1843 (1962).
- [19] R.L. White, J. Appl. Phys. 40, 1061 (1969).
- [20] A. M. Vibhakar, D. D. Khalyavin, P. Manuel, L. Zhang, K. Yamaura, P. G. Radaelli, A. A. Belik, and R. D. Johnson, Phys. Rev. B 99, 104424 (2019).
- [21] A. M. Glazer, Acta Crystallogr. Sect. B 28, 3384 (1972).
- [22] A. A. Belik, D. D. Khalyavin, L. Zhang, Y. Matsushita, Y. Katsuya, M. Tanaka, R. D. Johnson, and K. Yamaura, Chem. Phys. Chem. 19, 2449 (2018).
- [23] R. M. Bozorth, V. Kramer, and J. P. Remeika, Phys. Rev. Lett. 1, 3 (1958).
- [24] L. C. Chapon, P. Manuel, P. G. Radaelli, C. Benson, L. Perrott, S. Ansell, N. J. Rhodes, D. Raspino, D. Duxbury, E. Spill, and J. Norris, Neutron News 22, 22 (2011).
- [25] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevLett.124.127201 for further details of the neutron powder diffraction refinement, the symmetry analysis, the Dy³⁺ crystal electric field calculations, and the results of the ESR measurements, which includes Refs. [26–33].
- [26] L. Zhang, Y. Matsushita, K. Yamaura, and A. A. Belik, Inorg. Chem. 56, 5210 (2017).
- [27] N. E. Brese and M. O'Keeffe, Acta Crystallogr. Sect. B 47, 192 (1991).
- [28] B. J. Campbell, H. T. Stokes, D. E. Tanner, and D. M. Hatch, J. Appl. Crystallogr. 39, 607 (2006).
- [29] J. Rodríguez-Carvajal, Physica (Amsterdam) **192B**, 55 (1993).
- [30] M. Hutchings, Solid State Physics, Volume 16 (Academic Press, 1964), pp. 227–273.
- [31] A. J. Freeman and J. P. Desclaux, J. Magn. Magn. Mater. 12, 11 (1979).
- [32] V. A. Ivanshin, J. Deisenhofer, H.-A. Krug von Nidda, A. Loidl, A. A. Mukhin, A. M. Balbashov, and M. V. Eremin, Phys. Rev. B 61, 6213 (2000).
- [33] F. Köksal, I. Kartal, and B. Karabulut, Z. Naturforsch. A 54, 177 (1999).
- [34] This scenario is akin to alloys of niobium-vanadium and compounds with a mixture of deuterium and hydrogen, that give zero nuclear scattering length.
- [35] M. Eibschütz, S. Shtrikman, and D. Treves, Phys. Rev. 156, 562 (1967).
- [36] K. Amelin, U. Nagel, R. S. Fishman, Y. Yoshida, H. Sim, K. Park, J.-G. Park, and T. Rõõm, Phys. Rev. B 98, 174417 (2018).
- [37] D. D. Khalyavin, A. N. Salak, A. B. Lopes, N. M. Olekhnovich, A. V. Pushkarev, Y. V. Radyush, E. L. Fertman, V. A. Desnenko, A. V. Fedorchenko, P. Manuel, A. Feher, J. M. Vieira, and M. G. S. Ferreira, Phys. Rev. B 92, 224428 (2015).
- [38] D. D. Khalyavin, A. N. Salak, P. Manuel, N. M. Olekhnovich, A. V. Pushkarev, Y. V. Radysh, A. V. Fedorchenko, E. L. Fertman, V. A. Desnenko, and M. G. S. Ferreira, Z. Kristallogr. Cryst. Mater. 230, 767 (2015).
- [39] I. Dzyaloshinsky, J. Phys. Chem. Solids 4, 241 (1958).
- [40] M.-H. Whangbo, E. E. Gordon, H. Xiang, H.-J. Koo, and C. Lee, Acc. Chem. Res. 48, 3080 (2015).