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Carrier Phase Recovery in Optical Fiber Communication Systems Using High-Order Modulation Formats

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ABSTRACT

Nowadays, the coherent optical communication system plays an important role in communication field because of large capability and bandwidth. A coherent optical communication, based on high-order modulation and digital signal processing technologies, consists of optical transmitters, optical fiber lines, optical amplifiers and optical receivers. In the high-speed coherent optical communication system, the phase noise from the transmitter laser and the local oscillator laser can significantly degrade the performance of the signal transmission and detection, especially for the systems using high-order modulation format, such as m-ary phase shift keying (m-PSK) and m-ary quadrature amplitude modulation (m-QAM). Therefore, investigations on laser phase noise compensation algorithm based on digital signal processing technologies has become more and more significant. In this work, a multi-ring carrier phase recovery algorithm is developed for compensating the laser phase noise in optical fiber communication systems using high-order modulation formats. Degradations on the performance of communication systems due to the laser phase noise have been investigated. The system performance using the proposed algorithm and the conventional Viterbi-Viterbi algorithm were also evaluated in 9-channel and 15channel, 32-Gbaud, Nyquist-spaced QPSK, 16-QAM, 64-QAM and 256-QAM coherent transmission systems with considering the impact of the laser phase noise. It is found that the phase noise leads to stricter constraints on the linewidths of transmitter-side and receiver-side lasers, and it can greatly degrade the achievable information rates in communication systems. Besides, compared to the conventional Viterbi-Viterbi algorithm, which is usually applied in the QPSK system, our proposed algorithm can also well mitigate the laser phase noise in 16-QAM, 64-QAM and 256-QAM optical communication systems.

Keywords: Coherent optical communication system, Laser phase noise, Carrier phase recovery, Viterbi-Viterbi algorithm, High-order modulation formats

1. INTRODUCTION

Nowadays in the information age, the importance of communication technology has gradually become prominent, and various communication technologies have been developed rapidly. Among optical communication technologies, the coherent optical communication system plays an important role in communication field due to large capacity, long transmission distance and high spectrum efficiency.^{1,2} In recent years, digital signal processing (DSP) has evolved vigorously, and the use of DSP technology at the optical receiver to solve various problems in the transmission of optical signal has gradually become a hot issue in the optical communication field. In fact, the application of DSP technology has significantly improved the performance of the coherent optical system. During the process of optical signal transmission, the phase noise from the laser will increase the bit error rate(BER) and degrade the signal-to-noise ratio(SNR), which is one of the important factors affecting the performance of the coherent optical communication system.

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With the development of DSP technology, carrier phase recovery algorithms based on DSP technology have attracted extensive attention. In 2006, Pfau T et al. from the University of Stuttgart in Germany conducted the first real-time coherent optical communication experiment.³ They successfully achieved laser phase noise compensation for the 800Mb/s quadrature phase shift keying(QPSK) system using DSP technology. In 2010, Fatadin I et al. from the National Physical Laboratory of Teddington United Kingdom proposed a carrier phase recovery algorithm based on the Viterbi-Viterbi algorithm to perform QPSK partitioning on the Square 16-QAM system, which reduced the complexity of the hardware.⁴ In 2015, Syed et al. from Politecnico di Torino proposed a novel low-complexity two-stage digital feedforward carrier phase recovery algorithm.⁵ At the BER of 10^{-2} , for an OSNR penalty of 1 dB, the scheme in this paper could tolerate a linewidth-symbol duration product $\Delta v T_s$ of 3.7×10^{-5} .

In this work, we have investigated the impact of laser phase noise and have developed a modified Viterbi-Viterbi (MVV) algorithm to compensate for laser phase noise. Numerical simulations have been carried out in a multi-channel, 32-Gbaud Nyquist-spaced wavelength division multiplexing (WDM) optical communication system using the EDC, where the number of channels is set to 9 and 15, respectively. It is found that the phase noise leads to strict constraints on the linewidths of transmitter-side and receiver-side lasers, and it can greatly degrade the achievable information rates in communication systems. Besides, simulation results indicate that compared to the conventional Viterbi-Viterbi algorithm, which is usually applied in the QPSK system, the proposed algorithm can also well mitigate the laser phase noise in 16-QAM, 64-QAM and 256-QAM optical communication systems.

2. LASER PHASE NOISE AND MODIFIED VITERBI-VITERBI ALGORITHM

2.1 Principle of Laser Phase Noise

The noise of the semiconductor laser mainly arises from the spontaneous radiation. Each spontaneously radiated photon will add a part of the random field component to the coherent field, disturbing the amplitude and the phase of the original coherent field.⁶ Since R_{sp} (the rate of spontaneous radiation when entering the lasing mode) of the semiconductor laser is relatively high, this spontaneous radiation can occur frequently, which makes the intensity and the phase of the output signal fluctuate. The intensity fluctuations will degrade the signal-to-noise ratio (SNR) of the semiconductor laser, while phase fluctuations will result in a limited frequency linewidth.

The laser phase noise can be described as^{7,8}

$$\varphi_t = \sum_{i=-\infty}^t N_i \tag{1}$$

where N_i is an independent and identically distributed random Gaussian variable, of which the variance can be described as

$$\sigma_f^2 = 2\pi \Delta v / R_s = 2\pi (\Delta v T_s) \tag{2}$$

where Δv represents the linewidth, R_s denotes the symbol rate, and T_s represents the symbol period. As Equation (2) reveals, the laser phase noise variance increases with the linewidth of the laser and the symbol period of the transmission system. Besides, the laser phase noise will affect the performance of optical communication system, and will degrade the SNR and increase the BER.

2.2 Modified Viterbi-Viterbi Carrier Phase Recovery

The Viterbi-Viterbi algorithm is also known as the M-th power carrier phase recovery algorithm, which is mainly used to compensate the laser phase noise of the signal in the multi-ary phase shift keying (M-PSK) communication system.^{9,10}

In this paper we have improved the traditional Viterbi-Viterbi algorithm: The core idea of the algorithm is still to perform fourth power processing on the symbol points of which modulation phase conforms to the QPSK modulation format, and remove the modulation phase to estimate the laser phase noise at this symbol point. But the difference from the traditional Viterbi-Viterbi algorithm lies in that the algorithm proposed in this paper performs the rotation and the filtering operations on the symbol points on the intermediate ring.^{11–20} Thus the points on the intermediate ring can also be used to estimate the laser phase noise after processing. The algorithm proposed in this paper can use almost all symbol points for laser phase noise estimation, and the effect of the laser phase noise compensation is greatly improved.^{21–25} Taking 16QAM as an example, the principles and steps of the MVV algorithm are described as follows:



Figure 1. Constellation diagram of 16QAM system

1. Set the threshold and divide the loop

Normalize the input symbol sequence and adjust the amplitude to conform to the coordinate system shown in Figure 1. In this coordinate system, the radii of the three rings of the ideal constellation diagram are $\sqrt{2}$, $\sqrt{10}$, and $3\sqrt{2}$ respectively. The first step is to classify all the symbols in the symbol sequence into the innermost ring, middle ring or outermost ring by judging the magnitude of each symbol. In the coordinate system shown in Figure 1, the two thresholds of the ring division can be set as follows:

$$Thr_1 = (\sqrt{2} + \sqrt{10})/2 \tag{3}$$

$$Thr_2 = (3\sqrt{2} + \sqrt{10})/2 \tag{4}$$

Comparing the amplitude of each symbol of the input symbol sequence with Thr_1 and Thr_2 in turn, all points in the symbol sequence can be divided into two categories: the points, of which the amplitudes are less than Thr_1 or larger than Thr_2 , are classified as inner ring and outer ring, denoted as S_1 ; the points, of which the amplitudes are between Thr_1 and Thr_2 are classified as the points on the middle ring, denoted as S_2 . The modulation phase of S_1 is one of $\pi/4$, $3\pi/4$, $5\pi/4$, and $7\pi/4$, which means the traditional Viterbi-Viterbi algorithm can be used directly to remove the modulation phase, while the modulation phases of the symbols in S_2 are not the same as the modulation phase of the QPSK modulation format.

2. Perform fourth Power processing on S_1

From the Viterbi-Viterbi algorithm, we can know that the QPSK signal $exp(i(k\pi/4 + \varphi_0))$ can be perform on fourth power processing to obtain $-exp(4i\varphi_0)$. In order to compensate the -1 that appears after the fourth power processing, the symbol in S_1 is multiplied by $exp(i\pi/4)$ before being processed to the fourth power, which is denoted as $(S_1)^4$. 3. Rotate the middle ring and perform the fourth power processing on S_2

Observing the constellation diagram in Figure 1, we can see that the eight symbol points on the middle ring can be divided into two types: red symbol points and white symbol points. The phases of the red symbol points are respectively angle(1+3i), $\pi/2 + angle(1+3i)$, $\pi/angle(1+3i)$ and $3\pi/2 + angle(1+3i)$. The phases of the white points are respectively angle(3+1i), $\pi/2 + angle(3+1i)$, $\pi/angle(3+1i)$, $\pi/angle(3+1i)$ and $3\pi/2 + angle(3+1i)$ and $3\pi/2 + angle(3+1i)$ and $3\pi/2 + angle(3+1i)$. Among them, angle(1+3i) and angle(3+1i) represent respectively the angle of 1 + 3i and the angle of 3 + 1i.

The phases of the red symbol points can be performed on fourth power processing after being transformed into $\pi/4$, $3\pi/4$, $5\pi/4$, $7\pi/4$ by being rotated clockwise by $(angle(1+3i) - \pi/4)$. In the same way, the phases of the white symbol points can be performed on fourth power processing after being transformed into $\pi/4$, $3\pi/4$, $5\pi/4$, $7\pi/4$ by being rotated anticlockwise by $(angle(1+3i) - \pi/4)$.

Therefore, multiply S_2 by $exp(i(\theta - \pi/4))$ then perform the fourth power processing, and denote the result as $anticlc(S_2)^4$, where $\theta = angle(1 + 3i)$. After rotating the middle ring anticlockwise, the modulation phase of the white symbol points in the figure can be removed by fourth power processing, which are the correct points and should be kept, while the red symbol points rotated anticlockwise are wrong points and need to be eliminated. In the same way, after multiplying S_2 by $exp(-i(\theta - \pi/4))$ to rotate it clockwise and denoting the result as $clc(S_2)^4$, the red symbol points will become the correct point, while the white symbol points will become the wrong point.

4. Filter out the correct points, and estimate the laser phase noise

In general, we need to eliminate the additive white Gaussian noise before estimating the laser phase noise. Adding all the symbols in a continuous symbol block can greatly eliminate additive white Gaussian noise because the amplitude of the additive white Gaussian noise conforms to the Gaussian distribution. Since the laser phase noise changes continuously and slowly, it can be considered that the laser phase noise of each symbol in a symbol sequence within an appropriate length is approximately the same.

Considering the existence of the laser phase noise and the additive white Gaussian noise comprehensively, this paper adopts the following scheme to estimate the laser phase noise:

Set a sliding window with a fixed length, sum all the $anticlc(S_2)^4$ and $clc(S_2)^4$ in the window and normalize them respectively, denoted as $\Sigma(anticlcS_2)^4$ and $\Sigma(clcS_2)^4$. Subsequently, take the points of the innermost and outermost rings as the reference standard and filter out the correct symbols from $\Sigma anticlc(S_2)^4$ and $\Sigma clc(S_2)^4$.

After normalizing the symbols belonging to $\Sigma anticle(S_2)^4$ and $\Sigma cle(S_2)^4$ in the window, subtract them from $\Sigma(S_1)^4$ respectively, take the amplitude, and denote it as *abs*. If *abs* is less than the threshold *Thr*, then *abs* is considered to be small enough and the symbol is the correct symbol. After selecting all the correct points in the window in this way, sum all the correct points to eliminate the additive white Gaussian noise and divide the phase of the sum by 4 to obtain the estimated value of the laser phase noise φ_0 . Take φ_0 as the estimated value of laser phase noise of the center symbol point of the window. By traversing the sliding symbol block, the laser phase noise of all points in the symbol sequence can be estimated.

5. Phase unwrapping

In Matlab, the output range of the angle function is $[-\pi,\pi]$, so the range of the laser phase noise is $[-\pi/4,\pi/4]$. When the actual laser phase noise exceeds this range, the step change will bring errors. In order to avoid this situation, it is necessary to unwrap the estimated value of the laser phase noise.

$$\theta_n = \begin{cases} \theta_n - \pi/2, & \theta_n - \theta_n - 1 \ge \pi/4 \\ \theta_n, & pi/4 > \theta_n - \theta_n - 1 \ge -\pi/4 \\ \theta_n + \pi/2, & \theta_n - \theta_n - 1 \ge -\pi/4 \end{cases}$$
(5)

Compare θ_n estimated in the current window with θ_{n-1} estimated in the previous window. If θ_n is too large, decrease it by $\pi/2$; if θ_n is too small, increase it by $\pi/2$.

6. Perform phase noise compensation on the symbol sequence

Finally, the signal is restored with the estimated phase fluctuation to complete the carrier phase recovery.

As for DP-64QAM system and DP-256QAM system, from Figure 2 and Figure 3 we could see that the core idea of the algorithm is the same as DP-16QAM system and in this paper we will not illustrate specific steps.



Figure 2. Constellation diagram of 64QAM system



Figure 3. Constellation diagram of 256QAM system

3. TRANSMISSION SETUP

Figure 4 illustrates the transmission system setup of the multi-channel 32-Gbaud Nyquist-spaced wavelength division multiplexing (WDM) optical communication system using the following modulation formats: DP-16-QAM, DP-64-QAM, and DP-256-QAM. Detailed parameters of the transmission system are shown in Table 1.

At the transmitter, a 32-GHz spaced laser comb with a center wavelength of 1550 nm serves as the optical carrier. Subsequently, the WDM optical carriers are modulated respectively by 32-Gbaud signals via in-phase and quadrature (I-Q) modulators. Besides, the transmitted symbol sequences in each channel are random and independent. Based on the split-step Fourier solution of nonlinear Schrödinger equation (NLSE), the SSMF is simulated, and the attenuation coefficient(α), chromatic dispersion coefficient(D), nonlinear coefficient(γ) are shown in Table 1.

At the receiver, to realize the coherent detection, the signals are split into two orthogonal polarizations by the polarization beam splitter (PBS) before they are mixed with the LO laser carrier.

Subsequently, the signals are sampled by the analog-to-digital converters (ADCs). After the compensation of chromatic dispersion using DSP module,²⁶ the CPR module is used to compensate for the laser phase noise generated from the lasers at the transmitter and the receiver. The frequency offset and the PMD are neglected in all simulations.



Figure 4. Schematic of the 9-channel Nyquist-spaced optical fibre communication system using EDC. (NPS: Nyquist pulse shaping, PBS: polarisation beam splitter, PBC: polarisation beam combiner, LO: local oscillator, ADC: analogue-to-digital convertor)

Table 1. Transmission Sy	stem Parameters
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Parameter	Value
Symbol rate	32 Gbaud
Channel Spacing	$32~\mathrm{GHz}$
Central wavelength(both transmitter and LO)	$1550~\mathrm{nm}$
Number of Channels	9 and 15
Roll-off	0.1%
Attenuation coefficient(α)	0.2 dB/km
Chromatic dispersion $\operatorname{coefficient}(D)$	17 ps/nm/km
Nonlinear coefficient(γ)	0 / W / km
Span length	80 km
EDFA noise figure	544 GHz

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4. RESULTS AND DISCUSSIONS

Numerical simulations have been carried out in the 32-Gbaud DP-16QAM transmission system with different scenarios. In all simulations we keep the linewidth of the Tx laser the same as that of the LO laser.



Figure 5. BER versus optical launch power in the 9-ch, 32-Gbaud back-to-back transmission system with the linewidth of 1.5 MHz under DP-16QAM, DP-64QAM and DP-256QAM modulation formats.



Figure 6. Simulated curves of BER versus optical launch power in the 9-ch 32-Gbaud DP-QPSK transmission system with the linewidth of 1.5 MHz over the 40×80 km field link.

First we carried out an simulation in the 9-ch 32-Gbaud back-to-back transmission system with the linewidth of 1.5 MHz. Figure 5 provides the variation of BER versus optical launch power under different modulation formats, processed respectively by Viterbi-Viterbi carrier phase recovery algorithm(VV CPR) and Modified

Viterbi-Viterbi carrier phase recovery algorithm(MVV CPR). From the figure we can see that both VV CPR and MVV CPR greatly suppress the laser phase noise, and the effects of MVV CPR behaves better than VV CPR in all modulation formats.



Figure 7. The variation of BER versus optical launch power of 500 kHz and 1 MHz processed respectively by VV CPR and MVV CPR in the 9ch DP-64QAM system.

Then simulations have been implemented in the 9-ch 32-Gbaud DP-QPSK transmission system with the linewidth of 1.5MHz over the 40×80 km field link. From Figure 6 we can see that Viterbi-Viterbi carrier phase recovery algorithm could significantly compensate the laser phase noise.



Figure 8. The variation of BER versus optical launch power of 500 kHz and 1 MHz processed respectively by VV CPR and MVV CPR in the 15-ch DP-64QAM system.

Further simulations were also performed in the 9-ch 32-Gbaud DP-64QAM transmission system and 15-ch 32-Gbaud DP-64QAM transmission system over the 10×80 km field link with different linewidths. The variation of BER versus optical launch power of 500 kHz and 1 MHz processed respectively by VV CPR and MVV CPR in the 9ch system are summarized in Figure 7, and the results of 15ch system are illustrated in Figure 8. Compared with the results of the back-to-back system, the advantages of MVV are more prominent here. In the same system, the BER of the data processed by MVV CPR behaves one order of magnitude lower than that of the data processed by VV CPR. This gap can be further increased as the optical launch power grows. As shown in Figure 7 and Figure 8, the maximum improvement reaches three orders of magnitude. Besides, it can be seen that the reduction in BER caused by MVV can completely offset the damage to system performance caused by the 500 kHz increase in linewidth (from 500 kHz to 1 MHz). When the optical launch power is large enough, the BER of the system with the linewidth of 1 MHz processed by MVV CPR can be even one order of magnitude lower than that of the system with the linewidth of 500 kHz processed by VV CPR.

5. CONCLUSIONS

In this work, we have studied the impact of the laser phase noise and have developed a modified Viterbi-Viterbi carrier phase recovery algorithm. Numerical simulations have been carried out to illustrate the improvement in system performance caused by MVV CPR compared to traditional VV CPR. Simulation results indicate that the BER improvement by MVV can reach one order of magnitude under the same linewidth. Besides, the BER reduction brought by MVV can offset the performance degradation from the increase of laser linewidth by 500 kHz. Specifically, when the optical launch power is large enough, the BER of the system with the linewidth of 1 MHz processed by MVV CPR could be one order of magnitude lower than the BER of the system with the linewidth of 500 kHz processed by the traditional VV CPR.

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