

# Origin of High Mobility in Molybdenum-Doped Indium Oxide

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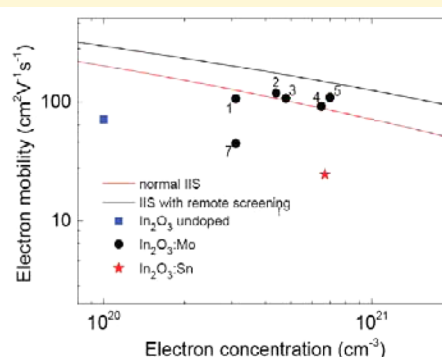
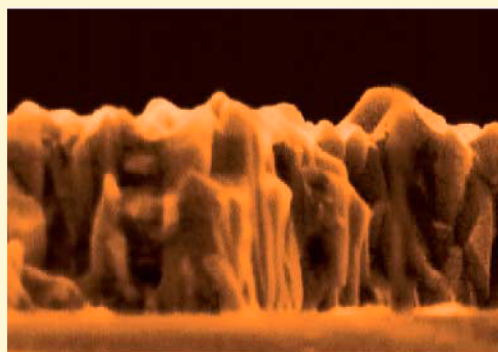
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**S** Supporting Information



**ABSTRACT:** Molybdenum-doped indium oxide (IMO) thin films prepared by aerosol-assisted chemical vapor deposition (AACVD) show significantly improved charge carrier mobilities as compared to nominally undoped films prepared by the same technique. The basis for this very unusual behavior has been investigated by density functional theory calculations using a hybrid Hamiltonian, mobility modeling, X-ray photoemission, and X-ray absorption spectroscopies. In contrast to previous claims that Mo acts as a three-electron donor, it is shown that substitutional Mo traps two electrons in localized states falling within the bulk bandgap and thus Mo is a simple one-electron donor. At the same time, there is very little hybridization of Mo 4d states with In 5s states at the bottom of the conduction band. This results in conduction that is spatially separated to some degree from the donors, giving rise to significantly reduced ionized impurity scattering, enhancing the carrier mobility. This is in contrast to Sn-doped  $\text{In}_2\text{O}_3$  where the conduction band minimum has significant Sn 5s character, resulting in regular ionized impurity scattering.

## 1. INTRODUCTION

Indium oxide ( $\text{In}_2\text{O}_3$ ) is amenable to degenerate n-type doping with tin to give a transparent conducting oxide (TCO) that combines optical transparency in the near-infrared and visible regions with a high electrical conductivity.<sup>1</sup> So-called indium tin oxide or ITO is still the most widely used conducting window material in photovoltaic devices, liquid crystal displays, and light-emitting diodes, despite the high material cost of indium.<sup>2–5</sup> This is a consequence of a relatively small fundamental bandgap that allows the charge neutrality level to fall well above the conduction band minimum, thus ensuring a high intrinsic dopability.<sup>6</sup> At the same time, optical transitions from the top of the valence band into the conduction band have very low oscillator strength so that indium oxide and ITO thin films remain transparent across the whole of the visible region.<sup>7</sup> The optimal room temperature electron mobility for nominally undoped indium oxide as found in high-quality thin films grown on (111) oriented yttrium-doped

zirconium dioxide substrates by oxygen plasma assisted molecular beam epitaxy is around  $225 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ .<sup>8</sup> Carrier concentrations on the order of  $1 \times 10^{17} \text{ cm}^{-3}$  found in these materials arise from adventitious donor doping, attributed to oxygen vacancies.<sup>8</sup> As is usual in semiconductor systems, n-type doping with an element (Sn) to the right of the host (In) in the periodic table leads to an increase in the charge carrier concentration, but also to a decrease in carrier mobility to values around  $70 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  for carrier densities in the mid  $1 \times 10^{20} \text{ cm}^{-3}$  range.<sup>1</sup> The latter is a consequence of the fact that the states close to the conduction band minimum have a strong contribution from the Sn 5s orbitals of the dopant atoms so that there is pronounced ionized impurity scattering.

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A common problem with heavily doped TCO materials is that the conduction electron plasmon energy lies in the near IR region, limiting the window of optical transparency.<sup>9–15</sup> Immediately above the plasmon energy a TCO material is transparent but below the film is highly reflecting. In addition, there is a strong absorption around the plasmon energy itself and this may intrude on the visible region at high carrier densities, especially for materials with low mobility where the plasma edge is strongly broadened by carrier lifetime effects. For this reason, high conductivity is best achieved by combining high mobility with relatively low carrier densities, rather than with high carrier densities and relatively low mobility.

Against this background, there has been a growing interest in the past few years in  $\text{In}_2\text{O}_3$  films incorporating alternative transition metal dopants including Mo, W, Nb, and Ti.<sup>16–21</sup> Mo has been of particular interest because of the remarkably high mobilities that have been found even in polycrystalline films. Thus, Gupta et al. claimed a mobility of  $250 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  at a carrier density of  $3.5 \times 10^{20} \text{ cm}^{-3}$  in thin films containing 2 atomic % Mo grown by pulsed laser deposition on quartz substrates held at  $500^\circ\text{C}$  under a background oxygen pressure of  $10^{-3}$  mbar.<sup>16</sup> This is an even higher mobility than the  $\text{cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  reported for a high-quality, single-crystalline, undoped  $\text{In}_2\text{O}_3$  thin film grown by plasma-assisted molecular beam epitaxy for an electron concentration of only  $5 \times 10^{16} \text{ cm}^{-3}$ .<sup>22</sup> The reason why the mobility in a polycrystalline film can exceed that found in epitaxial films of the highest quality remains unclear, however, although it is widely believed that Mo can act as a three-electron donor and it has therefore been argued that the ratio between charge carriers and scattering centers should be lower than with single electron donors such as Sn.<sup>23</sup> Although ionized impurity scattering-limited mobility for triply charged donors is expected to be one-third that for singly charged donors, if all other properties are equal.<sup>24</sup>

In the present study,  $\text{Mo:In}_2\text{O}_3$  films were prepared on silica-coated float glass substrates by aerosol-assisted chemical vapor deposition (AACVD). Mo/In in the precursor solution was varied from 1 to 7 mol %. To compare against  $\text{Mo:In}_2\text{O}_3$  samples, we also prepared Sn-doped  $\text{In}_2\text{O}_3$  (Sn/In in precursor solution kept at 2 mol %) by AACVD. It emerges that the Mo-doped films prepared in this way have a carrier concentrations of between  $3 \times 10^{20} \text{ cm}^{-3}$  and  $7 \times 10^{20} \text{ cm}^{-3}$ , up to a factor of 7 higher than for nominally undoped films prepared by the same technique. At the same time, the mobility of the charge carriers increases from  $71 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  for nominally undoped films to up to  $119 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  for a carrier density of  $4.4 \times 10^{20} \text{ cm}^{-3}$ . The latter mobility value is remarkably high for a polycrystalline film prepared by a relatively crude deposition technique at this carrier density. For the highest carrier density obtained of  $7 \times 10^{20} \text{ cm}^{-3}$ , the mobility is only reduced to  $109 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  producing a very low resistivity of  $8.3 \times 10^{-5} \Omega \text{ cm}$ .  $\text{Mo:In}_2\text{O}_3$  with Mo/In kept at 2 mol % in the precursor solution showed the highest charge carrier mobility. Thus, a  $\text{Sn:In}_2\text{O}_3$  thin films with Sn/In kept at 2 mol % was synthesized as a comparison. To help explain the surprising increase in mobility with Mo doping, we have carried out density functional theory calculations using a hybrid Hamiltonian, which faithfully reproduces the bulk band gap of  $\text{In}_2\text{O}_3$  itself. Unlike in previous calculations, which used the local density approximation,<sup>25</sup> we find that each Mo dopant atom traps two electrons in localized Mo 4d states lying in the bulk band gap so that Mo acts as a single rather than triple electron donor. These localized states are seen directly in valence band X-ray photoemission spectra.

## 2. EXPERIMENTAL AND COMPUTATIONAL DETAILS

**Deposition Procedure.** Depositions were carried out under nitrogen (99.99% from BOC). Precursors were placed in a glass bubbler and an aerosol mist was created using a piezoelectric device.<sup>26–29</sup> All chemicals were procured from Aldrich and were used as received.

$\text{Mo:In}_2\text{O}_3$  thin films were prepared from  $\text{InCl}_3 \cdot \text{H}_2\text{O}$  (0.4 g, 8.8 mmol) dissolved in methanol (25 mL) and  $(\text{NH}_4)_6\text{Mo}_7\text{O}_{24} \cdot 4\text{H}_2\text{O}$  was added (1, 2, 3, 4, 5, and 7 mol %). As a comparison an  $\text{Sn:In}_2\text{O}_3$  thin film was prepared from  $\text{InCl}_3 \cdot \text{H}_2\text{O}$  (0.4 g, 8.8 mmol) dissolved in methanol (25 mL) and  $\text{C}_4\text{H}_9\text{SnCl}_3$  was added (2 mol %). The solutions were stirred for 30 min and then atomized. The precursor flow was kept at  $0.6 \text{ l min}^{-1}$ . The glass substrate was  $\text{SiO}_2$  precoated (ca. 50 nm thick  $\text{SiO}_2$  barrier layer) standard float glass (NSG)  $15 \text{ cm} \times 4 \text{ cm} \times 0.3 \text{ cm}$ . A top plate was suspended 0.5 cm above the glass substrate to ensure a laminar flow. The substrate was maintained at a temperature of  $450^\circ\text{C}$  for a deposition time of 45 min. After the deposition, the bubblers were closed and the substrates were cooled under a flow of nitrogen. The glass substrate was allowed to cool with the graphite block to less than  $100^\circ\text{C}$  before it was removed. Coated substrates were handled and stored in air. The coated glass substrate was cut into ca.  $1 \text{ cm} \times 1 \text{ cm}$  squares for subsequent analysis.

**Film Characterization.** Powder X-ray diffraction (PXRD) patterns were measured in a modified Bruker-Axs D8 diffractometer with parallel beam optics and a PSD LynxEye silicon strip detector. This instrument uses an unmonochromated  $\text{Cu K}\alpha$  source operated at 40 kV with 30 mA emission current. The incident beam angle was set at  $1^\circ$  and the angular range of the patterns collected was  $10^\circ < 2\theta < 66^\circ$  with a step size of  $0.05^\circ$  counted at 0.5 s/step.

Scanning electron microscopy (SEM) was performed to determine surface morphology and film thickness using a JEOL JSM-6301F field-emission SEM at an accelerating voltage of 5 keV.

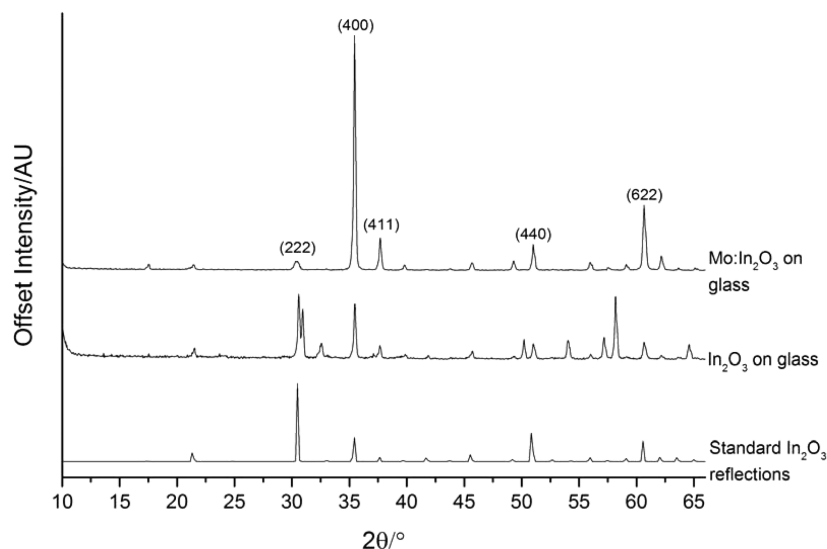
Hall effect measurements were carried out using the van Der Pauw method to determine the bulk resistivity ( $\rho$ ), sheet resistance, free carrier concentration ( $N$ ), and mobility ( $\mu$ ). A square array of Ohmic contacts arranged on  $1 \text{ cm}^2$  samples were then subjected to an input current of 1 mA and a calibrated magnetic field of 0.58 T. The transverse voltage was then measured. The measurement was repeated by reversing the direction of the magnetic field and the current.

Optical spectra were taken using a PerkinElmer Fourier transform Lambda 950 spectrometer over a wavelength range of 200 to 2250 nm (6.2 to 0.55 eV) in both transmission and reflection modes. This range embraces the ultraviolet (UV), visible, and near-infrared (NIR) regions. The spectra were referenced against an air background.

X-ray photoelectron spectroscopy (XPS) was performed in a Thermo Scientific K-alpha photoelectron spectrometer using monochromatic  $\text{Al-K}\alpha$  radiation. Survey scans were collected in the range 0–1100 eV (binding energy) at a pass energy of 160 eV. Higher-resolution scans were recorded for the main core lines at a pass energy of 20 eV. Valence band spectra were also recorded. Peak positions were calibrated using the C 1s peak and plotted using the CasaXPS software.

Mo/In K-edge X-ray absorption spectra (XAS) were measured on beamline (B18) at the UK synchrotron, Diamond, which operates at 3 GeV and 300 mA. The beamline is equipped with  $\text{Si}(111)$  double crystal monochromator, ion chambers for measuring incident and transmitted beam intensity and a 9 element Ge fluorescence detector for measurement in fluorescence mode. All the measurements were carried out in fluorescence mode and typically 6 scans were averaged to produce the spectra. Spectra were processed using ATHENA software and subsequent analysis of the EXAFS data were performed using EXCURVE.<sup>30,31</sup>

**Computational Methods.** All our DFT calculations were performed using the VASP code,<sup>32</sup> with interactions between the cores (In: [Kr], Mo: [Xe] and O: [He]) and the valence electrons described using the PAW method.<sup>33</sup> The calculations were performed using the HSE06 hybrid functional as proposed by Krukau et al.<sup>34</sup> In the HSE06 approach, a value of exact nonlocal exchange,  $\alpha$ , of 25%, and screening parameter of  $\omega = 0.11 \text{ bohr}^{-1}$  are added to the Perdew Burke Ernzerhof PBE formalism. The HSE06 approach has been proven to result in structural and band gap data in better agreement with experiment than standard



**Figure 1.** PXRD of nominally undoped  $\text{In}_2\text{O}_3$  and  $\text{Mo:In}_2\text{O}_3$  thin film samples prepared by the AACVD of  $\text{InCl}_3 \cdot x\text{H}_2\text{O}/(\text{NH}_4)_6\text{Mo}_7\text{O}_{24} \cdot 4\text{H}_2\text{O}$  with MeOH. Note the metastable rhombohedral  $\text{In}_2\text{O}_3$  phase in nominally undoped  $\text{In}_2\text{O}_3$  sample.

**Table 1.** Film Thickness, Sheet Resistance, Specific Resistivity, Charge Carrier Mobility, and Charge Carrier Density of a Nominally Undoped  $\text{In}_2\text{O}_3$  Film, a  $\text{Sn:In}_2\text{O}_3$  Film, and a Series of  $\text{Mo:In}_2\text{O}_3$  Films

Mo:In or Sn:In in solution (mol %)	film thickness (nm)	sheet resistance ( $\Omega \text{ sq}^{-1}$ )	$\rho$ ( $\Omega \text{ cm}$ )	$\mu$ ( $\text{cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ )	$N$ ( $\text{cm}^{-3}$ )
0	700	11.0	$7.7 \times 10^{-4}$	71	$1.1 \times 10^{20}$
2 Sn	680	5.6	$3.8 \times 10^{-4}$	25	$6.7 \times 10^{20}$
1 Mo	610	3.1	$1.9 \times 10^{-4}$	107	$3.1 \times 10^{20}$
2 Mo	650	1.8	$1.2 \times 10^{-4}$	119	$4.4 \times 10^{20}$
3 Mo	650	1.8	$1.2 \times 10^{-4}$	107	$4.8 \times 10^{20}$
4 Mo	680	1.8	$1.2 \times 10^{-4}$	92	$6.5 \times 10^{20}$
5 Mo	680	1.2	$8.3 \times 10^{-5}$	109	$7.0 \times 10^{20}$
7 Mo	651	6.9	$4.5 \times 10^{-4}$	45	$3.1 \times 10^{20}$

DFT functionals<sup>7,35–38</sup> and, crucially, to provide an excellent description of the electronic structure of  $\text{In}_2\text{O}_3$ . A planewave cutoff of 400 eV and a  $k$ -point sampling of gamma-centered  $3 \times 3 \times 3$  for the 40 atom primitive cell of  $\text{In}_2\text{O}_3$  was used, with the structure deemed to be converged when the forces on all the atoms were less than  $0.01 \text{ eV } \text{Å}^{-1}$ .

All oxygen sites in the bixbyite structure are equivalent with four indium nearest-neighbors, whereas there are two distinct cation sites ( $8b$  and  $24d$  in Wyckoff notation) that are each coordinated to 6 anions in distorted octahedra. One quarter of all the cations occupy the  $8b$  position, with the remaining three-quarters occupying the  $24d$  positions. In ITO only tin doping on the indium  $b$ -sites results in active donors.<sup>39,40</sup> We have tested the incorporation of one Mo into the 40 atom primitive cell of  $\text{In}_2\text{O}_3$  (i.e., replacing 6.25% of the In atoms) on both the  $8b$  and  $24d$  sites. Mo is 0.32 eV more stable on the  $8b$  site, indicating that it will have a very strong preference at room temperature and above for taking up this site. Previously, it was predicted that the  $8b$  site was only 0.04 eV more favorable using the LDA method;<sup>25</sup> however, the discrepancy in these energy differences is as of yet unexplained. Nevertheless, the trend of Mo preferentially sitting on the  $8b$  site is maintained. Our calculated lattice constants for cubic  $\text{In}_2\text{O}_3$  is 10.16 Å, which is within 0.40% of the experimental lattice, whereas the calculated band gap at the HSE06 level is 2.75 eV in good agreement with experimental measurements.<sup>37</sup>

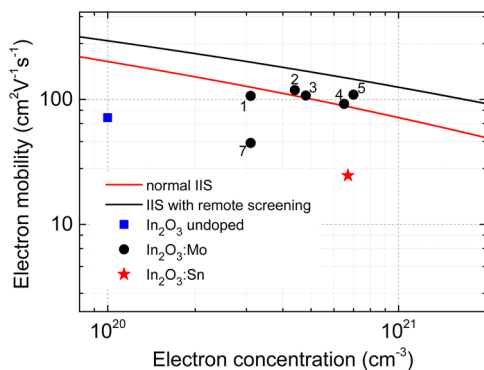
### 3. RESULTS AND DISCUSSION

#### XRD, Hall Effect, Optical, and SEM Characterization.

The films deposited were uniform, showed excellent coverage across the glass substrates and were adherent, passing the Scotch tape test. X-ray diffraction patterns of the as-deposited films formed by AACVD (Figure 1) confirmed the presence of  $\text{In}_2\text{O}_3$ .

The nominally undoped  $\text{In}_2\text{O}_3$  films contained both the metastable rhombohedral  $\text{In}_2\text{O}_3$  phase<sup>41</sup> as well as the cubic bixbyite  $\text{In}_2\text{O}_3$  phase. When molybdenum was introduced into the system only the bixbyite  $\text{In}_2\text{O}_3$  phase was observed. Molybdenum doping of  $\text{In}_2\text{O}_3$  also resulted in pronounced (100) texture.

The Hall effect measurements were performed at room temperature with the samples in van der Pauw configuration. The nominally undoped  $\text{In}_2\text{O}_3$ ,  $\text{Sn:In}_2\text{O}_3$ , and  $\text{Mo:In}_2\text{O}_3$  samples all showed n-type conductivity (Table 1). The charge carrier mobility and charge carrier concentration for nominally undoped  $\text{In}_2\text{O}_3$  were  $71 \text{ cm}^2/(\text{V s})$  and  $1 \times 10^{20} \text{ cm}^{-3}$ , respectively. The specific resistivity decreased with molybdenum doping as a consequence of an increase in both the charge carrier concentration and the charge carrier mobility. As shown in Figure 2, the carrier density increased to between  $3.1 \times 10^{20}$  and  $7.0 \times 10^{20} \text{ cm}^{-3}$  for between 1 and 5 mol % Mo and the mobility increased to between 92 and  $119 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ . The charge carrier concentrations in both nominally undoped  $\text{In}_2\text{O}_3$  and  $\text{Mo:In}_2\text{O}_3$  are much lower than in commercial ITO thin films, making them ideal for applications that require NIR transparency. The carrier density and mobility of an ITO film deposited by AACVD are also shown in Figure 2. Finally, the Hall effect results from the film prepared using 7 mol % Mo in Figure 2 indicate a lower mobility of  $45 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  at the same carrier density as the 1 mol % Mo film of  $3.1 \times 10^{20} \text{ cm}^{-3}$ . This corresponds to over-doping with excess Mo atoms acting as acceptors, compensating the donors and giving an increased density of ionized impurities to scatter electrons and reduction of the mobility.



**Figure 2.** Electron mobility and concentration for undoped, Sn-doped and Mo-doped  $\text{In}_2\text{O}_3$ . The numbers by the data points correspond to the mol % of Mo dopant in the solution used in the AACVD. The model curves for regular ionized impurity scattering (IIS) (red line) and for remotely screened IIS (black line). All calculations are for singly ionized Mo donor atoms.

Also shown in Figure 2 is the ionized impurity scattering-limited mobility as a function of carrier density calculated using the Brooks–Herring–Dingle model<sup>42</sup> including degeneracy and conduction band nonparabolicity with a conduction band edge effective mass of  $0.30m_0$ .<sup>22</sup> All calculations are for Mo donor atoms that are singly charged as justified by the DFT, XPS, and EXAFS results below. Ionized impurity scattering is dominant at carrier densities above  $1 \times 10^{20} \text{ cm}^{-3}$ , but the mobility can be expected to be reduced slightly further by polar optical phonon scattering.<sup>22</sup> Two curves are shown, the lower mobility one that simply represents regular ionized impurity scattering and the higher mobility one that includes a factor accounting for “remote” impurities as described below. Four of the experimental data points correspond to mobilities higher than the regular ionized impurity scattering limit. This result alone implies that conventional ionized impurity scattering cannot account for the observed mobilities. If an additional factor accounting for “remote” impurities is included, the higher mobility curve is obtained that is above all the experimental data points.

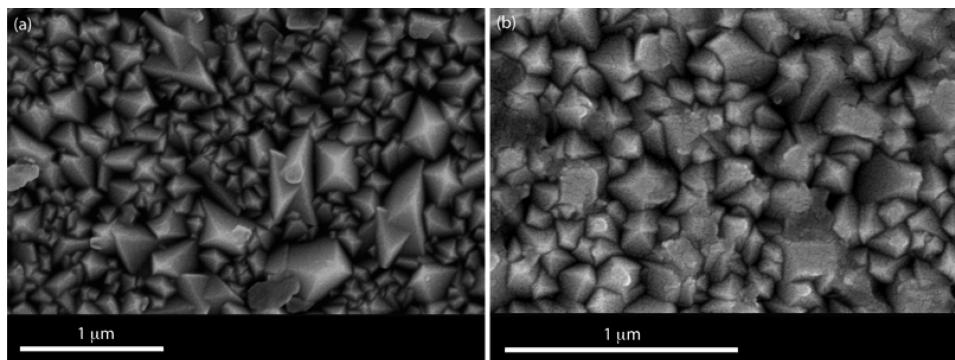
If the donor center does not contribute significantly to the conduction band minimum, as is the case here for Mo as determined below from our DFT results, the amplitude of the conduction band wave function in the vicinity of the donor center is small. Therefore, the conduction electrons do not experience scattering by the dopant’s screened Coulomb potential to the same extent as in Sn-doped  $\text{In}_2\text{O}_3$  where the Sn atoms do contribute significant orbital character to the

bottom of the conduction band. In this sense, the Mo dopant atoms can be considered as being “remote” impurities, at least compared with the Sn atoms in ITO. This is also the case for La-doped  $\text{BaSnO}_3$ , which exhibits high mobility as a result of the La orbitals lying several electron volts above the conduction band minimum rather than close in energy to it.<sup>43</sup>

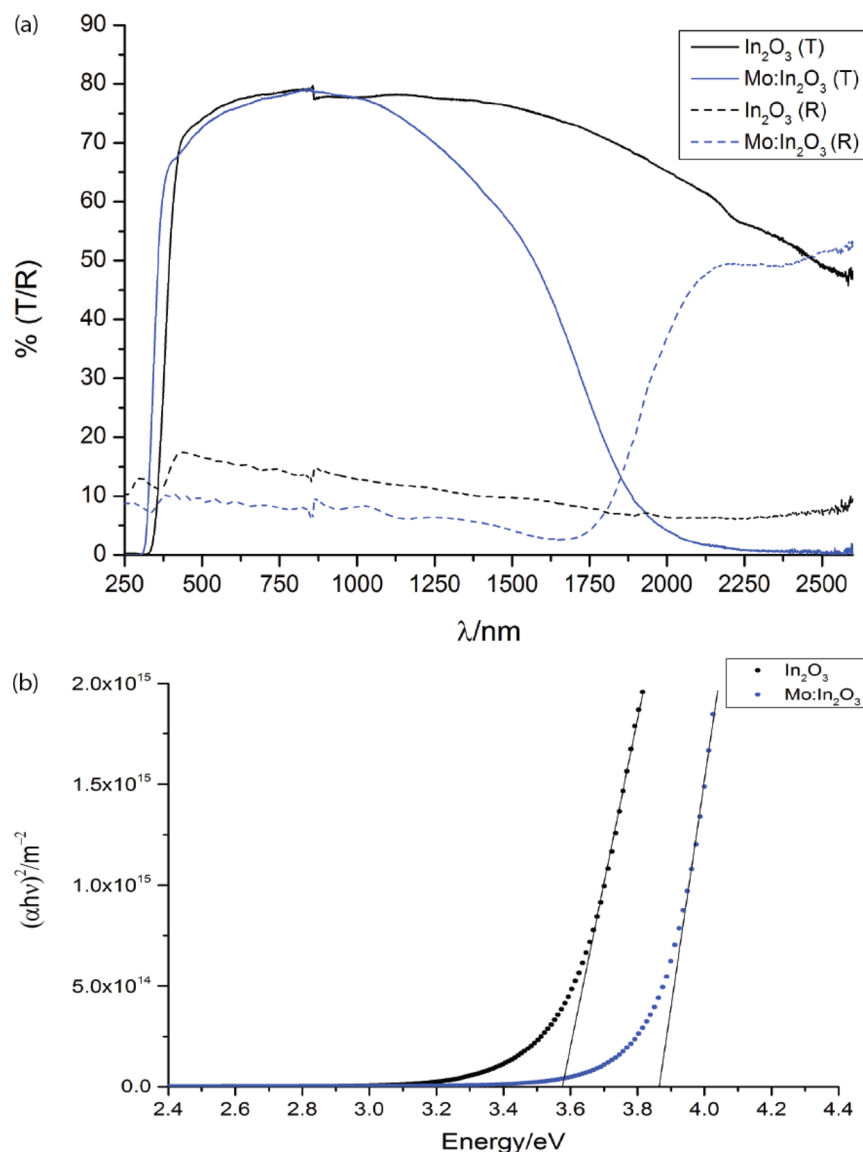
To make a difference, the separation of the Mo donors from the indium atoms that do contribute to the conduction band minimum needs to be comparable to the Thomas-Fermi screening length. If the In atoms have a distance  $d$  from the Mo donor atoms that is comparable to the Thomas Fermi screening length,  $\lambda_{\text{TF}}$ , then the Coulomb interaction that produces ionized impurity scattering is reduced by a factor  $\exp(-d/\lambda_{\text{TF}})$ . To estimate the magnitude of this effect, we will consider the minimum Mo–In separation of  $3.36 \text{ \AA}$  (see EXAFS results below), and Thomas-Fermi screening lengths of between  $9.1$  and  $5.3 \text{ \AA}$  for carrier densities of between  $8 \times 10^{19}$  and  $2 \times 10^{21} \text{ cm}^{-3}$ . This gives Coulomb scattering of between  $0.53$  and  $0.69$  times what it would be for the case of regular impurities in this carrier density range. And the corresponding enhancements of the ionized impurity scattering limited mobility range from  $1/0.69 = 1.4$  to  $1/0.53 = 1.9$  times. The resulting mobility versus carrier density curve is shown as the black line in Figure 2.

This situation is in part analogous to modulation doping of AlGaAs/GaAs heterostructures where the dopant atoms are located in the AlGaAs layers while the resulting conduction electrons flow through the spatially separated GaAs layer.<sup>44</sup> As a result, the electrons do not experience ionized impurity scattering by the dopants from which they originated. A similar but less dramatic spatial separation occurs in the current situation of the donor atom orbitals not contributing significantly to the bottom of the conduction band. Additionally, a different but related phenomenon has also been reported in nanoscale metal oxide semiconductor field effect transistors, whereby the ionized impurities in the channel are remotely screened by the close proximity of the highly doped, degenerate source and drain regions.<sup>45</sup>

The film microstructure and thickness was probed using SEM. The nominally undoped and molybdenum doped  $\text{In}_2\text{O}_3$  films both displayed a similar microstructure based on pyramidal crystallites with a particle size of around  $300\text{--}500 \text{ nm}$  (Figure 3). The surface microstructure of these films make them potentially useful as electrodes in silicon based solar cells where there is a need to increase the path length of incident light that can be achieved through optical scattering. The SEM of the  $2 \text{ mol \%}$  Sn-doped sample revealed similar sized grains as for the Mo-doped



**Figure 3.** SEM images of (a) nominally undoped  $\text{In}_2\text{O}_3$  and (b) Mo: $\text{In}_2\text{O}_3$  thin films deposited on silica coated float-glass substrates by the AACVD reaction of  $\text{InCl}_3 \cdot x\text{H}_2\text{O}/(\text{NH}_4)_6\text{Mo}_7\text{O}_{24} \cdot 4\text{H}_2\text{O}$  and methanol at  $450 \text{ }^\circ\text{C}$ .



**Figure 4.** UV/vis spectra (T/R) of nominally undoped and Mo:In<sub>2</sub>O<sub>3</sub> films prepared by the aerosol assisted chemical vapor deposition (AACVD) reaction of InCl<sub>3</sub>·xH<sub>2</sub>O/(NH<sub>4</sub>)<sub>6</sub>Mo<sub>7</sub>O<sub>24</sub>·4H<sub>2</sub>O with MeOH on silica coated float glass substrates at 450 °C.

samples but with inferior grain connectivity. The latter property probably accounts to some extent for the measured mobility for the Sn-doped film being lower than the optimum achieved for polycrystalline ITO.

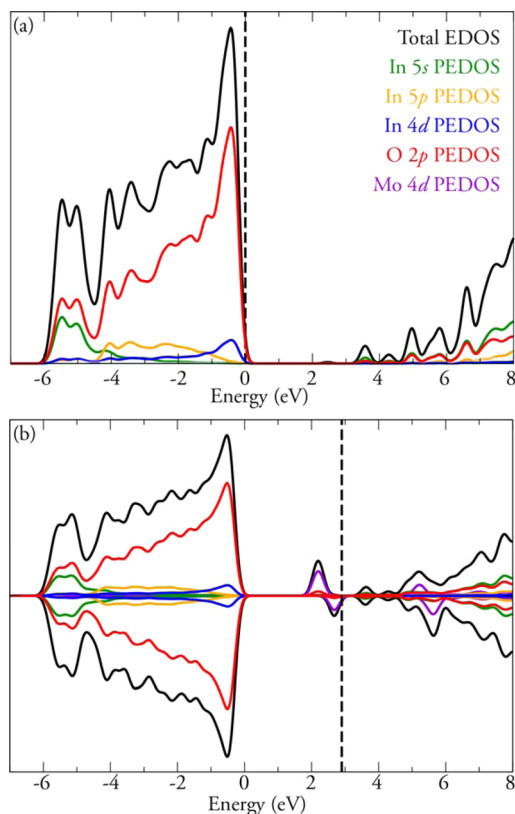
Optical spectra across the UV, visible and near IR regions were collected for nominally undoped In<sub>2</sub>O<sub>3</sub> and Mo:In<sub>2</sub>O<sub>3</sub> thin films in transmittance and reflectance geometry between 250 and 2250 nm and are shown in Figure 4. It can be seen that nominally undoped In<sub>2</sub>O<sub>3</sub> films prepared within the AACVD system have a transmittance of up to 80% in the visible region with an average of ~75% between 400–2000 nm. Similar high NIR transmittance was previously observed in nominally undoped SnO<sub>2</sub> and In<sub>2</sub>O<sub>3</sub> films having similar charge carrier concentrations but with considerably lower charge carrier mobilities.<sup>46,47</sup>

It is also evident from Figure 4a that with molybdenum doping, the transmittance in the visible region with wavelengths lower than 1000 nm (1.2 eV) remains essentially unaltered at just under 80%. The transmittance drops above 1000 nm in the IR because of increasing reflectivity and absorption on approaching and moving through the plasmon energy, which is estimated

from the energy at which the reflectivity reaches half its maximum value to be about 0.64 eV (1950 nm), in satisfactory agreement with the Hall carrier density. A similar carrier density may also be inferred from analysis of the In 3d core line (not shown), where final state structure due to final state screening and excitation of plasmon satellites is found.<sup>48–50</sup> In addition to the changes at long wavelength, Mo doping leads to a shift in the UV absorption onset to higher energy because of blocking of states at the bottom of the conduction band. Figure 4b shows the blue shift in a Tauc plot of (αhν)<sup>2</sup> versus photon energy hν is from 3.55 to 3.85 eV, a shift of about 0.30 eV (here α is the absorption coefficient).<sup>51,52</sup> This is the size expected when the carrier density increases from 1.1 × 10<sup>20</sup> cm<sup>-3</sup> to 4.4 × 10<sup>20</sup> cm<sup>-3</sup>, considering the influence of conduction band nonparabolicity.<sup>53,54</sup>

#### Density Functional Theory and Electronic Structure.

The full and partial densities of states of both pure and Mo-doped In<sub>2</sub>O<sub>3</sub> calculated using hybrid DFT are displayed in Figure 5a, b. The valence band of undoped In<sub>2</sub>O<sub>3</sub> is dominated by O 2p states, hybridized with In 5s states at the bottom of the valence band, In 5p states in the middle of the band and In 4d states at the top of



**Figure 5.** HSE06 calculated total and partial energetic density of states for (a) pure  $\text{In}_2\text{O}_3$  and (b) one Mo dopant on the 8b site in a 40 atom primitive cell corresponding to a carrier density of about  $1.9 \times 10^{21} \text{ cm}^{-3}$ . The valence band maximum is set to 0 eV. The dashed lines indicate the highest occupied states.

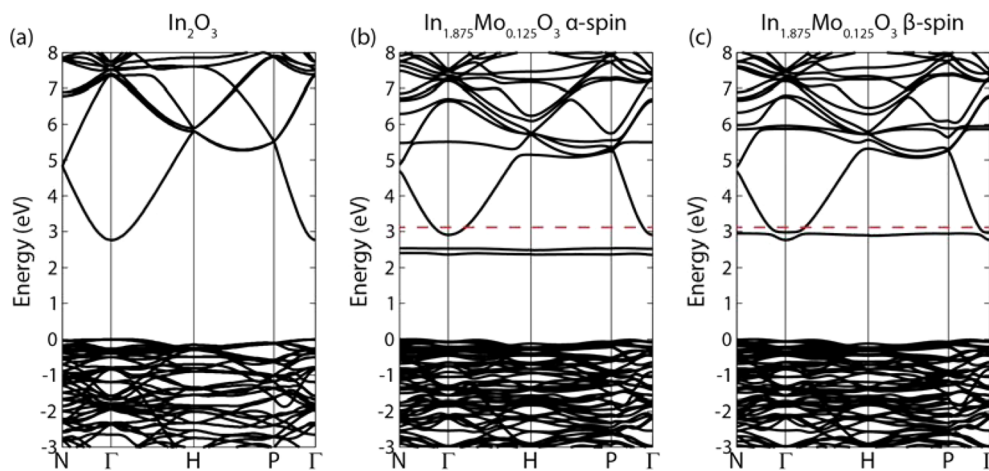
the band. The bottom of the conduction band is of dominant In 5s character but with strong hybridization with O 2p states. The experimental band gap of 2.9 eV<sup>54</sup> is reproduced quite well by the calculation, which gives a value of 2.75 eV. Mo doping shifts the Fermi level up above the conduction band minimum (CBM) but also introduces new Mo 4d states into the bulk band gap. Moreover there is no shrinkage in the energy between the CBM and the valence band minimum (VBM). Looking at the

band structure itself (Figure 6) we find that undoped  $\text{In}_2\text{O}_3$  has a strongly dispersing conduction band with a minimum at the  $\Gamma$  point and a VBM composed of relatively flat bands. For Mo-doped  $\text{In}_2\text{O}_3$  additional states of dominant Mo 4d character appear both above and below the CBM. Specifically two localized  $t_{2g}$   $\alpha$ -spin (spin-up) states are found in the band gap below the CBM, while the  $\beta$ -spin  $t_{2g}$  state lies above the CBM at the  $\Gamma$  point. This indicates that Mo is only donating 1 electron to the conduction band. Thus, in bulk  $\text{In}_2\text{O}_3$ , the Mo dopant is 4+ and not 6+ as had been previously postulated.<sup>23,55</sup> In addition, careful analysis of the contribution of Mo states to the conduction band revealed that at the  $\Gamma$  point the Mo contribution to states at the CBM is less than 3%. The flat band above that has 74% Mo character, indicating that the Mo states lie above the CBM, but with very little hybridization with the CBM. The Mo donates one electron but does not get involved in the conduction band, and therefore conduction electrons do not scatter off the dopant center in the way that is the case for Sn-doped  $\text{In}_2\text{O}_3$ , where the conduction band minimum has a very strong contribution (10% for the same unit cell) from Sn 5s states.<sup>56</sup>

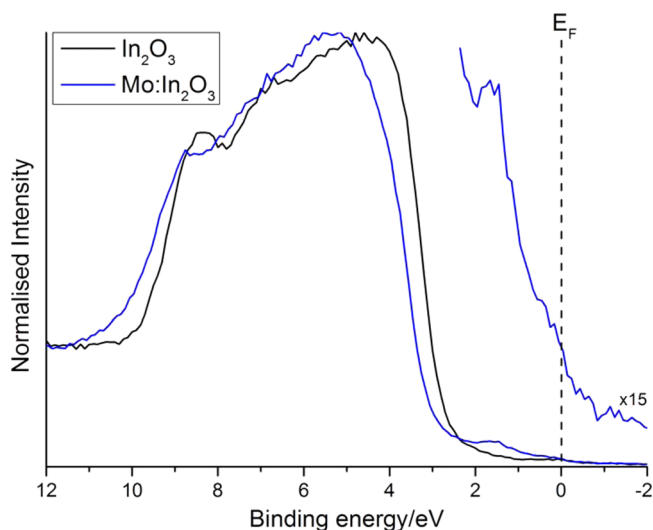
Mo-doping of  $\text{In}_2\text{O}_3$  has been examined previously by Medvedeva using computational methods, with the conclusion that Mo acts as a three-electron donor.<sup>25</sup> However, this study used the local density approximation (LDA) approach, which suffers from a severe band gap error and has been shown to erroneously favor delocalized electrons in semiconductors. A hybrid-DFT approach such as the HSE06 functional employed here rectifies these problems and yields a far more realistic electronic structure of a doped  $\text{In}_2\text{O}_3$ .<sup>57,58</sup>

**Valence Band XPS.** Valence band X-ray photoemission spectra are shown in Figure 7. The spectra are dominated by a broad valence band of O 2p states extending from the valence band onset to about 10 eV binding energy.

The valence band positions cannot simply be derived by linear extrapolation of the rising edge of the valence band to the baseline. It has been shown<sup>41</sup> that there is a rapid onset of the valence band density of states leading to an almost flat band. Broadening due to lifetime and instrument effects causes significant slope to the measured onset of the valence band. Therefore, extrapolating to the baseline results in a large underestimation in the VBM to surface Fermi level separation.



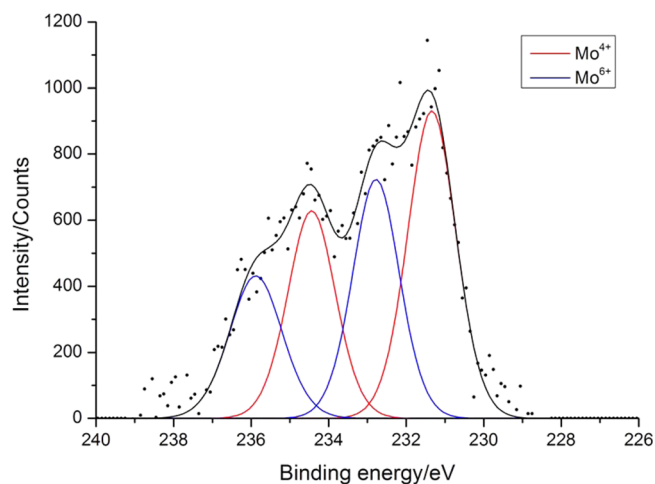
**Figure 6.** HSE06 calculated band structures for (a) pure  $\text{In}_2\text{O}_3$ , (b) spin up states for one Mo dopant on the 8b site in a 40 atom primitive cell, and (c) spin down states for one Mo dopant on the 8b site in a 40 atom primitive cell. The valence band maximum is set to 0 eV. The dashed red lines indicate the highest occupied states.



**Figure 7.** Normalized valence-band photoemission spectrum of nominally undoped  $\text{In}_2\text{O}_3$  and  $\text{Mo}:\text{In}_2\text{O}_3$  thin films deposited on glass substrates. Note the shift to higher binding energy for the  $\text{Mo}:\text{In}_2\text{O}_3$  sample because of Burstein–Moss filling of the conduction band. Also the  $\text{Mo}:\text{In}_2\text{O}_3$  sample shows Mo 4d states in the band gap consistent with computational results.

The shift of the onsets to higher binding energy for Mo-doped  $\text{In}_2\text{O}_3$  is indicative of population of the conduction band by excess charge carriers introduced by molybdenum doping and is analogous to the Burstein–Moss shift in optical spectra. More importantly the valence band photoemission data show occupied states in the bandgap, consistent with the computational results discussed above that revealed the presence of occupied localized Mo 4d states.

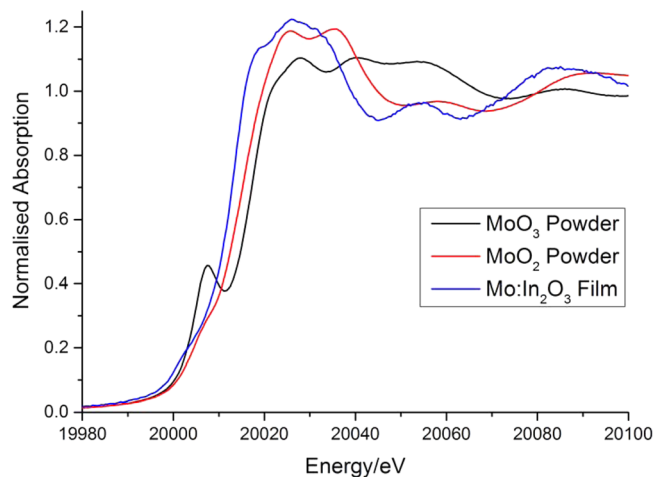
**Mo Core Level Spectroscopy.** Figure 8 shows the core photoemission spectrum the sample doped with 2% Mo in solution in the Mo 3d region. The effective Mo doping level in the near surface region was found to be 0.9%, corresponding to a Mo concentration of  $3 \times 10^{20} \text{ cm}^{-3}$ . Within the experimental uncertainty, this corresponds to the difference in carrier density between the nominally undoped and the doped films, strongly suggesting that Mo acts as a one-electron donor. To explore this idea further, we each fitted the Mo  $3d_{5/2}$  and Mo  $3d_{3/2}$  components of the spin–orbit doublet with a pair of Voigt functions superimposed on a Shirley background.<sup>19,23,59–62</sup> The high binding energy component found at 232.5 eV is at a similar energy to the value of 232.5 eV found in  $\text{MoO}_3$ <sup>59</sup> so the presence of  $\text{Mo}^{6+}$  in the near surface region can be inferred. This probably arises simply from oxidation of Mo close to the surface: similar contaminant structure has been observed for as-presented  $\text{MoO}_2$  and may be removed by extended annealing in UHV. Identification of the charge state associated with the low binding energy component is more problematic, although comparison may be made with  $\text{MoO}_2$ . The Mo 3d spectrum of this metallic oxide is complicated by final state screening by the very high density of mobile charge carriers giving a doublet of doublets with a shift of 1.73 eV between screened and unscreened peaks.<sup>59</sup> The binding energy of 231.3 eV found in the present work is very close to the value of 231.0 eV for the unscreened final state observed for  $\text{MoO}_2$ . Of course in IMO one might anticipate a superposition of screened and unscreened components similar to that found in the In 3d region. However, as was discussed above, Mo 4d states contribute very little to the conduction band and in this situation there will be minimal local final state screening of a



**Figure 8.** Mo 3d core level X-ray photoemission spectra of  $\text{Mo}:\text{In}_2\text{O}_3$  film prepared from the AACVD reaction of  $\text{InCl}_3 \cdot x\text{H}_2\text{O}/(\text{NH}_4)_6\text{Mo}_7\text{O}_{24} \cdot 4\text{H}_2\text{O}$  and methanol. The dots represent experimental data points and the solid lines are best fits to the data. The data was fitted with a Shirley background and Voigt components for the  $\text{Mo}^{4+}/\text{Mo}^{6+}$  environments.

Mo core hole, resulting in the absence of the screened  $\text{Mo}^{4+}$  component. Therefore, the lower binding energy doublet in Figure 8 is attributed to unscreened  $\text{Mo}^{4+}$  states and the higher binding energy doublet to conventional  $\text{Mo}^{6+}$  states associated with oxidized Mo at the surface.

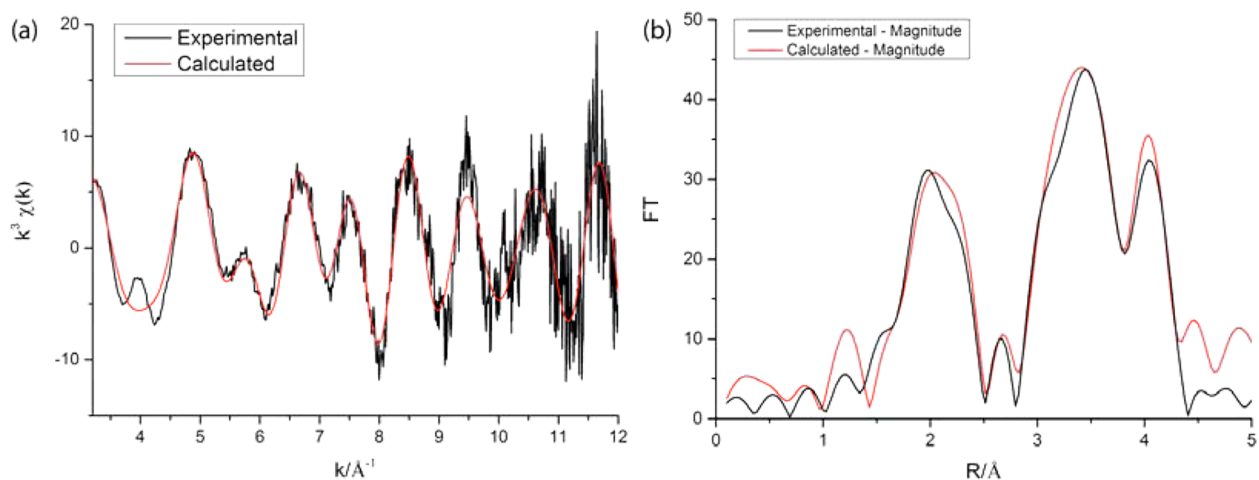
**X-ray Absorption Spectroscopy.** XAS was used as an additional probe of the electronic and geometric state of



**Figure 9.** Mo K-edge XANES of  $\text{Mo}:\text{In}_2\text{O}_3$  (2 mol % in solution) thin film and corresponding model compounds.

**Table 2. Structural Parameters Obtained from the Analysis of Mo K-Edge EXAFS Data on  $\text{Mo}:\text{In}_2\text{O}_3$  film**

system	atom pair	N–Co ordination number	R (Å), interatomic distance	$\sigma^2$ (Å <sup>2</sup> ), Debye–Waller
$\text{Mo}:\text{In}_2\text{O}_3$	Mo–O	6.4	2.05	0.012
	Mo–In	6.0	3.36	0.004
	Mo–In	6.0	3.82	0.006
$\text{In}_2\text{O}_3$	In–O	6	2.16	0.005
	In–In	6	3.36	0.005
	In–In	6	3.87	0.007



**Figure 10.** (a) Mo K-edge EXAFS for Mo:In<sub>2</sub>O<sub>3</sub> film and (b) associated Fourier transforms showing experimental and calculated data for real and imaginary components.

molybdenum atoms in Mo:In<sub>2</sub>O<sub>3</sub> in the bulk of the material. Although XPS measures tens of atomic layers into the sample, XAS is an atom-specific technique used to probe the bulk short-range structure. Figure 9 shows the Mo K-edge XANES for Mo:In<sub>2</sub>O<sub>3</sub> thin film, MoO<sub>2</sub>, and MoO<sub>3</sub> model compounds. It can clearly be seen that for MoO<sub>3</sub> there is a clear pre-edge feature at ca. 20 008 eV. The intensity of this pre-edge feature depends on the coordination around the metal center. The pre-edge intensity is greater for metal ions with tetrahedral coordination compared to octahedral coordination. The pre-edge intensity also depends on the electronic structure of the metal ions in a given oxidation state, for example d<sup>0</sup> systems showing a more intense pre-edge feature.<sup>63,64</sup> The MoO<sub>2</sub> model compound and Mo:In<sub>2</sub>O<sub>3</sub> do not exhibit this pre-edge feature, implying that Mo in Mo:In<sub>2</sub>O<sub>3</sub> is doping in the system as Mo<sup>4+</sup> consistent again with photo-emission and theoretical results.

Analysis of the Mo K-edge EXAFS data revealed that the average Mo–O distance of the first neighbor in Mo:In<sub>2</sub>O<sub>3</sub> thin film is ca 2.05 Å, shorter than the In–O distance in In<sub>2</sub>O<sub>3</sub> of ca. 2.16 Å, because of the smaller ionic radius of Mo<sup>4+</sup> in comparison to In<sup>3+</sup>. Importantly, the bond distance is more similar to MoO<sub>2</sub> and significantly different from MoO<sub>3</sub>, indicating no phase segregation to MoO<sub>2</sub>/MoO<sub>3</sub>. More striking differences between the structure of MoO<sub>2</sub> and the doped materials can be seen in the second and third neighbor distances; Mo–In distances were found to be similar to that observed for In–In in In<sub>2</sub>O<sub>3</sub>, which is very different from MoO<sub>2</sub>. The results of the analysis are given in Table 2, and the best fit between experimental data and the calculated Mo K-edge EXAFS along with the associated Fourier transforms of Mo:In<sub>2</sub>O<sub>3</sub> system are shown in Figure 10. These results clearly provide a direct evidence for the substitution of Mo<sup>4+</sup> ions in the In<sub>2</sub>O<sub>3</sub> lattice.

## CONCLUSIONS

AACVD was shown to be an effective method for the deposition of In<sub>2</sub>O<sub>3</sub> and Mo:In<sub>2</sub>O<sub>3</sub> thin films deposited on silica coated float glass via the AACVD reaction of unconventional CVD precursors InCl<sub>3</sub>·xH<sub>2</sub>O/(NH<sub>4</sub>)<sub>6</sub>Mo<sub>7</sub>O<sub>24</sub>·4H<sub>2</sub>O and methanol at a substrate temperature of 450 °C. Nominally undoped In<sub>2</sub>O<sub>3</sub> thin films gave surprisingly high charge carrier concentrations ( $1 \times 10^{20} \text{ cm}^{-3}$ ) and charge carrier mobilities ( $71 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ) comparable and superior to some intentionally doped In<sub>2</sub>O<sub>3</sub>. Molybdenum was substitutionally incorporated into the In<sub>2</sub>O<sub>3</sub>

structure and resulted in an increase in the charge carrier concentration to  $4 \times 10^{20} \text{ cm}^{-3}$  with a concomitant increase in the charge carrier mobility to  $119 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ , without a decrease in the average transmittance in the visible/NIR region. In Mo:In<sub>2</sub>O<sub>3</sub>, as the dopant density increased, the charge carrier mobility increased also. Hybrid-DFT calculations showed the molybdenum states exist high up in the conduction band, but the hybridization of Mo states to the CBM was low, and thus the conduction band electrons do not get scattered off the dopant center in the way that is the case for Sn-doped In<sub>2</sub>O<sub>3</sub>. This case is analogous to that of La:BaSnO<sub>3</sub>,<sup>43</sup> where the La donor states also appear high in the conduction band, meaning that the CBM is unchanged relative to pure BaSnO<sub>3</sub>, which is most likely the source of the extremely high mobilities reported for single-crystal and thin films.<sup>43,65–67</sup> Thus through a combination of XPS, XAS, and DFT calculations, we have explained the oxidation state of Mo:In<sub>2</sub>O<sub>3</sub> and the nature of the high electron mobility observed in Mo:In<sub>2</sub>O<sub>3</sub>.

## ASSOCIATED CONTENT

### Supporting Information

Additional figures (PDF). This material is available free of charge via the Internet at <http://pubs.acs.org>.

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### Notes

The authors declare no competing financial interest.

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