

1 **Room temperature magnetically ordered polar corundum GaFeO₃ displaying**
2 **magnetoelectric coupling**

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20 **Abstract**

21 The polar corundum structure type offers a route to new room temperature multiferroic
22 materials, as the partial LiNbO₃-type cation ordering that breaks inversion symmetry may be
23 combined with long range magnetic ordering of high spin d^5 cations above room temperature
24 in the AFeO₃ system. We report the synthesis of a polar corundum GaFeO₃ by a high-pressure
25 high-temperature route and demonstrate that its polarity arises from partial LiNbO₃-type cation
26 ordering by complementary use of neutron, X-ray and electron diffraction methods. In-situ
27 neutron diffraction shows that the polar corundum forms directly from AlFeO₃-type GaFeO₃
28 under the synthesis conditions. The A³⁺/Fe³⁺ cations are shown to be more ordered in polar
29 corundum GaFeO₃ than in isostructural ScFeO₃. This is explained by DFT calculations that

1 indicate that the extent of ordering is dependent on the configurational entropy available to
2 each system at the very different synthesis temperatures required to form their corundum
3 structures. Polar corundum GaFeO_3 exhibits weak ferromagnetism at room temperature that
4 arises from its Fe_2O_3 -like magnetic ordering, which persists to a temperature of 408 K. We
5 demonstrate that the polarity and magnetisation are coupled in this system, with a measured
6 linear magnetoelectric coupling coefficient of 0.057 ps/m. Such coupling is a prerequisite for
7 potential applications of polar corundum materials in multiferroic/magnetoelectric devices.

8

9 **1. Introduction**

10 New low-energy information storage and processing architectures have been proposed which
11 rely on magnetoelectric and multiferroic materials¹⁻², but the development of such systems is
12 hampered by a paucity of suitable candidate materials, which must combine magnetic and polar
13 electrical order at (or close to) room temperature. This is challenging because the electronic
14 structure requirements for the two ground states are antagonistic in several respects *e.g.*,
15 classical routes to polar materials rely on the coordination environments of closed shell s^2 and
16 d^0 cations which are not consistent with magnetism³⁻⁵. The perovskite BiFeO_3 partially solves
17 this problem by combining ferroelectrically- and antiferromagnetically-ordered sublattices⁶⁻⁷.
18 Several new approaches centred on the ABO_3 perovskite family have emerged recently, such
19 as strain-generated ferromagnetism in epitaxial thin films⁸⁻⁹, magnetic percolation at
20 morphotropic phase boundary compositions in bulk ceramics¹⁰ and symmetry engineering¹¹ in
21 bulk¹² and thin film materials¹³. However, the identification of other materials families where
22 the two ground states may co-exist at ambient temperature is less developed. By using the
23 connection between the polar LiNbO_3 structure and perovskite, we identified polar derivatives
24 of corundum as a new class of ternary oxide AFeO_3 materials that support both magnetic order
25 (from a sufficiently high concentration of Fe^{3+} cations) and electrical order (enabled by cation
26 site ordering), which can be targeted by high pressure synthesis methods¹⁴. The polar corundum
27 ScFeO_3 , the first compound of this type, is ordered magnetically above room temperature and
28 the limited extent of long-range cation site order is sufficient to break inversion symmetry,
29 producing electrical polarity (more recently, LiNbO_3 -type polymorphs of $\text{Mn}_2\text{FeTaO}_6$ ¹⁵ and
30 $\text{Zn}_2\text{FeTaO}_6$ ¹⁶ have been reported with low magnetic ordering temperatures by a similar
31 synthetic approach, and potential ferroelectric switching mechanisms have been investigated
32 computationally¹⁷). The crystal chemistry of ScFeO_3 is complex as, in addition to the

1 competition between bixbyite and partially ordered corundum phases,¹⁴ higher synthesis
2 pressures stabilise a perovskite phase, from which a fully ordered LiNbO₃-type polymorph
3 (with a correspondingly enhanced spontaneous polarisation and Néel temperature) is recovered
4 on decompression¹⁸. This implies that the structural chemistry of analogous AFeO₃
5 compositions (where A is a trivalent cation capable of adopting octahedral coordination) could
6 offer polarity and magnetism if synthesised under appropriate conditions.

7 The ternary ferrite GaFeO₃ represents one such candidate for isolation of a polar corundum
8 phase. While at ambient pressure ScFeO₃ adopts the fluorite-derived bixbyite structure with
9 Sc³⁺ and Fe³⁺ coordinated in an edge-sharing network of distorted MO₆ octahedra¹⁹, ambient
10 pressure GaFeO₃ adopts the polar orthorhombic AlFeO₃ structure with edge-sharing chains of
11 (Ga, Fe)O₆ octahedra and vertex-linked GaO₄ tetrahedra, but only exhibits long-range magnetic
12 ordering and magnetoelectric coupling well below room temperature²⁰⁻²³. Like ScFeO₃ and
13 InFeO₃²⁴, its structural behaviour at high pressures and temperatures shows complex interplay
14 between corundum and perovskite structures: at ambient temperature, hydrostatic compression
15 to pressures above 40 GPa converts the structure directly to an orthorhombic perovskite, which
16 in turn transforms on decompression to 25 GPa to a corundum-type phase which is retained
17 down to ambient pressure²⁵. Corundum-type GaFeO₃ can also be obtained directly by annealing
18 at a sufficiently high temperature and pressure²⁶ and by analogy with ScFeO₃ it is possible that
19 a polar variant of this structure will be accessible in this part of the phase diagram. We have
20 targeted and isolated such a polar corundum GaFeO₃ phase, demonstrating that a family of
21 materials adopt this structure. Polar corundum GaFeO₃ exhibits weak ferromagnetism above
22 room temperature, and the extent of the cation site order is enhanced with respect to that
23 observed in ScFeO₃, allowing the measurement of linear magnetoelectric coupling consistent
24 with the polar *R3c* space symmetry and the observed α -Fe₂O₃ – like magnetic order.

25

26 **2. Experimental Details**

27 **Synthesis:** Initially, the ambient pressure phase of GaFeO₃ was prepared from stoichiometric
28 mixtures of Ga₂O₃ (99.999%) and Fe₂O₃ (99.998%) reacted at 900 °C for 12 hours, 1300 °C
29 for 24 hours followed by 1400 °C for 2 hours in an alumina crucible in air. This precursor phase
30 was then annealed under flowing oxygen at 1300 °C for 10 hours, in order to maximise the
31 resistivity of the subsequent high pressure product. The GaFeO₃ starting materials were then
32 heated to 150, 500, 700, 900, 1100, 1300 and 1500 °C, respectively, for 10 minutes at 6 GPa

1 in a Pt-lined alumina crucible encapsulated within a graphite furnace in a Walker-type multi-
2 anvil press. The samples were then cooled to room temperature and the pressure released. The
3 high pressure phase forming at 900 °C was used for structural, electric and magnetic studies.

4 **Powder X-ray diffraction:** Phase identification was performed using a PANalytical X'Pert
5 Pro diffractometer in Bragg-Brentano geometry with monochromated Co K_{α1} radiation ($\lambda =$
6 1.78896 \AA). Synchrotron XRD data (SXRD) were collected from the I11 powder
7 diffractometer (Diamond Light Source, UK). The sample was loaded inside a 0.1 mm quartz
8 capillary and data were collected using an incident wavelength $\lambda = 0.827127(1) \text{ \AA}$ over a 2θ
9 range $2 - 150^\circ$, using the high resolution MAC detectors. Anomalous scattering data were
10 collected on beam line I11 from a sample loaded on to the external surface of a 0.3 mm
11 borosilicate capillary. A monochromator scan was used to measure the Ga K edge fluorescence
12 spectrum and an energy of 10.359 keV ($\lambda = 1.196901(5) \text{ \AA}$) was selected for the anomalous
13 scattering data set using the high resolution MAC detectors. A corresponding non-anomalous
14 data set was then collected from the same capillary at $\lambda = 0.826185(5) \text{ \AA}$.

15 **Powder neutron diffraction:** Time-of-flight neutron powder diffraction (NPD) data were
16 collected at ambient temperature and pressure on the POLARIS diffractometer at the ISIS
17 facility, Rutherford Appleton Laboratory (UK). The sample was contained in a quartz capillary
18 of diameter 1.5 mm, filled to a height of 40 mm. The data analysis was performed by Rietveld
19 refinement using Topas Academic (Version 5).

20 **In-situ powder neutron diffraction:** High-pressure high-temperature data were collected on
21 the medium-resolution high-flux PEARL diffractometer (ISIS, UK) using a Paris-Edinburgh
22 (PE) press²⁷. The sample was pelletised and placed in a high-pressure furnace assembly²⁸. The
23 furnace assembly was placed in between WC anvils in a V4 variant PE press dedicated to high
24 temperature pressure measurements. The sample pressure was determined by the equation of
25 state (EoS) of platinum²⁹. The temperature was determined by the resonance technique from
26 the Hf foils included in the sample volume³⁰. Time of flight data were collected using the 90
27 degree detector bank over a d-spacing range of 0.5-4 \AA and corrected for anvil attenuation
28 using in-house routines²⁷. The hydraulic load of the press was gradually increased until the
29 desired sample pressure was achieved prior to heating. The data analysis was performed by
30 Rietveld refinement using Topas Academic (Version 5).

31 **SQUID Magnetometry:** Magnetic measurements were carried out on powder samples using a
32 commercial superconducting quantum interference device (SQUID) magnetometer MPMS XL
33 – 7 and MPMS3 (Quantum Design, USA). Magnetization vs. temperature data were recorded
34 from 5 K to 900 K in the following modes: ZFC (zero-field cooling), FC (field cooling) and

1 TRM (thermoremanent magnetization). The magnetic field-dependent magnetization was also
2 measured at 10, 200, 400 and 420 K between -9 kOe and 9 kOe.

3 **Magnetoelectric coupling:** For magnetoelectric (ME) measurements, the polar corundum
4 sample was polished to a 5 micron finish using SiC paper in a semi-automatic polishing
5 machine. Ohmic contacts were made via sputtering Pt. ME measurements were carried out on
6 a modified SQUID magnetometer³¹. Prior to the measurements the sample was poled in the
7 following sequence: slowly cooled (1 - 2 K/min) from 350 K to 130 K in a 20 kOe magnetic
8 field and zero electric field (short circuit). At 100 K, an electric field of 350 – 400 kV/m was
9 applied while cooling down in the same magnetic field to the measurement temperature at 1
10 K/min. After poling, electric and magnetic fields were switched off and electrodes were short
11 circuited for 15 minutes.

12 **Dielectric constant** Dielectric properties were measured using an Agilent 4980 precision LCR
13 meter for frequencies of 20 Hz to 2 MHz in the temperature range of 30–500 °C. A ramp rate
14 of 1 °C min⁻¹ was used. The sample with sputter coated Pt electrodes on both sides was loaded
15 in a home-made sample holder and data were collected using the LABVIEW program.

16 **Differential Scanning Calorimetry (DSC):** Heat flow was measured from a powder sample
17 in an aluminium pan between room temperature to 500 °C by the modulated DSC technique
18 using a DSC Q2000 instrument (TA Instruments).

19 **In-situ resistance:** Two-probe dc electrical resistance measurements as a function of
20 temperature at 6 GPa were carried out using Keithley 220 programmable current source and
21 Keithley 2182 Nanovoltmeter. The GaFeO₃ powder was loaded into the alumina crucible and
22 Pt plates were employed on both the top and bottom of the crucible as the electrodes.

23 **ICP-OES measurements:** Powder samples of GaFeO₃ (approximately 50 mg) were dissolved
24 in 10 cm³ HF-HCl mixture (UniSolv Acid Dissolution Reagent 1, Inorganic Ventures) with 10
25 drops of concentrated HNO₃. The solution was then neutralised with 50 cm³ of triethanolamine-
26 triethylenetetramine solution (UNS-1 solution, Inorganic Ventures) and diluted to
27 approximately 20 ppm. The same protocol was used to prepare a standard solution from a
28 stoichiometric mixture of Ga₂O₃ and Fe₂O₃. Measurements were collected on a Spectro Ciros
29 Vision ICP-OES instrument.

30 **TEM-EDX:** EDX measurements were performed on a Jeol 2000FX using an EDAX EDX
31 detector. Sample powder was dispersed in 500µl of ethanol and a drop of the suspension was
32 dropped on a carbon coated TEM copper grid. EDX spectra were collected for several minutes
33 in order to obtain a suitable signal to noise ratio. Compositions were calculated from the mean
34 of 25 particles.

1 **Convergent beam electron diffraction (CBED):** Specimens were prepared using a FEI
2 Helios 600i focussed (Ga) ion beam instrument. Thin lamellae were sectioned and mounted on
3 Cu grids using the lift out technique. Primary milling was performed using an acceleration
4 voltage of 30kV, final cleaning passes were applied to specimen surfaces using a low energy
5 (5kV) polish. CBED experiments were performed in JEOL 2000FX microscope operated at
6 200keV.

7 **SAED and HAADF-STEM:** TEM specimens were prepared by grinding the powder sample
8 under ethanol and depositing several drops of the dispersion onto holey carbon grids. The
9 selected area electron diffraction (SAED) patterns were recorded using a Tecnai G2
10 microscope operated at 200 kV. The Fe and Ga distribution in the structure was investigated
11 using high angle annular dark field scanning TEM (HAADF-STEM) imaging. The experiment
12 was conducted on a probe aberration-corrected Titan 80-300 microscope operated at 300 kV.
13 Theoretical HAADF-STEM images have been calculated using the QSTEM 2.20 software.

14 **Mossbauer spectroscopy:** Mössbauer spectroscopy was performed in absorption, at room
15 temperature, using a WissEl (MA-260) electromagnetic Doppler drive system, a $^{57}\text{Co}(\text{Rh})$
16 gamma source, of actual activity of ~ 40 mCi and Xe-gas Reuter-Stokes proportional counter.
17 Canberra amplification, discrimination and scaling electronics were used to acquire sample and
18 α -Fe calibration spectra of width of 512 channels, to a level of approximately 10^7 counts per
19 channel. Samples were diluted with sucrose (icing sugar) for measurements at an approximate
20 ratio of 0.2, in order to prevent excessive line-shape distortion and non-resonant absorption.
21 Custom folding, absorber geometry modelling and non-linear least squares regression routines
22 were used for the extraction of the spectroscopic parameters and their errors. Isomer shifts are
23 referred to the source.

24 **Computational:** All calculations were performed under periodic boundary conditions, using
25 the CP2K³²⁻³³ code which employs a mixed Gaussian/plane-wave basis set. We employed
26 double- ζ polarization quality Gaussian basis sets³⁴ and a 600 Ry plane-wave cutoff for the
27 auxiliary grid, in conjunction with Goedecker–Teter–Hutter pseudopotentials³⁵⁻³⁶. Total
28 energy calculations and structural optimizations, including both atomic coordinates and cell
29 parameters, were performed at the hybrid density functional theory (DFT) level using the PBE0
30 exchange and correlation functional³⁷⁻³⁸, which has 25% Hartree-Fock exchange (HFX). The
31 HFX calculations were significantly accelerated by using the auxiliary density matrix method
32 (ADMM)³⁹ and a truncated potential⁴⁰, with which the HFX energy becomes zero beyond a
33 pre-defined real-space cutoff radius. For production quality calculations we have used the
34 cpFIT3 auxiliary basis sets and a cutoff radius of 4 Å, a convergence threshold of 5.0×10^{-6}

1 Ha for the self-consistent field cycle, and structural optimizations were considered to have
2 converged when the maximum force on all atoms falls below 4.5×10^{-4} Ha Bohr⁻¹.
3 Calculations were performed with the Γ -point approximation using a $2 \times 2 \times 1$ multiplication
4 of the hexagonal primitive cell consisting of 120 atoms. Additional calculations in a $3 \times 3 \times 1$
5 supercell (270 atoms) show that the relative energy between FM and AFM magnetic
6 configurations in the LiNbO₃ cation order converged to within 5 meV/f.u. in the $2 \times 2 \times 1$
7 supercell. A comprehensive and systematic configurational and compositional search on
8 ScFeO₃ and GaFeO₃ in the corundum structure was performed as part of this study (described
9 fully in the Supporting Information), in which the LiNbO₃ structure was identified as the
10 ground state of corundum-type ScFeO₃. The ground state of corundum-type GaFeO₃ was found
11 to be phase separated layers of Fe₂O₃ and Ga₂O₃, hence discussion of phase stability refers to
12 LiNbO₃ and “phase separated” as the ground state references for ScFeO₃ and GaFeO₃
13 respectively. Additional details of the computational study, including defect formation
14 energies, configurational search, and estimation of configurational entropies, are provided in
15 the Supporting Information (including Figures S1 – S3, and Tables S1 – S2).

16

17 **3. Results**

18

19 **3.1. Isolation and stability of corundum GaFeO₃**

20 Extensive investigation of (T, P) synthesis conditions in the multianvil cell revealed a 700-
21 900°C temperature range at 6 GPa that afforded a diffraction pattern that could be indexed
22 solely with a corundum unit cell after decompression and cooling to room temperature (Figure
23 1a). The composition was confirmed to be stoichiometric GaFeO₃ by ICP-OES measurements
24 (Table S3), with a high level of compositional homogeneity confirmed by TEM-EDX (Figure
25 S4). Reaction at higher temperatures produces Fe₃O₄ as a secondary phase in increasing
26 quantity (2 wt.% 1100°C, 19 wt.% 1500°C) while 500 °C affords partial conversion of ambient
27 pressure GaFeO₃ to the corundum structure. In-situ neutron diffraction data collected at 4.7
28 GPa confirms that the ambient pressure orthorhombic GaFeO₃ is converted directly to a
29 corundum-type phase (Figure 1b, c). Higher resolution information on the transformation
30 temperature is provided by in-situ measurement of dc resistance under the synthesis conditions:
31 by cycling a sample to increasing maximum temperatures, its resistance was found to decrease
32 irreversibly during cycles to 400 and 550 °C signifying the onset of the phase transformation,
33 before returning to near-reversible behaviour for cycles to 650 and 800 °C, consistent with

1 completed formation of the corundum phase (Figure 1d). A second sample was cycled four
2 times between $\sim 25 - 900$ °C and showed an irreversible decrease in resistance on the first cycle,
3 which coincides with the resistivity of subsequent cycles at 550 °C (Figure S5), implying that
4 complete conversion to the corundum is achieved at this temperature. This is consistent with
5 both the ex-situ PXRD where the pattern is already dominated by the corundum phase at 500
6 °C, and the in-situ NPD where the refined AlFeO_3 -phase content reaches a minimum plateau
7 at 575 °C.

8 To better understand the isolation of polar corundum GaFeO_3 under high pressure reaction
9 conditions, we calculated the enthalpies of different polymorphs of GaFeO_3 at different
10 pressures up to 40 GPa. We considered the ambient pressure AlFeO_3 -type structure, an
11 orthorhombic perovskite structure, the LiNbO_3 and ilmenite ordered corundum structures, and
12 the ground state corundum configuration produced by our configurational search (in which Ga
13 and Fe form a structure with distinct [001] blocks at either end of the corundum cell, see
14 Supporting Information and Figure S1). Their enthalpies were compared with those of the
15 binary oxides using the ambient pressure forms $\alpha\text{-Fe}_2\text{O}_3$ and $\beta\text{-Ga}_2\text{O}_3$ as the references. Finally,
16 an estimate of the configurational entropies available to the AlFeO_3 - and LiNbO_3 -type
17 structures was calculated at 1200 K (see Supplementary Text). The calculated entropies as a
18 function of pressure are plotted in Figure 2a, with the estimated entropic contribution to the
19 total energy at 1200 K overlaid for these two structure types to illustrate the estimated extent
20 of entropic stabilization. The equivalent calculations for the same polymorphs of ScFeO_3 , using
21 $\alpha\text{-Fe}_2\text{O}_3$ and bixbyite-type Sc_2O_3 as the references, are shown in Figure 2b.

22 For GaFeO_3 , the ambient pressure AlFeO_3 structure is the most stable ternary phase at 0 GPa,
23 and is stable relative to the binaries when configurational entropy of 98.8 meV/f.u. at 1200 K
24 is considered. At this pressure, the LiNbO_3 structure is unstable with respect to its binary
25 constituents by 159 meV/f.u at 0 K. With increasing pressure, the AlFeO_3 structure is
26 progressively destabilised, and the corundum-type structures become the most stable beyond
27 ~ 3 GPa. Among the corundum-type structures, the LiNbO_3 cation ordering is found to be more
28 stable than the ilmenite ordering at all pressures. At ~ 30 GPa the perovskite structure becomes
29 more stable than the LiNbO_3 structure, which is in good agreement with experimental work²⁵.
30 In ScFeO_3 , the LiNbO_3 structure is the most stable ternary phase at 0 GPa but is less stable than
31 the binary mixture by 128 meV/f.u; the orthorhombic perovskite phase is stabilised more
32 rapidly with pressure and becomes the most enthalpically stable phase at ~ 7 GPa.

1 These results show that configurational entropy due to disorder of Ga and Fe cations in the
2 AlFeO_3 and corundum lattices at the synthesis temperatures plays a critical role in the
3 stabilisation of the ternary phases. This is consistent with our configurational search of
4 corundum-type GaFeO_3 (see Figure 3a), where a total of 151 configurations, including the fully
5 ordered LiNbO_3 structure, are found within 50 meV/f.u. ($\sim 0.5 kT$ at the synthesis temperature
6 of 1200 K) of the lowest energy configuration: these may correspond to states that are
7 accessible under the synthesis temperature. This contrasts with ScFeO_3 , which has only 5
8 configurations within 50 meV/f.u. of the fully ordered LiNbO_3 ground state (Figure 3b),
9 indicating that a higher temperature is required to entropically stabilise the corundum structure
10 of ScFeO_3 by accessing a greater number of configurations.

11

12 **3.2. Structural analysis**

13 The synchrotron powder X-ray diffraction (SXRD) patterns of GaFeO_3 synthesised at high
14 pressure could be indexed to an R -centered hexagonal unit cell with lattice parameters $a =$
15 $5.01936(4) \text{ \AA}$, $c = 13.5903(1) \text{ \AA}$, as shown in Figure 4a, which is consistent with the corundum
16 structure adopted by $\alpha\text{-Fe}_2\text{O}_3$ ⁴¹⁻⁴². The observed reflection conditions (h - $h0$ l: $h+l = 3n$, $l = 2n$),
17 also observed in selected area electron diffraction (SAED) patterns (Figure 4c), are consistent
18 with $R3c$ and $R\bar{3}c$ space groups which correspond to the polar LiNbO_3 and non-polar (fully
19 disordered) corundum structures respectively. These systematic absences preclude the
20 possibility of an ilmenite structure type with $R\bar{3}$ space symmetry. Regarding the possible
21 acentric $R3c$ and centrosymmetric $R\bar{3}c$ structural models of GaFeO_3 , the very similar X-ray
22 scattering factors of Fe^{3+} and Ga^{3+} preclude unambiguous space group assignment from
23 Rietveld refinement against PXRD data alone. We addressed this problem in two parts: firstly,
24 by using convergent beam electron diffraction (CBED) to determine the point group of the
25 GaFeO_3 corundum; and secondly by employing powder neutron diffraction and anomalous X-
26 ray scattering to determine the extent of the cation ordering.

27 The whole pattern symmetry of the $[5\bar{5}1]$ zone from CBED (Figure 4b) displays only a single
28 m symmetry element. Considering only trigonal crystal systems this permits the assignment of
29 the $3m$ point group⁴³ and along with the observed reflection conditions from PXRD data
30 indicates that the high pressure phase of GaFeO_3 crystallises in the non-centrosymmetric $R3c$
31 space group. To confirm the assignment of the $R3c$ space group and investigate the degree of
32 cation order in GaFeO_3 , neutron powder diffraction (NPD) analysis of two samples synthesised
33 by the same protocol utilized the modest contrast in the neutron scattering lengths of Fe (9.45

1 fm) and Ga (7.288 fm). The appearance of Bragg peaks that were not present in the SXRD
2 pattern, including two intense reflections at 4.14 and 4.54 Å, confirmed the presence of long
3 range magnetic order at room temperature. The magnetic structure was determined by
4 representational analysis using the SARAh package⁴⁴ and found to be a $k = 0$ G-type
5 antiferromagnetic arrangement analogous to the high temperature antiferromagnetic structure
6 of α -Fe₂O₃⁴⁵ with spins aligned parallel to the a axis. Structural models in $R3c$ (LiNbO₃) and
7 $R\bar{3}c$ (corundum) were refined against four Polaris data banks simultaneously, with the magnetic
8 structure modelled in a $P1$ cell. In the disordered corundum ($R\bar{3}c$) refinement, the magnitudes
9 of the magnetic moments were constrained to a single refined value to reflect the statistical
10 distribution of Fe³⁺ cations. In the cation-ordered model ($R3c$), the occupancies of Ga³⁺ and
11 Fe³⁺ on each site in the nuclear phase were refined with a constraint on the total composition,
12 and the magnetic phases were modelled with two independently refined moments, whose
13 positions in the $P1$ cell corresponded to the LiNbO₃-type cation ordering. In addition to site
14 occupancy refinement in the LiNbO₃ model, atomic coordinates and isotropic thermal
15 displacement parameters (B_{iso}) were refined with B_{iso} constrained to be equal for the Fe/Ga
16 sites.

17 For both samples the best goodness of fit was obtained from refinement in the $R3c$ space group,
18 with $R\bar{3}c$ (disordered corundum) giving the higher χ^2 (see Tables S4 and S5). Inspection of the
19 refined $R3c$ model revealed that the refined cation occupancies from the nuclear scattering in
20 $R3c$ resulted in compositions of [Ga_{0.68(2)}Fe_{0.32(2)}][Ga_{0.32(2)}Fe_{0.68(2)}]O₃ (36(2) % ordered, defined
21 by the difference in site occupancy) and [Ga_{0.62(3)}Fe_{0.38(3)}][Ga_{0.38(3)}Fe_{0.62(3)}]O₃ (24(3)% ordered)
22 for the two samples, which is consistent with the relative magnitudes of the ordered spins on
23 each site in the magnetic structure: the ordered moment at the Fe-rich site in sample 1 refined
24 to 2.15(2) μ_B , whilst that of the Fe-poor site refined to 1.03(3) μ_B . Assuming that individual Fe
25 have the same moment at each site, then the refined (average) moments are due to different
26 populations of Fe at each site, which yields [Ga_{0.68(1)}Fe_{0.32(1)}][Ga_{0.32(1)}Fe_{0.68(1)}]O₃, and the
27 equivalent calculation for sample 2 yields [Ga_{0.65(1)}Fe_{0.35(1)}][Ga_{0.35(1)}Fe_{0.65(1)}]O₃. The Rietveld
28 fits are shown together with the refined $R3c$ model in Figure 5. The consistency between the
29 extent of cation ordering obtained directly from the nuclear scattering, and the extent of
30 ordering obtained independently from the magnetic scattering, in addition to the superior
31 goodness of fit, confirms the assignment of polar $R3c$ symmetry. The polarization of GaFeO₃
32 was calculated as 6.9 $\mu\text{C}\cdot\text{cm}^{-2}$ from a formal point charge model, using the program PSEUDO⁴⁶
33 with the refined atomic coordinates of sample 1.

1 Anomalous scattering synchrotron X-ray diffraction at the Ga K edge provides an alternative
2 probe of the extent of cation order. The *R3c* model was refined simultaneously against two
3 histograms, collected at ambient temperature at resonant (10.359 keV) and non-resonant
4 (15.119 keV) energies from sample 1. The background was fitted by refinement of a
5 Chebyshev polynomial function, and peak profiles were modelled by a Pearson VII function
6 with a refined axial divergence correction. Lattice parameters, atomic coordinates and isotropic
7 thermal displacement parameters were refined independently for each site, and a Suortti surface
8 roughness (absorption) correction was refined for each histogram. Initially a series of $[\text{Ga}_x\text{Fe}_{1-x}]$
9 $[\text{Ga}_{1-x}\text{Fe}_x]\text{O}_3$ models with the extent of cation ordering (x) varied systematically between $0 \leq$
10 $x \leq 1$ were refined, and the resulting plot of χ^2 vs x (Figure S6) showed two shallow minima
11 centred approximately at $x = 0.4$ and $x = 0.6$, consistent with the partial cation ordering
12 observed by NPD. By allowing x to refine freely, a composition
13 $[\text{Ga}_{0.596(4)}\text{Fe}_{0.404(4)}][\text{Ga}_{0.404(4)}\text{Fe}_{0.596(4)}]\text{O}_3$, which is 19.2(6)% ordered, was obtained which is
14 within four standard deviations of the NPD value (furthermore, the shallow minima in χ^2 vs x
15 indicate that the reported least squares errors on x from SXR D are underestimated). Both the
16 NPD and SXR D results are also consistent with the computational screening of configurational
17 entropy; the average cation order in the 2331 configurations examined and displayed in Figure
18 3, weighted by their relative population at 900 °C, yields a value of $[\text{Ga}_{0.61}\text{Fe}_{0.39}][\text{Ga}_{0.39-}$
19 $\text{Fe}_{0.61}]\text{O}_3$.

20 HAADF-STEM was used as a local probe to image the cation ordering directly. The two
21 crystallographic positions jointly occupied by Fe and Ga form separate atomic columns in the
22 structure as viewed along the $[24\bar{6}1]$ ($= \langle 100 \rangle_p$) direction (Figure S7). In HAADF-STEM, the
23 observed intensity is proportional to the composition of the atomic columns and scales
24 approximately as $Z^{1.6-1.9}$ (where Z is the average atomic number of the projected columns).
25 Because of a very small difference between the average Z of the Fe-rich and Ga-rich atomic
26 columns ($Z = 27.6$ and 29.4 , respectively), the associated difference in brightness is expected
27 to be subtle (see the calculated intensity profile in Figure 6c). Nevertheless, the intensity
28 profiles taken from the experimental $[24\bar{6}1]$ HAADF-STEM image (Figure 6a, b) show
29 systematic intensity differences reminiscent of that observed on the profile from the calculated
30 image (Figure 6c). All of these structural analyses confirm the *R3c* space group with partial
31 Ga/Fe order in the polar corundum structure.

32

3.3. Magnetic order and magnetoelectric coupling

Mössbauer spectroscopy of polar corundum GaFeO₃ at ambient temperature and pressure confirms the long range magnetic order demonstrated at room temperature by neutron diffraction (Figure 7d, with fitted parameters shown in Table 3). The absorption pattern is clearly decomposed into a combination of two magnetically-ordered sites, with average hyperfine fields of 39.48 T and 33.09 T, respectively (the larger of the two being close to that of Goethite⁴⁷ with its transition temperature of ~400 K⁴⁸) which account for 91.09(2) % of the fitted area, with the remainder assigned to one asymmetric paramagnetic doublet accounting for 8.91(2) % of the fitted area, which is a dynamic line shape resulting from the proximity of the Néel temperature. The two main sites exhibit significant static hyperfine field distributions of width of 0.2 – 0.3 T. The fitted isomer shift (IS) of 0.25 mm/s and quadrupole splitting of 0.19 mm/s are consistent with Fe³⁺, but the IS is smaller than expected for a typical octahedral coordination in an oxide, which may be due to the high degree of static disorder in the system. Isomer shifts of <0.25 mm/s have been reported under applied hydrostatic pressure for a corundum GaFeO₃ produced by transformation from the metastable perovskite (and thus likely to be highly ordered)²⁵, demonstrating a high degree of sensitivity of IS to local coordination environment in this system.

Figure 7a shows the magnetisation of polar corundum GaFeO₃ measured in an applied magnetic field of 1000 Oe in zero field cooled (ZFC), field cooled (FC) and thermoremanent magnetisation (TRM) from 300 K to 500 K. ZFC/FC divergence appears at 408 K together with the onset of TRM. The M(H) isotherms in Figure 7b are consistent with this magnetic ordering temperature of 408 K. The linear isotherm at 420K shows that the sample is paramagnetic, with hysteresis observed at and below 400K, consistent with weak ferromagnetism occurring simultaneously with the antiferromagnetic order. ZFC, FC and TRM magnetisation data between 5 and 350 K (Figure S8), show that no magnetic transition occurs below 408K. The remanent magnetisation was 0.012 μ_B/f.u. at 10 K (Figure 7b).

In order to minimise spurious signals caused by leakage currents, magnetoelectric measurements were carried out at 10 K on the polar corundum GaFeO₃ sample poled both electrically and magnetically (the resistivity at 10 K, measured in-situ, was 2.38 x 10¹² Ω.m). The ME susceptibility (α), measured as the slope of the induced ac magnetization (*M_{ac}*) versus the applied ac electric field amplitude (*E_{ac}*) is 0.057 ps/m. (Figure 7c). The observation of linear magnetoelectric coupling is consistent with the symmetry of the magnetic structure: above the

1 Morin transition,⁴⁵ α -Fe₂O₃ adopts $2/m$ magnetic point symmetry (which is centrosymmetric,
2 permitting weak ferromagnetism but not linear magnetoelectric coupling⁴⁹), but the cation
3 ordering in polar corundum GaFeO₃ eliminates the inversion centre, thus lowering the magnetic
4 point symmetry to m ,⁵⁰ which permits both weak ferromagnetism and linear magnetoelectric
5 coupling⁴⁹. The observed magnitude of α is similar to that observed in other Fe-based polar
6 magnetoelectrics that are ordered magnetically above room temperature.^{10, 12, 51} Attempts to
7 measure electrical polarization loops were hampered by the high dielectric loss at room
8 temperature, whilst measurements at 100 K were possible at applied fields of up to 120 kVcm⁻¹
9 but did not achieve ferroelectric switching.

12 3.4. Thermal stability

13 To test the thermal stability and decomposition behaviour of polar corundum GaFeO₃ at
14 ambient pressure, the as-made samples were annealed at different temperatures between 300 –
15 1000 °C in air. Ex-situ PXRD patterns of the post-annealed samples showed that the
16 orthorhombic ambient pressure phase is recovered after annealing at 1000 °C, but the
17 corundum unit cell is retained after annealing at 300 – 800 °C with no apparent decomposition
18 (Figure S9). However, DSC (Figure 9) and in-situ dielectric measurements (Figure 10)
19 collected on heating from 25 – 500 °C show an endothermic peak, and a corresponding peak
20 in the dielectric constant, which is frequency-independent (Figure S10) and centred at
21 approximately 200 °C. The feature is strongly pronounced during the first heating cycle and
22 absent in subsequent cycles, which indicates the occurrence of an irreversible phase transition.
23 To investigate whether this is associated with a loss of polarity in the sample, CBED images,
24 magnetisation and magnetoelectric coupling data were collected on annealed samples.

25 Figure 7c shows the ME susceptibility α decreases from 0.057 ps/m for as-made polar
26 corundum GaFeO₃ to 0.003 ps/m for the sample annealed at 380 °C: for this sample, the
27 induced magnetic moment is below the detection limit of 10⁻⁹ emu. Close inspection of the
28 CBED whole pattern symmetry for the $[\bar{1}11]$ zone axis (Figure S11) reveals the sample to have
29 retained $3m$ point symmetry, which implies that the sample has retained some residual polarity.
30 Taken together with the magnetoelectric measurements, this implies that the polarity of the
31 material (via the cation ordering) is diminished, but not eliminated entirely, by annealing polar
32 corundum GaFeO₃ at this temperature. The weak ferromagnetism, which arises from the α -

1 Fe₂O₃-type magnetic structure, is also retained after thermal treatment (Figure S12). This is
2 consistent with the $2/m$ magnetic point symmetry of α -Fe₂O₃ above the Morin transition⁴⁵: the
3 **loss of** cation ordering in polar corundum GaFeO₃ **would restore** the inversion centre, thus
4 **raising** the magnetic point symmetry **back to $2/m$** (which is centrosymmetric, permitting weak
5 ferromagnetism but not linear magnetoelectric coupling⁴⁹).

6 4. Discussion

7 Under the high temperature, high pressure conditions applied in this study, a corundum phase
8 of GaFeO₃ forms directly from the ambient pressure phase, in contrast to the sequence of phases
9 observed on application of pressure at room temperature where a corundum phase is accessed
10 via a non-quenchable perovskite phase²⁵. The fact that the phase does not form by
11 transformation from the high pressure perovskite phase^{18, 25} means that the extent of Ga/Fe
12 ordering is limited, producing the polar corundum structure rather than the fully ordered
13 LiNbO₃ structure. NPD and X-ray anomalous scattering experiments demonstrate a greater
14 degree of ordering in GaFeO₃ than in the isostructural ScFeO₃. Our computational results imply
15 that GaFeO₃ should have a greater tendency towards cation disorder than ScFeO₃ at a given
16 synthesis temperature, as demonstrated by the higher number of accessible cation
17 configurations in GaFeO₃ (Figure 3). This originates from the small overall energy cost of
18 Ga/Fe site swaps in GaFeO₃, while only the antisite Sc/Fe defect within face-shared dimers is
19 energetically possible in ScFeO₃. While the enthalpy of the polar corundum phase of both
20 GaFeO₃ and ScFeO₃ is unstable relative to the binary oxides, the higher entropic content of
21 GaFeO₃ (provided by the large number of thermally accessible cation configurations in the
22 corundum cell at the synthesis temperature) means that its polar corundum phase is stabilised
23 at lower temperature than that of ScFeO₃. Experimentally, this results in polar corundum
24 GaFeO₃ being stabilized at 900 °C, while polar corundum ScFeO₃ must be synthesized at a
25 much higher temperature of 1400 °C. The effect of the different synthesis temperatures of the
26 two materials is expected to have an impact on the extent of cation ordering. From our previous
27 Monte Carlo simulation of ScFeO₃¹⁴, it was clear that between 1300 and 1450 K, ScFeO₃
28 transformed from a mainly ordered to a mainly disordered structure: it is also clear that ScFeO₃
29 is calculated to be much more ordered than GaFeO₃ at 1200 K, with a site occupancy of ~0.9.
30 This indicates that the experimentally observed cation disorder in polar corundum ScFeO₃ is
31 driven by the enhanced configurational entropy at the higher synthesis temperature. In GaFeO₃,
32 the low synthesis temperature of 900 °C provides sufficient configurational entropy to stabilise
33 the polar corundum, but it is insufficient to disorder the material to the same extent as seen for

1 ScFeO₃ synthesised at 1400 °C, and consequently produces more ordered compounds. We note
2 the creation of anti-site defects in LiNbO₃-type GaFeO₃ (*e.g.* by swapping cations in adjacent
3 face-sharing MO₆ octahedra, as described in Supporting Information) is less energetically
4 demanding than in LiNbO₃-type ScFeO₃, see Table S2, and the anti-site defects may be partly
5 responsible for the cation disorder in polar corundum GaFeO₃. It is possible that another source
6 of disorder could originate from the precursor of corundum GaFeO₃, *i.e.* the ambient pressure
7 AlFeO₃-type, in which extent of cation ordering is dependent on the synthesis conditions⁵² and
8 predicted from our simulation based on small energy costs of creating anti-site defects (see
9 Table S6 in the Supporting Information). This implies that a more ordered polar corundum
10 GaFeO₃ may be obtained from a highly ordered precursor, *e.g.* the fully ordered perovskite, as
11 observed experimentally in ScFeO₃¹⁸.

12 In most respects the refined crystal structure of GaFeO₃ is very similar to that of ScFeO₃. The
13 unit cell volume of GaFeO₃ is approximately 10 % smaller than that of ScFeO₃ on account of
14 the smaller ionic radius of Ga³⁺ (0.62 Å) versus Sc³⁺ (0.745 Å). This is an isotropic contraction
15 driven by the smaller average size of the MO₆ coordination octahedra, as indicated by the
16 similar *c/a* ratios in the two compounds (2.71 and 2.69, respectively). The unit cell dimensions
17 of GaFeO₃ are very close to those of α-Fe₂O₃⁴¹⁻⁴² and are consistent with those reported from
18 corundum structured GaFeO₃ in a recent in-situ high pressure study²⁵. The refined metal-oxide
19 distances, illustrated in Figure 5, lie in the range 1.93 – 2.13 Å, and the refined volume of the
20 Ga-rich MO₆ polyhedra (10.49 Å³) are slightly smaller than those of the Fe-rich polyhedra
21 (10.64 Å³), consistent with the relative ionic radii. As in the binary corundums and ScFeO₃,
22 the cations are displaced from the centres of the face-sharing MO₆ octahedra by electrostatic
23 repulsion.

24 Polar corundum GaFeO₃ exhibits weak ferromagnetism with an ordering temperature of 408
25 K; this is approximately 50 K higher than the ordering temperature observed in ScFeO₃¹⁴,
26 which may be due to its enhanced cation ordering. The remanent magnetisation of GaFeO₃
27 (0.012 μ_B / f.u.) is comparable to that observed in ScFeO₃ (0.0106 μ_B / f.u.)¹⁴. The combination
28 of weak ferromagnetism and absence of inversion symmetry permits magnetoelectric coupling
29 in GaFeO₃. The observed linear magnetoelectric susceptibility (α) of 0.057 ps m⁻¹ is small in
30 comparison to other Fe-based polar weak ferromagnetic ceramics^{10,51}, but the fact that the room
31 temperature structure is identical to the structure at the measurement temperature (10 K)
32 implies that, given definition of a suitable processing protocol, magnetoelectric coupling may
33 be attainable under ambient conditions in this compound. The magnitude of this coupling falls

1 below a detectable value when the sample is heated to 380 °C at ambient pressure. DSC and
2 dielectric measurements suggest that this is due to an irreversible phase transition, CBED
3 patterns however indicate that $3m$ point symmetry is still present in the sample. This indicates
4 that the polarity of the sample (driven by the cation ordering that defines the polar corundum
5 structure type) is degraded sufficiently to weaken the ME response below the detection limit,
6 but is not entirely eliminated by annealing under these conditions. Ultimately, the ambient
7 pressure phase is recovered by annealing at a sufficiently high temperature.

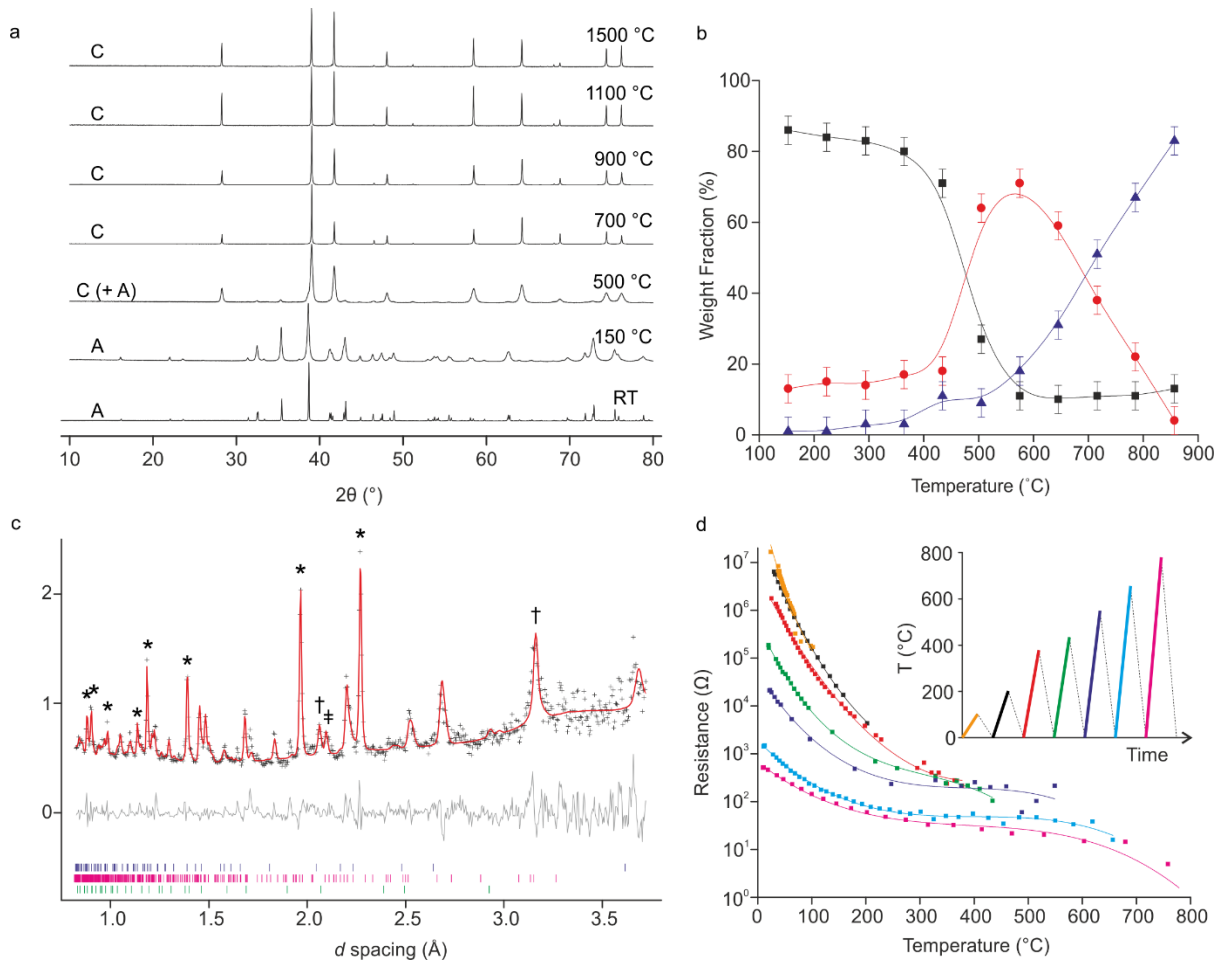
8 **5. Conclusions**

9 GaFeO₃ is the second member of the polar corundum family, and the first to display ME
10 coupling. The enhanced cation site order in GaFeO₃ over ScFeO₃ confirms the distinction of
11 this family both from non-polar corundum and from fully LiNbO₃-ordered derivatives: the less
12 extreme synthesis conditions required to access polar corundum indicate that a broad family of
13 materials should be accessible, for example through multiple cation decoration of corundum.

14 The magnetoelectric coupling shows that the engineered co-existence of magnetisation and
15 polarisation in new structural families is a route to coupling these degrees of freedom – thin
16 film growth, already achieved for ScFeO₃¹⁴, is a route to tune this further. The relationship
17 between M , α and the cation site order is also controllable via site-ordering extent. The absence
18 of measurable magnetic impurities under the optimised synthesis conditions is consistent with
19 the stability and chemical robustness of this new family of room temperature polar magnetic
20 magnetoelectric materials.

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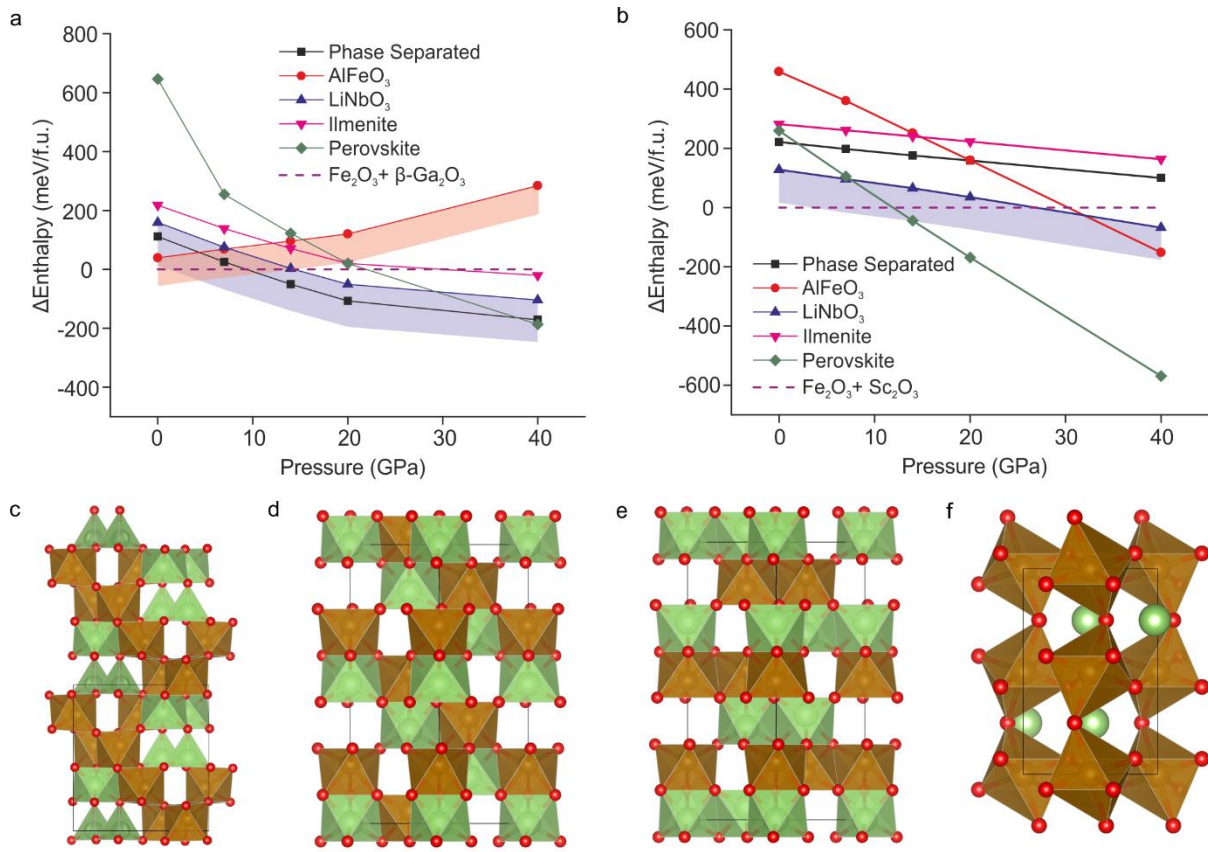


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3 **Figure 1:** Formation of the corundum phase by high temperature high pressure annealing. (a)
 4 Laboratory PXRD patterns obtained from GaFeO₃ quenched from a range of temperatures after
 5 annealing at 6 GPa. Patterns labelled A contain the starting AlFeO₃-structured phase, and those
 6 labelled C contain the corundum phase. (b) Refined weight fraction of the AlFeO₃ (black),
 7 corundum (red) phases and spinel decomposition phase (blue) as a function of temperature at
 8 6 GPa from in-situ neutron diffraction. (c) Rietveld refinement against in-situ neutron data
 9 collected at 6 GPa, 500 °C. Blue tick marks = corundum phase, magenta = AlFeO₃ phase, green
 10 = spinel phase. Asterisks (*) mark peaks from the Pt pressure calibrant; daggers (†) mark
 11 graphite peaks, double dagger (‡) marks a vanadium peak. (d) In-situ resistance measurements
 12 collected from a pellet of GaFeO₃ at 6 GPa cycled to increasing temperatures. Lines are a guide
 13 to the eye. The colours of the points correspond to their position in the heating sequence, which
 14 is shown inset.

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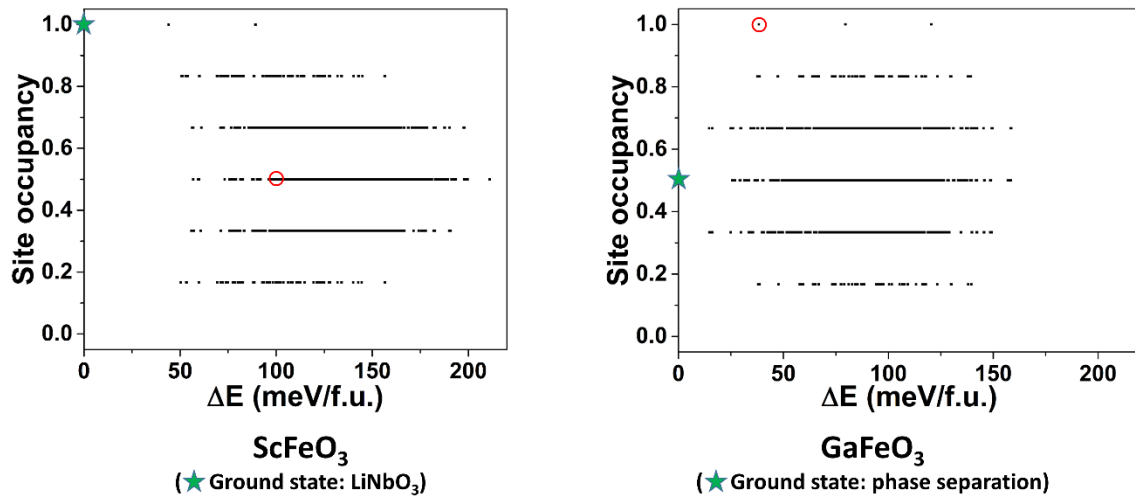
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2 **Figure 2:** Calculated enthalpies as a function of pressure for (a) GaFeO₃ polymorphs in the
3 AFM state, and (b) ScFeO₃ polymorphs in the AFM state, plotted relative to the binary oxides
4 α -Fe₂O₃ + β -Ga₂O₃ and α -Fe₂O₃ + Sc₂O₃. The shaded areas represent an estimate of the
5 configurational entropy of GaFeO₃ and ScFeO₃ at the respective synthesis temperatures of 1200
6 K and 1800 K: 98.8 meV/f.u. for the ambient pressure AlFeO₃-type GaFeO₃; 143 meV/f.u. for
7 corundum GaFeO₃ and 106 meV/f.u. for corundum ScFeO₃. (c) the ambient pressure AlFeO₃-
8 type structure of GaFeO₃ viewed along [001], which features edge-sharing chains of (Fe, Ga)
9 octahedra parallel to vertex-linked GaO₄ tetrahedra, (d) the polar LiNbO₃-type cation ordering
10 in the corundum structure, (e) the non-polar FeTiO₃ (ilmenite)-type cation ordering in the
11 corundum structure, (f) the optimised *Pbnm* perovskite-type structure used for this calculation,
12 which represents the phase that is accessible experimentally under applied pressures of 25
13 GPa²⁵. Atom colours: green = Ga(Sc), brown = Fe, red = O.

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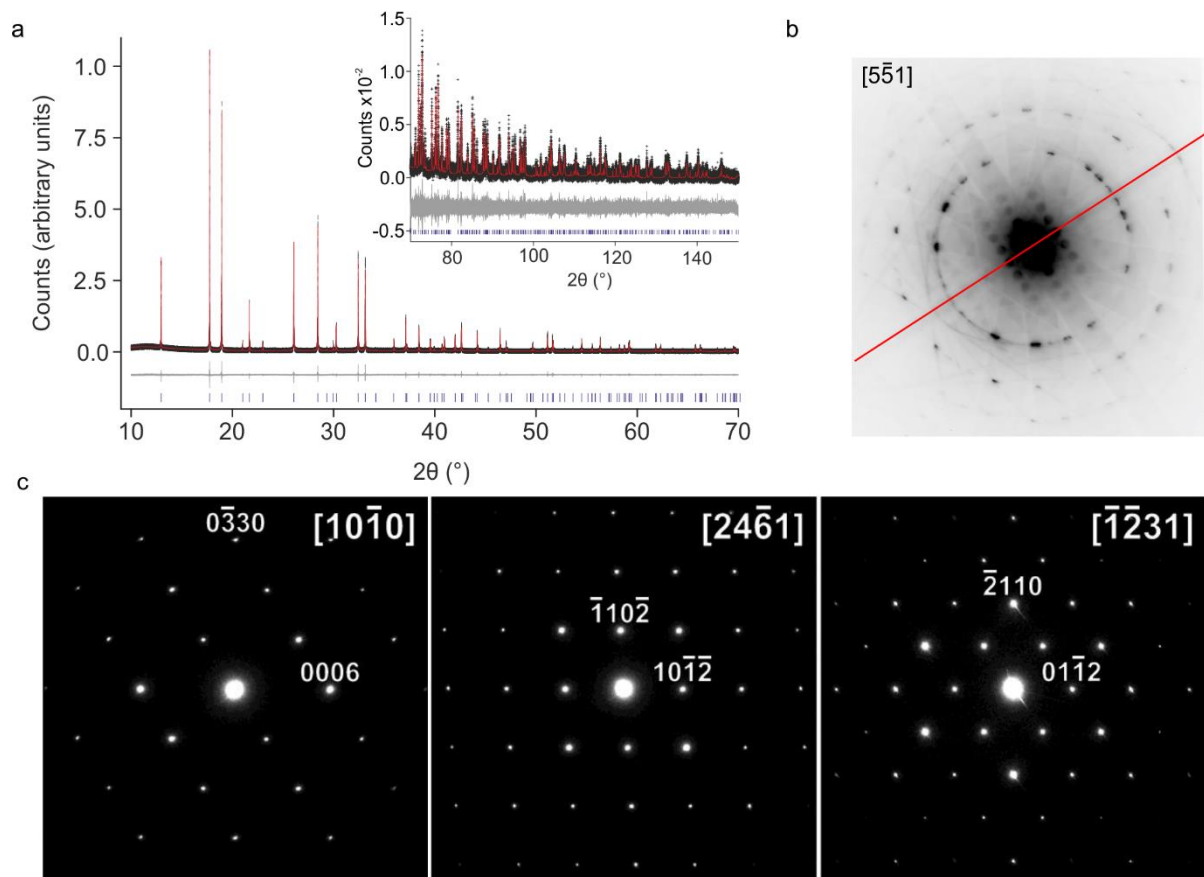
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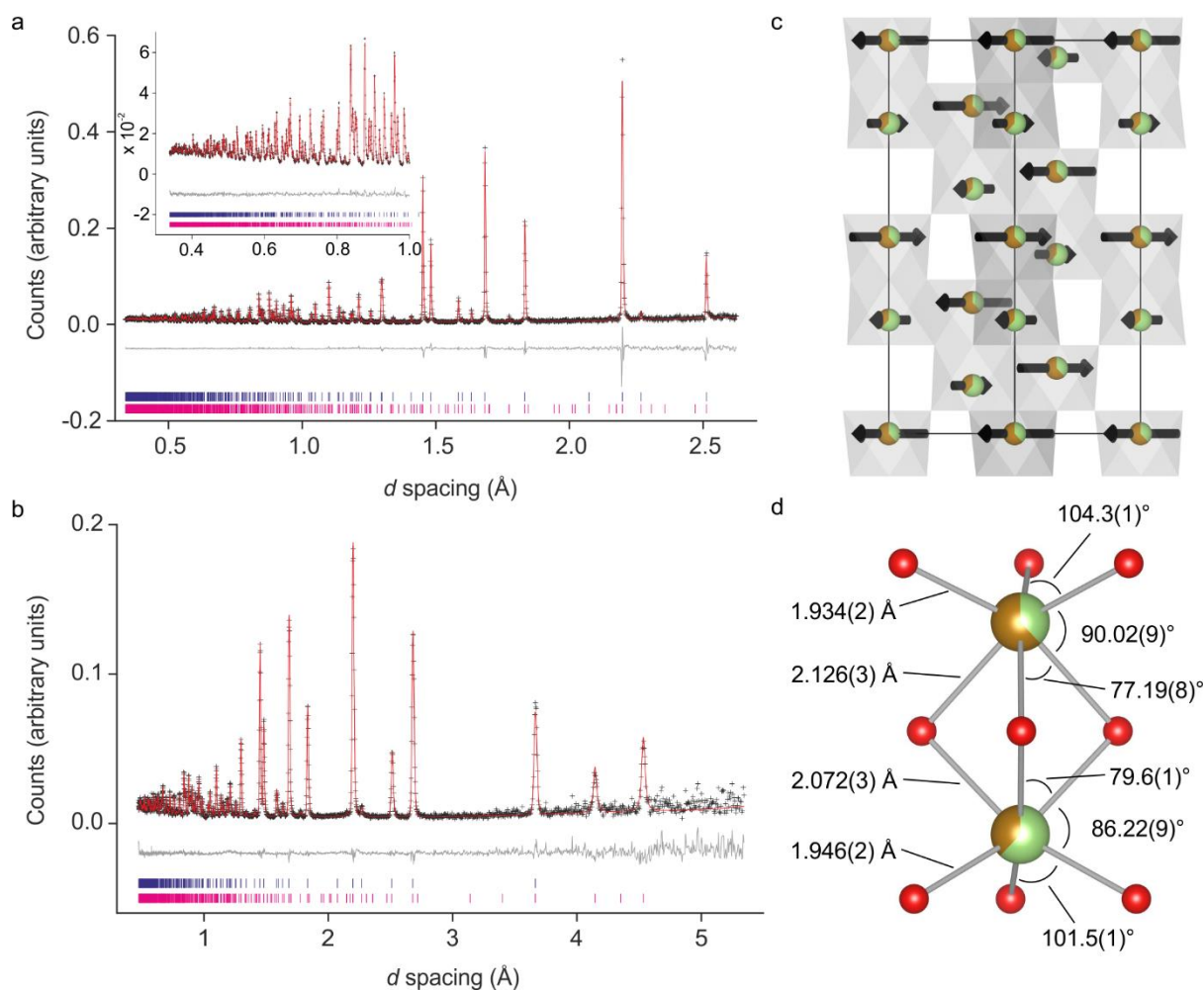
Figure 3: Calculated stabilities of different cation configurations in a hexagonal corundum-type unit cell. Site occupancies (defined as the proportion of Fe³⁺ cations in a given configuration that are coincident with Fe³⁺ positions in the fully ordered LiNbO₃ structure) of different configurations are plotted against their relative energies with respect to the ground state of ScFeO₃ (left) and GaFeO₃ (right). The phase separated structure of ScFeO₃ and the LiNbO₃-type GaFeO₃ are highlighted in red circles. The lowest energy configuration is marked with a green star symbol.

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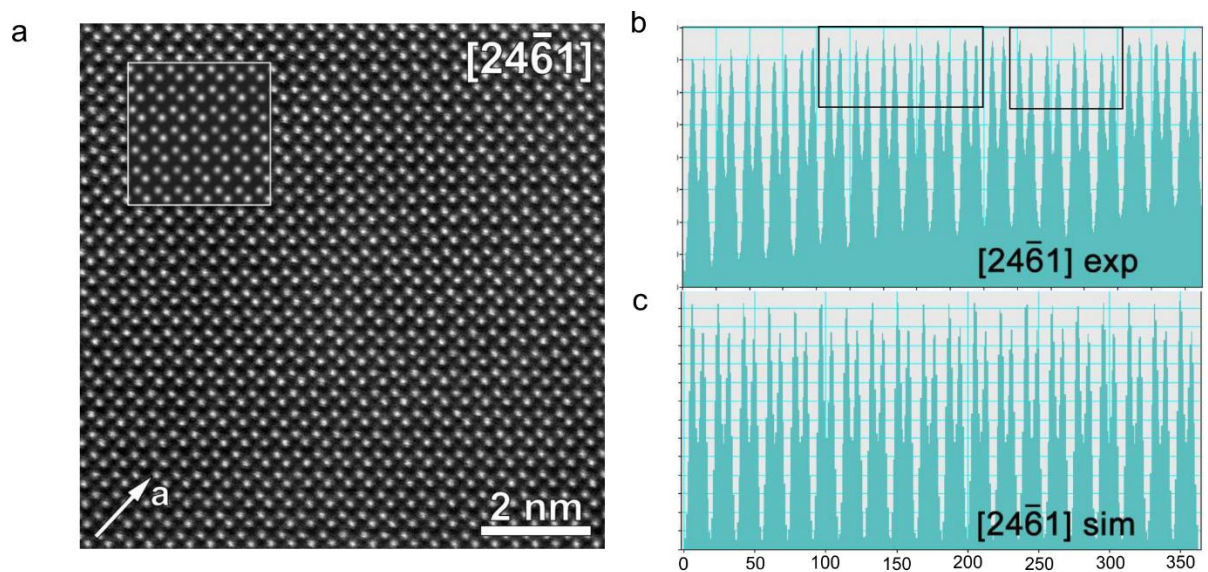
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 2 **Figure 4:** Unit cell and space group determination. (a) LeBail fit to SXRD data ($\lambda = 0.8256185$
 3 \AA) of corundum GaFeO_3 in the hexagonal setting of space group $R\bar{3}c$, which has the highest
 4 symmetry consistent with the systematic absences, yields a refined unit cell of dimensions $a =$
 5 $5.01959(3)$, $c = 13.5907(2)$ \AA . The fit to high angle data ($70 < 2\theta < 150^\circ$) is inset. Black markers
 6 = y_{obs} , red line = y_{calc} , grey line = $y_{\text{obs}} - y_{\text{calc}}$, blue tick marks = allowed hkl reflections. (b)
 7 CBED $[5\bar{5}1]$ zone axis pattern of corundum GaFeO_3 , which contains a mirror plane as the only
 8 symmetry element, consistent with space group $R3c$. (c) SAED patterns from three different
 9 zone axes, confirming the rhombohedral cell and systematic absences observed by SXRD.

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Figure 5: Refined polar corundum structure of GaFeO₃. (a) Rietveld refinement against NPD data from the Polaris back-scattering bank (inset: fit to the low d -spacing region), and (b) against Polaris bank 3 ($2\theta = 52.2^\circ$), which features two intense peaks of magnetic origin in the range $4 < d < 5$ Å; black markers = y_{obs} , red line = y_{calc} , grey line = $y_{\text{obs}} - y_{\text{calc}}$, blue tick marks = nuclear structure, magenta tick marks = magnetic structure. (c) The refined nuclear and magnetic structure of GaFeO₃ viewed along 110. At each atom, green segments indicate Ga occupancy, brown segments indicate Fe occupancy, black arrows indicate magnetic moments which are ordered parallel to the a axis in an antiferromagnetic arrangement. The magnitudes of the ordered moments are indicated by the sizes of the arrows. (d) The local coordination environments of the two crystallographically independent cation sites, which occupy adjacent face-sharing octahedra. The colours indicate the extent of occupancy by Fe (brown) and Ga (green).

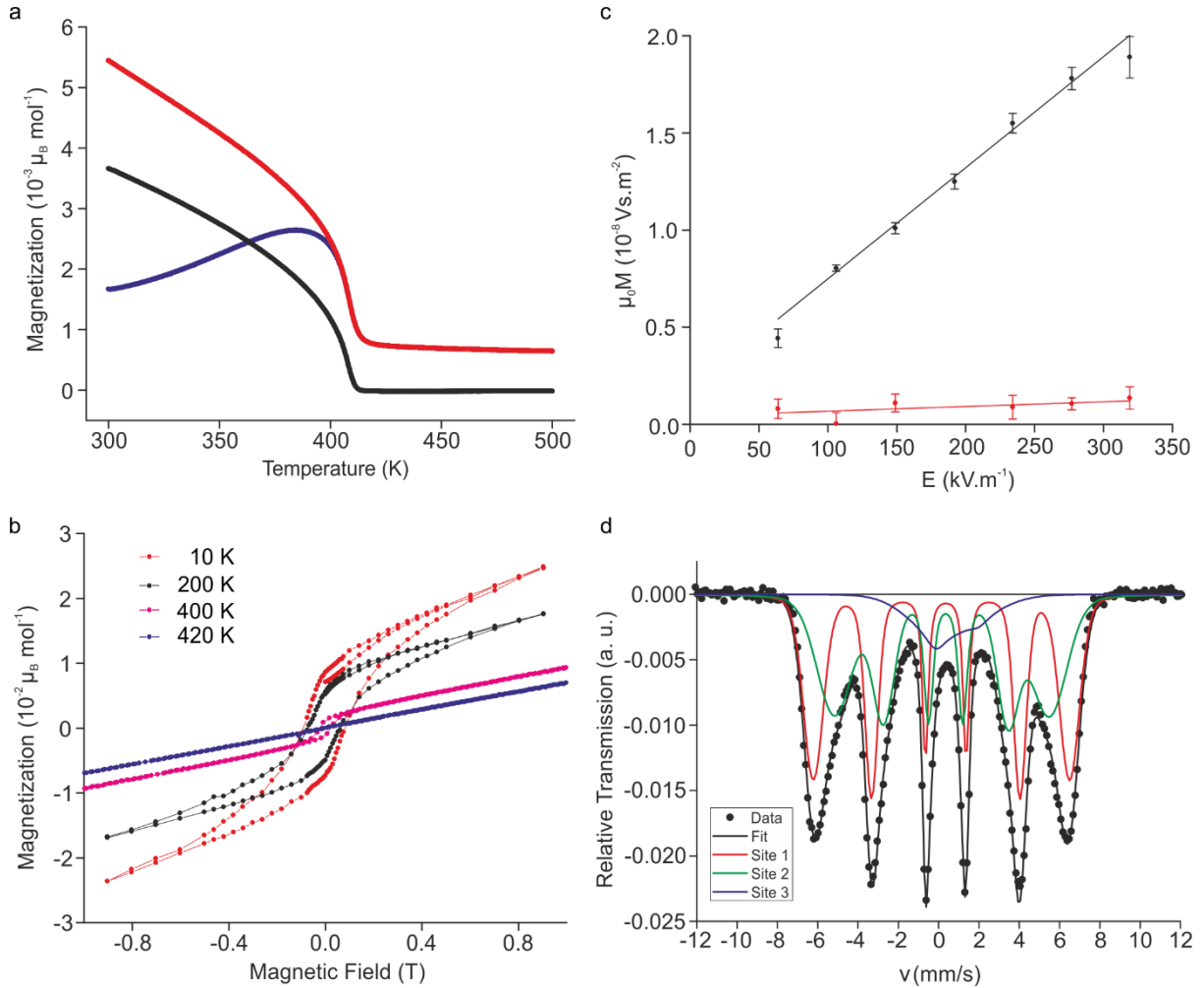


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2 **Figure 6:** HAADF-STEM analysis of polar corundum GaFeO₃ (a) Experimental HAADF-
 3 STEM image from the [24̄61] axis, with a simulated image (inset) generated from the refined
 4 (PND) crystal structure. (b) Intensity profiles measured from individual rows of atomic
 5 columns over large areas from the experimental image, and (c) intensity profiles measured
 6 over large areas from the simulated image. Regions in (b) that resemble the simulated
 7 structure of (c) are marked with black rectangles.

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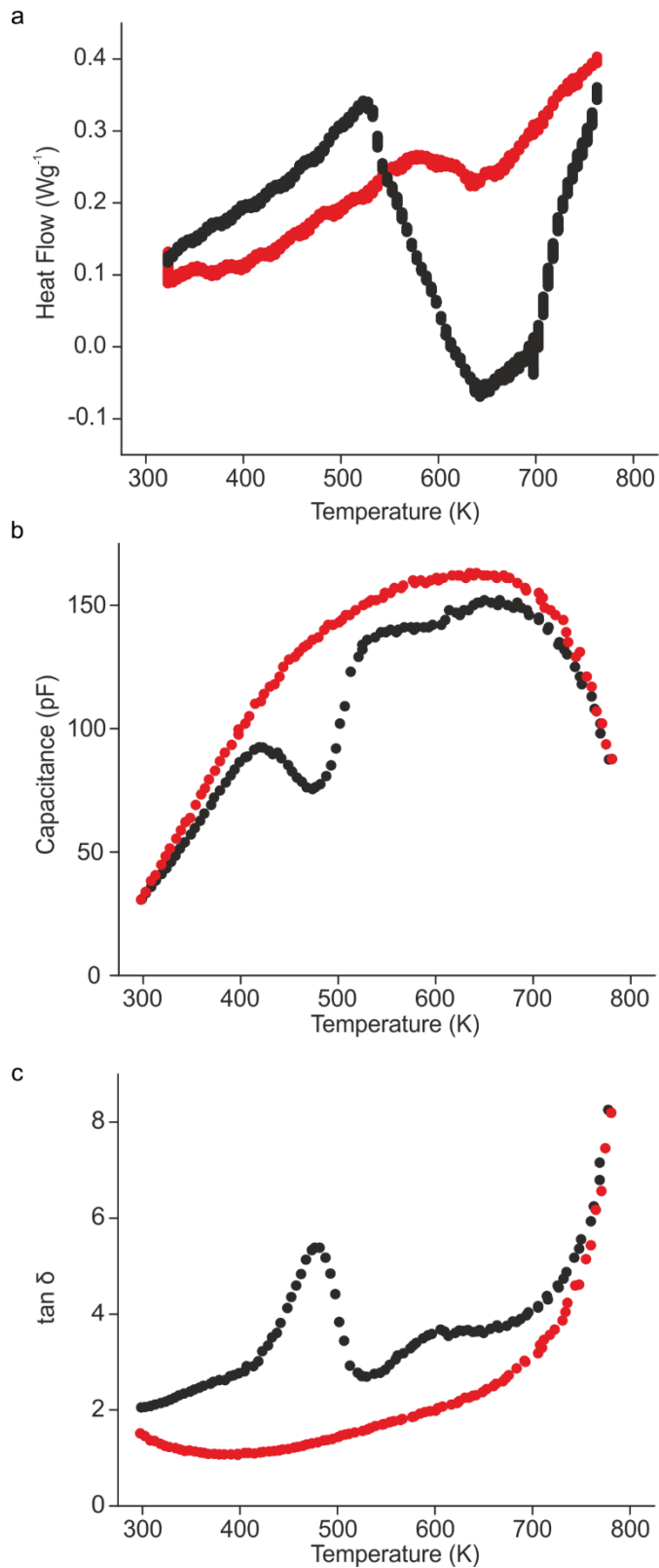
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6 **Figure 7.** Magnetic properties of polar corundum GaFeO₃. (a) Zero-field cooled (blue points),
 7 field-cooled (red points) and remanent (black) magnetization as a function of temperature in
 8 the range 300 – 500 K, measured with an applied field of 0.1 T. (b) Magnetization as a function
 9 of applied magnetic field at temperatures of 10 K (red points), 200 K (black points), 400 K
 10 (magenta points) and 420 K (blue points). (c) Induced ac magnetization versus applied ac
 11 electric field amplitude at 10 K for two samples: as-made (black points), and post-annealed at
 12 380 °C (red points). (d) ⁵⁷Fe Mössbauer spectrum at ambient temperature, showing hyperfine
 13 splitting consistent with long-range magnetic ordering, and fitted with a three-site model (see
 14 Table 3 for fitted parameters).

15



1

2 **Figure 8:** Calorimetric and dielectric behaviour of polar corundum GaFeO_3 synthesised at
 3 900 °C. (a) DSC scans performed on heating, black points represent the first cycle and red
 4 points represent the second cycle. (b) Capacitance data recorded on first heating cycle (black
 5 points) and second heating cycle (red points). (c) Dielectric loss recorded on first heating
 6 cycle (black points) and second heating cycle (red points).

7

1

2 **Table 1:** Structural parameters for $R3c$ GaFeO₃ (sample 1) from Rietveld refinement against
 3 room temperature NPD, with refined lattice parameters $a = 5.01871(9)$ Å, $c = 13.5879(3)$ Å, V
 4 $= 296.39(1)$ Å³.

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	x	y	z	$B_{\text{iso}} / \text{Å}^2$	Occ.	M / μ_B
Ga(1)	0	0	0	0.231(3)	0.32(2)	
Fe(1)	0	0	0	0.231(3)	0.68(2)	1.03(3)
Fe(2)	0	0	0.28919(5)	0.231(3)	0.32(2)	2.15(2)
Ga(2)	0	0	0.28919(5)	0.231(3)	0.68(2)	
O(1)	0.3026(2)	-0.0046(4)	0.8922(3)	0.284 (5)	1	

6

7

8 **Table 2:** Structural parameters for $R3c$ GaFeO₃ (sample 2) refined against room temperature
 9 NPD data, with refined lattice parameters $a = 5.02547(9)$ Å, $c = 13.6057(3)$ Å, $V = 297.31$ (2)
 10 Å³.

11

	x	y	z	$B_{\text{iso}} / \text{Å}^2$	Occ.	M / μ_B
Ga(1)	0	0	0	0.216(4)	0.38(3)	
Fe(1)	0	0	0	0.216(4)	0.62(3)	1.08(4)
Fe(2)	0	0	0.28906(5)	0.216(4)	0.38(3)	2.00(3)
Ga(2)	0	0	0.28906(5)	0.216(4)	0.62(3)	
O(1)	0.3030(3)	-0.0033(5)	0.8916(2)	0.34(2)	1	

12

13 **Table 3:** Mössbauer fitting parameters for the spectrum of Figure 7. The errors are provided
 14 in brackets.

Site	B_{hf} (T)	ΔB_{hf} (T)	IS (mm/s)	QS (mm/s)	A (%)
1	39.49(2)	0.28(1)	0.249(3)	0.21(1)	44.00(1)
2	33.11(2)	0.37(1)	0.257(3)	0.19(1)	47.09(1)
3	0	0	0.93(1)	2.16(3)	8.91(1)

15

16

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