

ExoMol line list – XXI. Nitric Oxide (NO)

Andy Wong,¹ Sergei N. Yurchenko,² Peter Bernath,¹ Holger S. P. Müller,³
Stephanie McConkey² and Jonathan Tennyson²★

¹Department of Chemistry and Biochemistry, Old Dominion University, 4541 Hampton Boulevard, Norfolk, VA 23529, USA

²Department of Physics and Astronomy, University College London, London WC1E 6BT, UK

³I. Physikalisches Institut, Universität zu Köln, Zùlpicher Str. 77, D-50937 Köln, Germany

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ABSTRACT

Line lists for the X ²Π electronic ground state for the parent isotopologue of nitric oxide (¹⁴N¹⁶O) and five other major isotopologues (¹⁴N¹⁷O, ¹⁴N¹⁸O, ¹⁵N¹⁶O, ¹⁵N¹⁷O and ¹⁵N¹⁸O) are presented. The line lists are constructed using empirical energy levels (and line positions) and high-level *ab initio* intensities. The energy levels were obtained using a combination of two approaches, from an effective Hamiltonian and from solving the rovibronic Schrödinger equation variationally. The effective Hamiltonian model was obtained through a fit to the experimental line positions of NO available in the literature for all six isotopologues using the programs SPFIT and SPCAT. The variational model was built through a least squares fit of the *ab initio* potential and spin–orbit curves to the experimentally derived energies and experimental line positions of the main isotopologue only using the DUO program. The *ab initio* potential energy, spin–orbit and dipole moment curves (PEC, SOC and DMC) are computed using high-level *ab initio* methods and the MARVEL method is used to obtain energies of NO from experimental transition frequencies. The line lists are constructed for each isotopologue based on the use of the most accurate energy levels and the *ab initio* DMC. Each line list covers a wavenumber range from 0 to 40 000 cm^{−1} with approximately 22 000 rovibronic states and 2.3–2.6 million transitions extending to $J_{\max} = 184.5$ and $v_{\max} = 51$. Partition functions are also calculated up to a temperature of 5000 K. The calculated absorption line intensities at 296 K using these line lists show excellent agreement with those included in the HITRAN and HITEMP data bases. The computed NO line lists are the most comprehensive to date, covering a wider wavenumber and temperature range compared to both the HITRAN and HITEMP data bases. These line lists are also more accurate than those used in HITEMP. The full line lists are available from the CDS <http://cdsarc.u-strasbg.fr> and ExoMol www.exomol.com data bases; data will also be available from CDMS <http://www.cdms.de>.

Key words: planetary systems.

1 INTRODUCTION

NO has been detected in several interstellar environments ranging from a starburst galaxy (Martin et al. 2003, 2006) to dark clouds (McGonagle et al. 1990) and numerous star-forming regions (Ziurys et al. 1991). It is also present in the atmospheres of Earth, Mars and Venus, and its emission is a major source of nightglow in these three planets (Eastes, Huffman & Leblanc 1992; Cox et al. 2008; Royer, Montmessin & Bertaux 2010). The presence of NO in Earth’s atmosphere has a significant impact on depletion of the ozone layer (Barry & Chorley 2010; Wayne 2000) and originates

from the reaction of N₂O with O(¹D) in the stratosphere. In the troposphere, the major sources of NO are of anthropogenic origin as it is produced during fuel combustion at temperatures of ~2300 K (Flagan & Seinfeld 1988) and through soil cultivation. Because NO (and NO₂) catalyse the production of tropospheric ozone, it is important to try to reduce NO emissions (amongst other air pollutants). Whilst NO has not yet been detected in an exoplanet atmosphere, it is likely present in its gaseous form in terrestrial-type atmospheres, for example produced during a storm soon after a lightning shock (Ardaseva et al. 2017).

There are currently two commonly used data bases that contain line lists for NO in its electronic ground state: HITRAN (Rothman et al. 2013) that covers ¹⁴N¹⁶O, ¹⁴N¹⁸O and ¹⁵N¹⁶O, and is designed for use near room temperature, and HITEMP (Rothman et al. 2010)

★E-mail: j.tennyson@ucl.ac.uk.

that allows the spectrum of $^{14}\text{N}^{16}\text{O}$ to be modelled up to 4000 K. HITRAN and HITEMP data bases contain 103 702 and 115 610 transitions, respectively, with $J_{\text{max}} = 125.5$ and $v_{\text{max}} = 14$.

The aim of this work is to produce line lists for the $X^2\Pi$ electronic ground state of nitric oxide for its parent isotopologue ($^{14}\text{N}^{16}\text{O}$, hereafter NO), and five major isotopologues ($^{14}\text{N}^{17}\text{O}$, $^{14}\text{N}^{18}\text{O}$, $^{15}\text{N}^{16}\text{O}$, $^{15}\text{N}^{17}\text{O}$ and $^{15}\text{N}^{18}\text{O}$). Using a combination of high-level *ab initio* methods, accurate fitting to a comprehensive set of experimental data and variational modelling, six line lists for these species were constructed. These line lists consist of rovibronic energy levels, with all of the associated quantum numbers, transition wavenumbers and *Einstein-A* coefficients. The computed line lists form part of the ExoMol data base (Tennyson et al. 2016c) that aims to provide a comprehensive set of high-temperature line lists for molecules that may be present in hot atmospheres such as those of exoplanets, planetary discs, brown dwarfs and cool stars (Tennyson & Yurchenko 2012). Many ExoMol line lists have already been used in the characterization and modelling of brown dwarf and exoplanet atmospheres (Tinetti et al. 2007; Beaulieu et al. 2011; Cushing et al. 2011; Morley et al. 2014, 2015; Yurchenko et al. 2014; Barman et al. 2015; Canty et al. 2015; Molliere et al. 2015; Tsiasas et al. 2016).

The ExoMol data base already contains line lists for numerous diatomic molecules generated by the ExoMol project: AIO (Patrascu, Tennyson & Yurchenko 2015), BeH, MgH and CaH (Yadin et al. 2012), SiO (Barton, Yurchenko & Tennyson 2013), CaO (Yurchenko et al. 2016b), CS (Paulose et al. 2015), NaCl and KCl (Barton et al. 2014), NaH (Rivlin et al. 2015), PN (Yorke et al. 2014), ScH (Lodi, Yurchenko & Tennyson 2015) and VO (McKemmish, Yurchenko & Tennyson 2016). Line lists available from other sources include: CrH (Burrows et al. 2002), FeH (Dulick et al. 2003), TiH (Burrows et al. 2005), CaH (Li et al. 2012), MgH (GharibNezhad, Shayesteh & Bernath 2013), CN (Brooke et al. 2014), OH (Brooke et al. 2016), NH (Brooke, Bernath & Western 2015) and ZrS (Farhat 2017).

These line lists often include many of the abundant isotopologues and greatly extend the calculated range of J and v in comparison to the HITRAN and HITEMP data bases. High-temperature line lists are useful in the characterization of brown dwarfs (Yurchenko et al. 2014), which have atmospheric temperatures ranging from 500 to 3000 K (Perryman 2014). The hot NO line lists produced from this work can be used directly in characterization of the spectra of such objects, as well as in atmospheric models (de Vera & Seckbach 2013).

The remainder of this paper is divided into several sections. Section 2 outlines the methods used in the calculation of energy levels and production of the line lists, whilst Section 3 presents the results of this work – mainly the NO line list, the calculated partition function and radiative lifetimes. Absorption line intensities and cross-sections are also shown. Finally, Section 4 discusses the implications of this work, and how it will be significant to the astrophysical community.

2 METHODS

2.1 Experimental data

2.1.1 Extraction of experimental data

Transition frequencies for the $X^2\Pi$ electronic ground state of NO were collected from selected experimental papers, see Table 1, along with any given quantum numbers and uncertain-

ties for all six isotopologues. This table also indicates whether a data set was used for the MARVEL analysis (M), SPFIT calculations (S) or both (see below). We used the MARVEL program (Measured Active Rotational-Vibrational Energy Levels; Furtenbacher, Császár & Tennyson 2007; Furtenbacher & Császár 2012a) to derive energy levels of the main isotopologue $^{14}\text{N}^{16}\text{O}$ based on the experimental transition data available in the literature. These data were then utilized to refine our *ab initio* model using the DUO program (Yurchenko et al. 2016a). The more extensive SPFIT set of experimental frequencies covering all six isotopologues was used to obtain NO spectroscopic constants in a global fit using the effective Hamiltonian programs SPFIT and SPCAT (Pickett 1991).

2.1.2 MARVEL

MARVEL is an algorithm that calculates rovibronic energy levels from a given set of experimental transitions. The online¹ version of the program was used, as the output files are formatted to be more user-friendly. An extraction from our MARVEL input file is given in Table 2.

The experimental literature was chosen to ensure that a full range of transitions was included whilst minimizing duplication of data. Although the default MARVEL procedure utilizes all of the data included in the input file (Furtenbacher & Császár 2012b), if there happens to be any data overlap between papers, only the most accurate (and in general the most recent) data are considered. Only transitions within the ground electronic state were considered for our MARVEL analysis.

Pure rotational transition frequencies were taken from Van den Heuvel et al. (1980), Lovas & Tiemann (1974) and Varberg et al. (1999), whilst transitions between the two spin-components ($X^2\Pi_{\frac{1}{2}}$ and $X^2\Pi_{\frac{3}{2}}$) were taken from Mandin et al. (1994). Rovibrational transitions, extending up to $\Delta v = 3$, $v' = 22$ and $J' = 58.5$, were taken from the work by Amiot (1982), Amiot & Verges (1980), Bood et al. (2006), Coudert et al. (1995), Lee et al. (2006), Mandin et al. (1997, 1998) and Spencer et al. (1994).

It should be noted that the spectroscopic notation is not consistent in the literature, thus making it necessary to generate a consistent set of quantum numbers for each transition. For many of the rovibrational papers, the P , Q and R labels were used to derive J' if J' and J'' had not already been specified. In the case of Amiot (1982) and Amiot & Verges (1980), the projection of the total angular momentum (Ω) was determined by assigning transitions labelled P_1 and R_1 to a value of $\Omega'' = \frac{1}{2}$ and those labelled P_2 and R_2 to the corresponding $\Omega'' = \frac{3}{2}$. Rotationless parities of lower levels were given in terms of e and f by Coudert et al. (1995), Mandin et al. (1994, 1997) and Spencer et al. (1994). For papers that did not specify parity, this was resolved by duplicating the data set and assigning the parity e to one set and the parity f to the other. Hyperfine splitting was also resolved, albeit only in a few pure rotational papers (Van den Heuvel et al. 1980; Lovas & Tiemann 1974; Varberg et al. 1999); however, at this stage of our analysis the hyperfine splitting was ignored. For rovibrational transitions sharing the same quantum numbers (Ω' , Ω'' , J' , J'' and e/f) but different frequency, an average of the two frequencies was taken and the frequency uncertainty was propagated. In lieu of any specified transition frequency uncertainties, estimates were made based upon the precision with which frequencies were quoted.

¹ <http://kkkrk.chem.elte.hu/Marvelonline>

Table 1. Experimental papers on NO spectra.

Source	States	Isotopologue; methods ^a	M/S ^b	Range in J and/or v
64James	James (1964)	NO; IR	M	$J = 0.5-21.5$
64JaThxx	James & Thibault (1964)	NO; IR	M	$J = 1.5-21.5$
70Neumann	Neumann (1970)	NO; RF, μ	S	$J = 0.5-7.5, v = 0$
72MeDyxx	Meerts & Dymanus (1972)	NO, ¹⁵ N ₂ O; IR	S	$J = 0.5-8.5, v = 0$
76Meerts	Meerts (1976)	NO; RF	S	$J = 4.5-5.5, v = 0$
77DaJoMc	Dale et al. (1977)	NO; IR-RF DR	S	$J = 4.5-5.5, v = 0, 1$
78AmBaGu	Amiot, Bacis & Guelachvili (1978)	NO; FTIR	S	$J = 0.5-40.5, v = 1-0, 2-1$
78HeLeCa	Henry et al. (1978)	NO; FTIR	S	$J = 0.5-28.5, v = 3-0$
79AmGuxx	Amiot & Guelachvili (1979)	¹⁵ NO, ¹⁵ N ¹⁷ O, ¹⁵ N ¹⁸ O; FTIR	S	$J = 0.5-41.5, v = 1-0, 2-1$
79PiCoWa	Pickett et al. (1979)	NO; mmW, smmW	S	$J = 0.5-4.5, v = 0$
80AmVexx	Amiot & Verges (1980)	NO; Emi, FTIR 2900–3810 cm ⁻¹	M,S	$J = 0.5-57.5, v = 0-15, \Delta v = 2$
80TeHeCa	Teffo et al. (1980)	¹⁵ NO, ¹⁵ N ¹⁸ O; FTIR	S	$J = 0.5-32.5, v = 1-0, 2-0, 3-0$
80VaMeDy	Van den Heuvel, Meerts & Dymanus (1980)	NO; TuFIR	M	$J = 7.5-10.5$
81LoMcVe	Lowe et al. (1981)	NO; IR-RF DR	S	$J = 12.5-20.5, v = 0, 1$
82Amiot	Amiot (1982)	NO; Emi, FTIR, 3800–5000 cm ⁻¹	M,S	$J = 0.5-59.5, v = 7-22, \Delta v = 3$
86HiWeMa	Hinz, Wells & Maki (1986)	NO; heterodyne IR	S	$J = 1.5-32.5, v = 1-0$
91SaYaWi	Saleck, Yamada & Winnewisser (1991)	¹⁵ NO, N ¹⁸ O ^c ; mmW, smmW	S	$J = 0.5-4.5, v = 0$
92RaFrMi	Rawlins et al. (1992)	NO; IR ChLumi, 2.7–3.3 μ m	M	5.2–6.8 μ m $v' = 2-3$
94DaMaCo	Dana et al. (1994)	NO; FTIR	M,S	$J = 2.5-24.5, v = 2-1$
94MaDaCo	Mandin et al. (1994)	NO; FTIR	M	$J = 1.5-20.5, v = 1-0$
94SaLiDo	Saleck et al. (1994)	N ¹⁷ O and ¹⁵ N ¹⁸ O; mmW	S	$J = 0.5-2.5, v = 0$
94SpChGi	Spencer et al. (1994)	NO; FTIR 1780–1960 cm ⁻¹	M,S	$J = 0.5-25.5, v = 1-0$
95CoDaMa	Coudert et al. (1995)	NO; FTIR ^d 1730–1990 cm ⁻¹	M,S	$J = 0.5-41.5, v = 1-0$
96SaMeWa	Saupe et al. (1996)	NO; heterodyne IR	S	$J = 8.5-18.5, v = 1-0$
97DaDoKe	Danielak et al. (1997)	O ₂ /N ₂ ; Ebert spectrograph	M	$v = 0-7$
97MaDaRe	Mandin et al. (1997)	NO; FTIR, 3600–3800 cm ⁻¹	M,S	$J = 2.5-32.5, v = 2-0$
98MaDaRe	Mandin et al. (1998)	NO; FTIR, 3600–3720 cm ⁻¹	M	$J = 2.5-17.5, v = 3-1$
99VaStEv	Varberg, Stroh & Evenson (1999)	NO; TuFIR, 11–157 cm ⁻¹	M	$J = 2.5-38.5$
99VaStEv	Varberg et al. (1999)	NO; ¹⁵ NO; TuFIR, 11–157 cm ⁻¹	S	$J = 2.5-38.5, v = 0$
01LiGuLi	Liu et al. (2001)	NO; IR LMR, μ	S	$J = 1.5-2.5, v = 1-0$
06LeChOg	Lee, Cheah & Ogilvie (2006)	NO; FTIR	M	$J = 0.5-30.5, v' = 2-6$
06BoMcOs	Bood, McIlroy & Osborn (2006)	NO; NICE-OHMS	M	$J = 2.5-16.5, v = 7-0$
15MuKoTa	Müller et al. (2015)	N ¹⁸ O; TuFIR, 33–159 cm ⁻¹	S	$J = 3.5-26.5, v = 0$

^aUnlabelled atoms refer to ¹⁴N or ¹⁶O. Abbreviations: IR (infrared), FT (Fourier transform), ChLumi (chemiluminescence), Emi (emission), DR (double resonance), μ (dipole moment), RF (radio frequency), MW (microwave), mmW (millimetre wave), smmW (submillimetre wave), TuFIR (tunable far-infrared) and LMR (laser magnetic resonance).

^bUsed for MARVEL (M) and/or SPFIT (S).

^cNO FIR data not used.

^dWavenumber recalibration proposed, see Section 2.4.

Table 2. MARVEL format of the experimental data: extract from the MARVEL input file.

Wavenumber (cm ⁻¹)	Uncertainty (cm ⁻¹)	J'	Parity'	v'	Ω'	J''	Parity''	v''	Ω''	Reference
1985.3307	0.005	42.5	–	1	0.5	41.5	+	0	0.5	95CoDaMa80
1806.6561	0.005	17.5	+	1	1.5	18.5	–	0	1.5	95CoDaMa81
1806.6561	0.005	17.5	–	1	1.5	18.5	+	0	1.5	95CoDaMa82
1802.5924	0.005	18.5	+	1	1.5	19.5	–	0	1.5	95CoDaMa83
1802.5924	0.005	18.5	–	1	1.5	19.5	+	0	1.5	95CoDaMa84
1798.4950	0.005	19.5	+	1	1.5	20.5	–	0	1.5	95CoDaMa85
1798.4950	0.005	19.5	–	1	1.5	20.5	+	0	1.5	95CoDaMa86
1794.3687	0.005	20.5	+	1	1.5	21.5	–	0	1.5	95CoDaMa87
1794.3687	0.005	20.5	–	1	1.5	21.5	+	0	1.5	95CoDaMa88
1790.2060	0.005	21.5	+	1	1.5	22.5	–	0	1.5	95CoDaMa89
1790.2060	0.005	21.5	–	1	1.5	22.5	+	0	1.5	95CoDaMa90
1786.0180	0.005	22.5	+	1	1.5	23.5	–	0	1.5	95CoDaMa91

The e/f parity of the lower energy states were converted to \pm -total parity using the following standard relations:

$$e : \text{parity} = (-1)^{J-1/2}$$

$$f : \text{parity} = (-1)^{J+1/2},$$

where -1 and $+1$ corresponds an odd (–) parity and even parity (+), respectively. The $+$ \leftrightarrow $-$ selection rule was used to determine the parity of the upper state. For each transition, the electronic state and the projection of the electronic angular Λ remained unchanged as only rovibrational transitions within the X ²Π electronic ground state were considered in this work.

The quoted uncertainty of some transition frequencies was found to be either too large or too small. In these cases, the uncertainty value was adjusted to agree with the MARVEL-suggested uncertainty. After some trial and error, a clean run in MARVEL with no errors was achieved yielding a network of 4106 energy levels for NO with $v_{\max} = 22$, $J_{\max} = 58.5$ and a term value maximum of $36\,200\text{ cm}^{-1}$. The MARVEL energies obtained and the input file containing experimental transition frequencies are given as supplementary material to this paper.

The MARVEL procedure has previously been used to treat two other open shell diatomics of astronomical importance: C_2 (Furtenbacher et al. 2016) and TiO (McKemmish et al. 2017). The treatment of a single, albeit $^2\Pi$, state here proved to be much simpler than either of those studies, which included a large number of electronic transitions.

2.2 *Ab initio* calculations

The *ab initio* potential energy curve (PEC), spin-orbit curve (SOC) and dipole moment curve (DMC) for the $X^2\Pi$ electronic ground state of NO were calculated using MOLPRO (Werner et al. 2012). An active space representation of (7,2,2,0) was chosen and an internally contracted multireference configuration interaction (icMRCI) method was used with Dunning-type basis sets (Peterson & Dunning 2002). A quadruple- ζ aug-cc-pwCVQZ-DK basis set was used to calculate the PEC and SOC, whereas the DMC was calculated using a quintuple- ζ aug-cc-pwCV5Z-DK basis set. The range of 0.6–10.0 Å was used with a dense grid of 350 geometries. Relativistic corrections for the DMC were also evaluated based on the Douglas–Kroll–Hess (DKH) Hamiltonian that included core correlation. The *ab initio* PEC and SOC are shown in Fig. 1.

A quadruple- ζ basis set was considered sufficient for the PEC and SOC as these *ab initio* curves were fitted to the experimental data using DUO. A more accurate level of theory MRCI/aug-cc-pwCV5Z-DK (Werner & Knowles 1988; Balabanov & Peterson 2005, 2006) with the relativistic corrections based on the DKH Hamiltonian and core-correlated was used for the DMC as implemented in MOLPRO (Werner et al. 2012). The DMC was calculated using the energy-derivative method (Lodi & Tennyson 2010) that calculates the dipole moment as a derivative of the electronic energy $E(F)$ with respect to an external electric field F ($F = 0.0005\text{ au}$ in this case) using finite differences. A dipole moment of $\mu_e = 0.166\text{ D}$ at an equilibrium internuclear distance $r_e = 1.15\text{ Å}$ was obtained. Neumann (1970) reported an experimental value for $\mu_0 = 0.15782(2)\text{ D}$, and Liu et al. (2001) determined $\mu_0 = 0.1595(15)\text{ D}$ and $\mu_1 = 0.1425(16)\text{ D}$. Our value agrees very well with our values which are 0.1553 D and 0.1381 D, respectively. The *ab initio* DMC is shown in Fig. 2.

2.3 DUO: FITTING

DUO is a program designed to solve a coupled Schrödinger equation for the motion of nuclei of a given diatomic molecule characterized by an arbitrary set of electronic states (Yurchenko et al. 2016a). Based on Hund’s case (a), DUO is capable of both refining PECs (by fitting data to experimental energies or transition frequencies) and producing line lists. An extensive discussion of this method to calculate the direct solution of the vibronic Schrödinger equation has been given in a recent topical review (Tennyson et al. 2016b).

For this study, the range of computed J levels was chosen to roughly correspond to all bound states of the system, i.e. to all states below D_0 ($J = 0.5\text{--}184.5$). The vibrational basis set was specified to

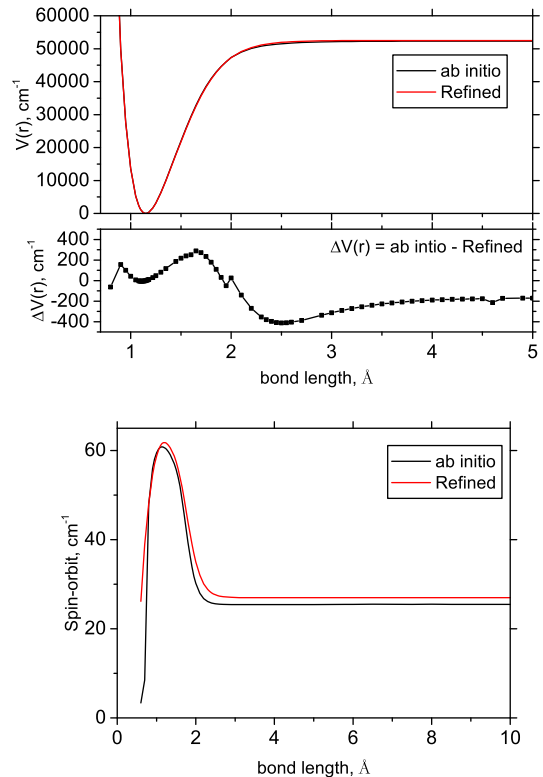


Figure 1. *Ab initio* and DUO refined PECs (upper display) and SOCs (lower display). The middle display shows the difference between the *ab initio* and refined PECs.

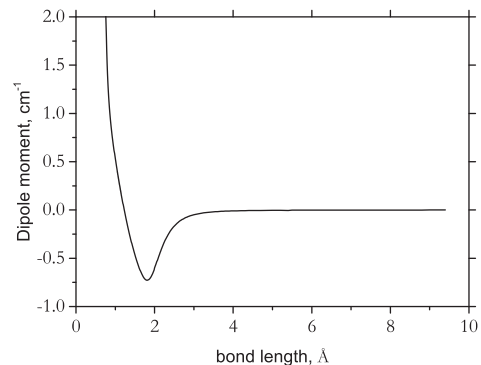


Figure 2. *Ab initio* MRCI/aug-cc-pwCV5Z-DK DMC of NO.

have $v_{\max} = 51$, which also corresponds to the maximum number of vibrational states (taken at $J = 0$). The sinc DVR method defined on a grid of 701 points evenly distributed between 0.6 and 4.0 Å was used in integrations. The sinc DVR allows one to reduce the number of points with no significant loss of accuracy. For example, all energies obtained with this grid coincide with the energies obtained using a larger grid of 3001 points to better than 10^{-6} cm^{-1} .

The PEC and SOC were defined using the Extended Morse Oscillator (EMO) potential (Lee et al. 1999) given by

$$V(r) = V_e + D_e [1 - \exp(-\beta_{\text{EMO}}(r)(r - r_e))]^2, \quad (1)$$

where D_e is the dissociation energy, N is the expansion order parameter, r_e is the equilibrium internuclear bond distance and β_{EMO} is the distance-dependent exponent coefficient, defined as

$$\beta_{\text{EMO}}(r) = \sum_{i=0}^N B_i y_p(r)^i \quad (2)$$

and y_p is the Šurkus variable (Šurkus, Rakauskas & Bolotin 1984) given by

$$y_p(r) = \frac{r^p - r_e^p}{r^p + r_e^p} \quad (3)$$

with p as a parameter. The EMO form is our common choice for representing PECs of diatomics (Lodi et al. 2015; Patrascu et al. 2015; McKemmish et al. 2016; Yurchenko et al. 2016b). It guarantees the correct dissociation limit and also allows extra flexibility in the degree of the polynomial around a reference position R_{ref} , which was defined as the equilibrium internuclear separation (r_e) in this case. It is also very robust in the fit. The disadvantage of EMO is that it does not correctly describe the dissociative part of the curve. As we show below, this drawback does not have a significant impact on our line lists.

A reasonable alternative to EMO is the Morse/long-range (MLR) potential representation (Roy & Henderson 2007; Roy et al. 2009; Le Roy et al. 2011), which guarantees a physically correct, multipole-type representation of the PEC as inverse powers of r for $r \rightarrow \infty$. The disadvantage of MLR (at least according to our experience) is that it is less robust than EMO in refinements, requiring very careful determination of the switching and damping functions (see, for example, Le Roy et al. 2011). Furthermore, Lodi, Polyansky & Tennyson (2008) showed that for strongly bound systems the multipole-type expansion is unnecessary and ‘possibly harmful’, except for very large values of r ($> 10a_0$ in case of H_2). Therefore, our choice was to use EMO. As shown below, our line list is truncated at $40\,000\text{ cm}^{-1}$, and thus does not come close to the long range of the NO PEC.

The *ab initio* PEC and SOC were fitted to the experimental line positions of $^{14}\text{N}^{16}\text{O}$ available in the literature combined with the experimentally derived energies generated by MARVEL. From our experience, a combination of line positions and energy levels provides a more stable fit. A total of nine potential expansion parameters (B_0, \dots, B_8) was required in order to obtain an optimal fit. The addition of any more parameters did not improve the fit significantly. In the case of the SOC refinement, an inverted EMO function is used (Fig. 1) and required only four expansion parameters (B_0, \dots, B_3) to achieve a satisfactory fit.

The experimental value D_0 is $52\,400 \pm 10\text{ cm}^{-1}$ estimated by Callear & Pilling (1970) using fluorescence experiments and from Ackermann & Miescher (1969). We decided to refine the dissociation energy (D_e) and not to constrain it to the experimental value of Callear & Pilling (1970). Varying D_e parameter led to a more compact form of $\beta_{\text{EMO}}(r)$ with $N = 6$ instead $N = 8$; fewer expansion parameters usually means a more stable extrapolation. In fact, Devvie & Peyerimhoff (1988) noted in their MRD-CI study the change of the dominant character of the reference electronic configurations in NO PEC at about 3 and 5 bohr (29 100 and 51 800 cm^{-1} , respectively), when approaching the dissociation $\text{N}(^4S) + \text{O}(^3P)$ (from $\pi^4\pi^*$ to $\sigma\pi^3\pi_x^*\pi_y^*\sigma^*$). That is, it is difficult to obtain a reliable connection between the equilibrium and experimental D_0 without sampling the highly vibrationally excited states ($v > 48$) experimentally in the fit. Due to the lack of these data and because the dissociation region was not our priority, we decided to adopt the

Table 3. Parameters for the refined PECs and SOCs, modelled using the EMO function, see equation (1).

Parameter	Potential energy curve	Spin-orbit curve
V_e (cm^{-1})	0	61.793 456 406 12
D_e (cm^{-1})	52 495.307 750 971	26.977 570 670 68
r_e (Å)	1.150 786 315 1853	1.2
p	4	4
N_l^a	2	1
N_r^a	8	4
B_0	2.765 732 762 123 20	1.378 287 151 9399
B_1	0.177 399 628 680 01	0.241 635 314 6388
B_2	0.129 966 585 645 91	−2.468 288 846 2767
B_3	1.817 477 680 304 30	5.516 106 647 1770
B_4	−9.767 860 824 393 20	
B_5	32.552 617 956 793 00	
B_6	−57.640 022 462 208 00	
B_7	55.246 373 834 427 00	
B_8	−21.231 743 969 255 00	

^aThe upper bound parameter N in equation (2) is defined as $N = N_l$ for $r \leq r_e$ and $N = N_r$ for $r > r_e$.

Table 4. Parameters for the refined spin-rotation and Λ -doubling expressions, modelled using the Šurkus polynomial expansion, see equation (4).

Parameter	Spin-rotation	$\Lambda - [p + 2q]$
r_e (Å)	1.150 786 315 1853	1.150 786 315 1853
p	4	3
N	1	1
A_0	−0.004 731 777 744 3454	0.006 135 737 949 9906
A_1	−0.017 510 291 840 8170	−0.005 784 869 380 2985

refined D_e value. Our final SO-free D_0 is 51 608 (6.400 eV), which is 800 cm^{-1} away from the experiment. This should not affect the quality of our line list for the selected temperatures. The D_0 value is estimated using the refined value of $D_e = 52\,495.3\text{ cm}^{-1}$ (see Table 3) and the lowest energy relative to the PEC minimum V_e of $E_{J=0.5, \Omega=0.5, v=0} = 887.100\text{ cm}^{-1}$. Polak & Fiser (2004) reported a high-level *ab initio* level D_e value [MR-ACPF(TQ)] of $51\,140\text{ cm}^{-1}$ (6.340 eV).

The resulting EMO parameters, including the reference (equilibrium) bond length (r_e), dissociation energy (D_e), expansion (B_n) and p parameters are listed in Table 3. The *ab initio* PECs and SOCs are compared to the refined curves from DUO in Fig. 1. The *ab initio* PEC is in good agreement with the refined PEC, despite the very aggressive fit applied with a large number of B_n expansion parameters. The *ab initio* SOC was changed substantially by fitting, although the overall shape of the *ab initio* SOC is maintained in the refined curve, which is reassuring.

To account for spin-rotation and Λ -doubling effects, a polynomial expansion based on the Šurkus-variables was used:

$$V(r) = D_e + (1 - y_p^{\text{eq}}) \sum_{n \geq 0}^N A_n (y_p^{\text{eq}})^n, \quad (4)$$

where N and p are parameters, and A_n is an expansion parameter refined in DUO. Both the spin-rotation $\gamma(r)$ and Λ -doubling $[p + 2q](x)$ (see, for example Brown & Merer 1979) functions were fitted with two expansion parameters A_0 and A_1 . These are given in Table 4 along with the p and N parameters. Varying the Born–Oppenheimer

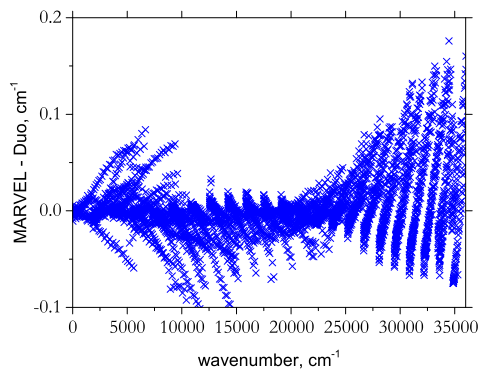


Figure 3. Observed – Calculated residuals of the final energy level fit, where the calculated values are the refined energies calculated by DUO and the observed values are the MARVEL energies and experimental frequencies.

breakdown corrections (Le Roy & Huang 2002) did not lead to a significant improvement, at least within the root mean squares achieved, and therefore were excluded from the fit. In fact, the effective interaction with other electronic states was partly recovered by inclusion of the Lambda-doubling and spin-rotation effective functions.

Experimental transition frequencies were introduced to the data set at the final stage of the fitting procedure in order to generate the most accurate set of parameters possible. The final residuals from fitting the DUO energy levels are plotted in Fig. 3. Notably, the largest residuals originate from energy levels with high J and v , in particular $J > 35.5$ and $v > 14$. Although some residuals have values ranging up to 0.13 cm^{-1} , 80.0 per cent of the fitted frequencies have Obs.–Calc. values of $\leq 0.02 \text{ cm}^{-1}$, yielding a root mean square (rms) of 0.015 cm^{-1} . Complete DUO input and output files are provided in the supplementary information that also include the fitted PEC and SOC.

2.4 SPFIT: determination of NO spectroscopic parameters

Rotational and rovibrational transitions for NO and its isotopologues were fitted simultaneously in order to determine an accurate set of spectroscopic parameters for the $X^2\Pi$ electronic ground state of NO. In an earlier study by Müller et al. (2015), only rotational and heterodyne infrared measurements of the main isotopic species were taken into account. Here, Dunham-type parameters along with some parameters describing the breakdown of the Born–Oppenheimer approximation (Watson 1973; Watson 1980) were determined for all isotopologues in one fit using the diatomic Hamiltonian outlined by Brown et al. (1979) that also provides isotopic dependences for the lowest order parameters required to fit a $^2\Pi$ diatomic radical. More details were given, for example, in a study of the BrO radical (Drouin et al. 2001).

Fitting and prediction of the spectra, here as well as previously, were carried out using programs SPFIT and SPCAT (Pickett 1991). These programs employ Hund’s case (b) quantum numbers throughout which are appropriate at higher rotational quantum numbers. Conversion of Hund’s case (b) quanta to case (a) or vice versa depends on the magnitude of the rotational energy relative to the magnitude of the spin–orbit splitting. For $2B(J - 0.5)(J + 0.5) < |A|$, levels with $J + 0.5 = N$ correlate with $^2\Pi_{1/2}$ and levels with $J - 0.5 = N$ correlate with $^2\Pi_{3/2}$; for larger values of J , the correlation is reversed. The reversal occurs between $J = 5.5$ and 6.5 in

the case of the NO isotopologues. Atomic masses were taken from the 2012 Atomic Mass Evaluation (Wang et al. 2012) which takes into account fairly recent mass determinations for ^{14}N (Thompson, Rainville & Pritchard 2004), ^{18}O (Redshaw, Mount & Myers 2009) and ^{17}O (Mount et al. 2010).

A large body of ground state rotational data involving almost all stable NO isotopologues was used in the previous work. The isotopic species are NO (Neumann 1970; Meerts & Dymanus 1972; Meerts 1976; Dale et al. 1977; Pickett et al. 1979; Lowe et al. 1981; Varberg et al. 1999), ^{15}NO (Meerts & Dymanus 1972; Saleck et al. 1991; Varberg et al. 1999), N^{18}O (Saleck et al. 1991; Müller et al. 2015) and N^{17}O and $^{15}\text{N}^{18}\text{O}$ (Saleck et al. 1994). $v = 1$ Λ -doubling transitions (Dale et al. 1977; Lowe et al. 1981) and $v = 1-0$ heterodyne infrared data (Hinz et al. 1986; Saube et al. 1996) for the main isotopic species were also included. The experimental uncertainties were critically evaluated; the reported uncertainties were employed in the fits in most cases. Frequency errors in spectroscopic measurements, possibly a consequence of misassignments, are not uncommon. Asvany et al. (2008) and Amano (2010) revealed frequency errors of $\sim 60 \text{ MHz}$ in the $J = 1-0$ transitions of H_2D^+ and CH^+ , respectively, from earlier measurements. These were obtained by new laboratory measurements. Frequency errors of $\sim 15 \text{ MHz}$ were found in two hyperfine structure lines of SH^+ by radio astronomical observations and spectroscopic fitting (Müller et al. 2014) and confirmed by more recent laboratory measurements (Halfen & Ziurys 2015). More subtle, because they are almost within the estimated uncertainties, were frequency errors in a large line list of the SO radical which were caused by the failure of a frequency standard (Klaus et al. 1996). In the present case, uncertainties were reduced (for a small number of lines) or increased (for a very small number of lines) if the reported uncertainties of a (sub) set of transition frequencies appeared to be judged too conservatively or too optimistically, respectively. If the reported uncertainties were deemed to be appropriate for the most part, but a few lines had rather large residuals in the fits (usually more than four times the uncertainties), these lines were omitted.

Extensive sets of Fourier transform infrared data from several sources were added to the line list in the present study. We used commonly the most accurate data in cases of multiple studies with essentially the same quantum number coverage.

The initial spectroscopic parameters (Müller et al. 2015) reproduced the NO $v = 1-0$ data of Spencer et al. (1994) well, and the spectroscopic parameters barely changed after the fit. We used the reported uncertainties in the fit and included the Λ -doubling as far as it had been resolved experimentally. Four lines, $Q(0.5)f$ and e of $^2\Pi_{1/2}$ and $R(11.5)$ and $R(19.5)$ of $^2\Pi_{3/2}$, however, showed residuals between five and almost 10 times the reported uncertainties. The remaining lines were reproduced within the experimental uncertainties both before and after adjustment of the spectroscopic parameters after these four lines were omitted from the fit. The uncertainties of some parameters were improved.

The NO $v = 1-0$ data of Coudert et al. (1995) had some overlap with the rovibrational data already in the fit. A trial fit suggested that these data were 0.00012 cm^{-1} too high, a considerable fraction of the reported uncertainties ranging from 0.00015 to 0.00022 cm^{-1} , with rather small scatter. All transition frequencies were reproduced very well after modifying the transition frequencies by 0.00012 cm^{-1} . The final rms error for these data was only slightly worse than 0.4, indicating a slightly conservative judgement of the adjusted data. This data set was the only one for which the line positions were adjusted. In all other data sets pertaining to

the main isotopic species, we did not find any clear evidence for possible calibration errors.

The $v = 2-1$ data of Mandin et al. (1997) were added next with their reported uncertainties. In no other instances were uncertainties specified; these were estimated to be reproduced within uncertainties, on average, in the final fits. In the case of a small number of lines in a data set with residuals much larger than most other lines, these lines were omitted, and the uncertainties were evaluated on the basis of the remaining lines. Uncertainties of 0.0002 and 0.0003 cm^{-1} were assumed for the $v = 2-0$ data of Dana et al. (1994) in the $^2\Pi_{1/2}$ and $^2\Pi_{3/2}$ spin ladder, respectively. We assumed an uncertainty of 0.0005 cm^{-1} for the $v = 1-0$ and $2-1$ data of Amiot et al. (1978).

The extensive $\Delta v = 2$ data of Amiot & Verges (1980) were included next, followed by the $v = 3-0$ data of Henry et al. (1978) and the $\Delta v = 3$ data of Amiot (1982). An additional constraint was a smooth trend from lower v to higher v for two extensive sets of data. Uncertainties were between 0.0005 cm^{-1} for $v = 2-0$ and a few more to 0.0024 cm^{-1} for $v = 15-13$ of Amiot & Verges (1980). We applied 0.0007 cm^{-1} for the data of Henry et al. (1978) and from 0.002 cm^{-1} for $v = 10-7$ and a few more to 0.004 cm^{-1} for $v = 22-19$ of Amiot (1982).

The quality of the $\Delta v = 2$ data of Hallin et al. (1979) up to $v = 6-4$ was questioned by Amiot & Verges (1980) because of the low resolution and the large deviations of the transition frequencies. The P -branch transition assignments in $v = 2-0$ are essentially complete up to $J = 65.5$ with additional assignments reaching $J = 77.5$. Transition frequencies up to $J = 64.5$ could be reproduced to 0.008 cm^{-1} , but the impact of these data on the spectroscopic parameter values and uncertainties was negligible. Higher J data were too sparse and showed very large residuals with some scatter that could not be reduced sufficiently with parameter values that were deemed reasonable. The higher v data from that work showed even larger scatter in the residuals, such that the data of Hallin et al. (1979) were omitted entirely.

Overtone spectra involving larger Δv involved transition frequencies too limited in J and in accuracy such that we did not consider these data.

Data for ^{15}NO and $^{15}\text{N}^{18}\text{O}$ were taken from Teffo et al. (1980); the uncertainties used for ^{15}NO were 0.0005, 0.0010 and 0.0015 cm^{-1} for $v = 1-0$, $2-0$ and $3-0$, respectively, and slightly lower for the two overtone bands of $^{15}\text{N}^{18}\text{O}$. Additional data for ^{15}NO , $v = 1-0$ and $2-1$, as well as the $v = 1-0$ bands of $^{15}\text{N}^{17}\text{O}$ and $^{15}\text{N}^{18}\text{O}$ were taken from Amiot & Guelachvili (1979) with uncertainties of 0.0003 cm^{-1} .

Our Hamiltonian for NO has been described earlier (Müller et al. 2015); however, in order to fit the FTIR data pertaining to the main isotopic species, we had to add several vibrational corrections to the mechanical and fine-structure parameters. These parameters were carefully chosen at each step of the fitting procedure by searching among the reasonable parameters for the one that reduces the rms error of the fit the most. A new parameter sometimes led to large changes in the value of one or more spectroscopic parameters. Such a parameter was kept in the fit only if additional transition frequencies did not lead to drastic changes in the value of this parameter. If two parameters led to similar reductions in the rms error and both together led to a much larger reduction than either one, both parameters were kept in the fit; the decision was postponed otherwise.

The isotopic FTIR data required Born–Oppenheimer breakdown parameters to the lowest order vibrational parameter (Y_{10}) to be added. Other Born–Oppenheimer breakdown parameters were

Table 5. Present and previous spectroscopic parameters^a (MHz) for NO determined from the isotopic invariant fit.

Parameter	Present	Previous
$U_{10}\mu^{-1/2} \times 10^{-3b}$	57 081.2389 (52)	56 240.216 66 (14)
$U_{10}\mu^{-1/2}\Delta_{10}^{\text{N}}m/M_{\text{N}}$	2104.2 (54)	
$U_{10}\mu^{-1/2}\Delta_{10}^{\text{O}}m_e/M_{\text{O}}$	573.6 (56)	
$Y_{20} \times 10^{-3}$	−422.325 96 (105)	
Y_{30}	293.06 (33)	
Y_{40}	−3.551 (49)	
Y_{50}	−0.3646 (37)	
$Y_{60} \times 10^3$	−3.264 (134)	
$Y_{70} \times 10^3$	−0.191 75 (192)	
$U_{01}\mu^{-1}$	51 119.4625 (41)	51 119.6807 (42)
$U_{01}\mu^{-1}\Delta_{01}^{\text{N}}m_e/M_{\text{N}}$	−4.5308 (29)	−4.4692 (29)
$U_{01}\mu^{-1}\Delta_{01}^{\text{O}}m_e/M_{\text{O}}$	−4.0820 (27)	−4.0272 (27)
Y_{11}	−525.8760 (20)	−526.7633 (22)
Y_{21}	−0.433 78 (145)	
$Y_{31} \times 10^3$	−4.92 (33)	
$Y_{41} \times 10^3$	−0.817 (35)	
$Y_{51} \times 10^6$	1.34 (170)	
$Y_{61} \times 10^6$	−1.323 (30)	
$U_{02}\mu^{-2} \times 10^3$	−163.9557 (23)	−163.9441 (30)
$U_{02}\mu^{-2}\Delta_{02}^{\text{N}}m_e/M_{\text{N}} \times 10^3$	0.0440 (23)	0.0447 (24)
$Y_{12} \times 10^3$	−0.451 88 (96)	−0.4842 (55)
$Y_{22} \times 10^6$	−15.24 (47)	
$Y_{32} \times 10^6$	0.696 (58)	
$Y_{42} \times 10^6$	−0.100 7 (20)	
$Y_{03} \times 10^9$	41.282 (182)	37.940 (114)
$Y_{13} \times 10^9$	−6.74 (28)	
$A_{00}^{\text{BO}} \times 10^{-3}$	3695.038 00 (69)	3695.104 22 (65)
$A_{00}^{\text{BO}}\Delta_{00}^{\text{A,N}}m_e/M_{\text{N}}$	186.24 (27)	204.98 (26)
$A_{00}^{\text{BO}}\Delta_{00}^{\text{A,O}}m_e/M_{\text{O}}$	151.30 (38)	167.83 (38)
A_{10}	−7069.06 (95)	−7335.247 (55)
A_{20}	−123.86 (62)	
A_{30}	−5.757 (105)	
$A_{40} \times 10^3$	52.0 (68)	
$A_{50} \times 10^3$	−11.084 (147)	
A_{01}	0.1248 (59)	0.1228 (59)
γ_{00}	−193.05 (21)	−193.40 (21)
γ_{10}	6.741 (46)	7.4763 (55)
γ_{20}	0.345 (30)	
$\gamma_{30} \times 10^3$	−7.3 (33)	
$\gamma_{40} \times 10^3$	1.512 (105)	
$\gamma_{01} \times 10^3$	1.5300 (133)	1.6110 (56)
$\gamma_{11} \times 10^3$	0.164 (24)	
$p_{00}^{\text{BO,eff}}$	350.623 39 (91)	350.623 40 (91)
$p_{00}^{\text{BO}}\Delta_{00}^{\text{p,N}}m_e/M_{\text{N}} \times 10^3$	−17.12 (93)	−17.11 (93)
$p_{10} \times 10^3$	−403.50 (32)	−403.50 (32)
$p_{01} \times 10^6$	34.1 (12)	34.1 (12)
q_{00}	2.844 718 (39)	2.844 711 (39)
$q_{10} \times 10^3$	−44.283 (65)	−44.282 (65)
$q_{01} \times 10^6$	42.313 (112)	42.319 (112)

^aNumbers in parentheses are 1σ uncertainties in units of the least significant figures. Previous parameter values from Müller et al. (2015). ^bPrevious value corresponds to an effective $Y_{10} \times 10^{-3}$.

barely determined, at best, and were omitted from the final fits. The final spectroscopic parameters are given in Tables 5 and 6, derived parameters are in Table 7, in both cases presented alongside data from the previous study (Müller et al. 2015). The reported uncertainties are only those from the respective fits; uncertainties of the atomic masses (Wang et al. 2012) (for the Δ s and for r_e), the mass of the electron in atomic mass units (for the Δ s), or of the

Table 6. Present and previous hyperfine parameters^a (MHz) for NO determined from the isotopic invariant fit.

Parameter	Present	Previous
$a_{00}(\text{N})$	84.3042 (106)	84.3042 (106)
$a_{10}(\text{N}) \times 10^3$	-202.3 (211)	-202.3 (211)
$b_{F,00}(\text{N})$	22.270 (21)	22.271 (21)
$b_{F,10}(\text{N}) \times 10^3$	250. (43)	249. (43)
$c_{00}(\text{N})$	-58.8904 (14)	-58.8904 (14)
$d_{00}(\text{N})$	112.619 48 (132)	112.619 47 (132)
$d_{10}(\text{N}) \times 10^3$	-30.3 (27)	-30.3 (27)
$d_{01}(\text{N}) \times 10^6$	105.6 (145)	105.6 (145)
$eQq_{1,00}(\text{N})$	-1.8986 (32)	-1.8986 (32)
$eQq_{1,10}(\text{N}) \times 10^3$	77.4 (64)	77.4 (64)
$eQq_{2,00}(\text{N})$	23.1126 (62)	23.1126 (62)
$eQq_{S,00}(\text{N}) \times 10^3$	-6.89 (83)	-6.89 (83)
$C_{I,00}(\text{N}) \times 10^3$	12.293 (27)	12.293 (27)
$C'_{I,00}(\text{N}) \times 10^3$	7.141 (123)	7.141 (123)
$a_{00}(\text{O})$	-173.0583 (101)	-173.0583 (101)
$b_{F,00}(\text{O})$	-35.458 (109)	-35.460 (109)
$c_{00}(\text{O})$	92.868 (171)	92.871 (171)
$d_{00}(\text{O})$	-206.1216 (70)	-206.1216 (70)
$eQq_{1,00}(\text{O})$	-1.331 (47)	-1.330 (47) ^b
$eQq_{2,00}(\text{O})$	-30.01 (163)	-30.02 (163)
$C_{I,00}(\text{O}) \times 10^3$	-32.7 (23)	-32.7 (23)

^aNumbers in parentheses are 1σ uncertainties in units of the least significant figures. Previous parameter values from Müller et al. (2015). ^bSmall error in value corrected.

Table 7. Derived parameters (MHz, pm, unitless)^a of NO from the isotopic invariant fit.

Parameter	Present	Previous
$Y_{10} \times 10^{-3}$	57 083.936 69 (89)	
Δ_{10}^{N}	0.9410 (24)	
Δ_{10}^{O}	0.3032 (29)	
Y_{01}	51 110.849 70 (68)	51 111.1842 (11)
Δ_{01}^{N}	-2.262 44 (146)	-2.231 66 (147)
Δ_{01}^{O}	-2.328 23 (156)	-2.296 99 (156)
B_e	51 110.888 44 (76)	
r_e	115.078 7929 (9)	
$Y_{02} \times 10^3$	-163.911 79 (49)	-163.8994 (27)
Δ_{02}^{N}	-6.84 (35)	-6.96 (37)
A_{00}	3695 375.54 (39)	3695 477.03 (21)
$\Delta_{00}^{\text{A,N}}$	1.2866 (18)	1.4160 (18)
$\Delta_{00}^{\text{A,O}}$	1.1939 (30)	1.3243 (30)
p_{00}	350.606 27 (17)	350.606 29 (17)
$\Delta_{00}^{\text{p,N}}$	-1.246 (68)	-1.246 (68)

^aNumbers in parentheses are 1σ uncertainties in units of the least significant figures. r_e in pm, Δ s unitless, all other parameters in MHz. Previous parameter values from Müller et al. (2015); empty fields indicate values have or could not be determined except for the previous effective Y_{10} value that was devoid of all vibrational corrections.

conversion factor from B_e to the moment of inertia, derived from Mohr, Taylor & Newell (2012) (see also Müller et al. (2013) for the conversion factor), are negligible here. The line, parameter and fit files will be available in the CDMS² (Müller et al. 2005). The comparison between present and previous spectroscopic parameters is frequently quite favourable. The addition of new parameters due

to new data can lead to changes outside the combined uncertainties; such changes can even be relatively large in cases in which a lower order parameter is comparatively small in magnitude with respect to the magnitude of a higher order parameter. An example for the latter case is A_{10} , examples for the former are the related changes in A_{00}^{BO} and its Born–Oppenheimer breakdown parameters.

Sensitive overtone measurements of NO isotopologues, similar to those carried out for CO $v = 3-0$ (Mondelain et al. 2015) and $v = 4-0$ (Campargue, Karlovets & Kassi 2015), are probably the most straightforward way to improve the NO spectroscopic parameters and predictions of rovibrational spectra, especially those of minor isotopic species.

Predictions based on the present set of spectroscopic parameters (generated with SPCAT) should be quite good up to J of around 60 or 70 for low values of v and for the main isotopic species, but considerable caution is advised beyond J of 90. The quality of the predictions is expected to deteriorate somewhat towards $v = 20$. The vibrational states $v = 20, 21$ and 22 are at the edge of the data set; predictions involving these states should be reasonable. Extrapolation in v should be viewed with more caution; data involving $v = 25$ may be reasonable. By comparing to the corresponding DUO values, which were obtained from an independent fit, the prediction error of these two methods should be within 0.07 cm^{-1} for $v = 25$ and not exceed 1 cm^{-1} for $v = 27$. Using the same argument for rotational excitations, we find that the difference between the $J = 99.5$ energies obtained with two methods grow from 0.1 cm^{-1} ($v = 0$, $\tilde{E} = 16\,300 \text{ cm}^{-1}$) to 9.5 cm^{-1} ($v = 20$, $\tilde{E} = 41\,300 \text{ cm}^{-1}$) and then to 96 cm^{-1} ($v = 27$, $\tilde{E} = 51\,500 \text{ cm}^{-1}$). These differences give an indication of both the SPCAT and DUO extrapolation errors at high v and J .

On the basis of the available data, we expect predictions for ¹⁵NO to be slightly less reliable, and those of isotopologues involving ¹⁸O or ¹⁷O somewhat less reliable still at low values of v . Moreover, predictions involving $v = 5$ and higher should be viewed with considerable caution.

2.5 DUO: LINE LIST

2.5.1 Line list calculations

The line list computed in DUO comprises two files (Tennyson et al. 2016c); the `.states` file contains the running number, line position (cm^{-1} , i.e. energy term value), total statistical weight and associated quantum numbers. The `.states` file also includes lifetimes for each state and Landé g -factors. The `.trans` file contains the upper and lower level running number, *Einstein-A* coefficients (s^{-1}) and transition wavenumber (cm^{-1}). The *Einstein-A* coefficient is the rate of spontaneous emission between the upper and lower energy levels.

The NO ground electronic state line list was computed with DUO using the nuclear statistical weights $g_{\text{ns}} = (2I_{\text{N}} + 1)(2I_{\text{O}} + 1)$, where I_{N} and I_{O} are the nuclear spins of the nitrogen (1 for ¹⁴N and 1/2 for ¹⁵N) and oxygen (0 for ¹⁶O and ¹⁸O and 5/2 for ¹⁷O) atoms, respectively.

The complete ¹⁴N¹⁶O line list contains 21 688 states and 2281 042 transitions in the wavenumber range 0–40 000 cm^{-1} , extending to a maximum rotational quantum number of 184.5 and a maximum vibrational quantum number of 51; an extract of the `.states` and `.trans` files are shown in Tables 8 and 9, respectively.

Line lists for the six combinations of ¹⁴N, ¹⁵N, ¹⁶O, ¹⁷O and ¹⁸O were computed, without any adjustments to the fit; only the masses were altered to the values specified above.

² <http://www.astro.uni-koeln.de/site/vorhersagen/pickett/beispiele/NO/>

Table 8. Extract from the states file of the $^{14}\text{N}^{16}\text{O}$ line list.

i	Energy (cm $^{-1}$)	g_i	J	τ	g_J	Parity	e/f	State	v	Λ	Σ	Ω	emp/calc
1	0.000 000	6	0.5	inf	−0.000 767	+	e	X1/2	0	1	−0.5	0.5	e
2	1876.076 228	6	0.5	8.31E-02	−0.000 767	+	e	X1/2	1	1	−0.5	0.5	e
3	3724.066 346	6	0.5	4.25E-02	−0.000 767	+	e	X1/2	2	1	−0.5	0.5	e
4	5544.020 643	6	0.5	2.89E-02	−0.000 767	+	e	X1/2	3	1	−0.5	0.5	e
5	7335.982 597	6	0.5	2.22E-02	−0.000 767	+	e	X1/2	4	1	−0.5	0.5	e
6	9099.987 046	6	0.5	1.81E-02	−0.000 767	+	e	X1/2	5	1	−0.5	0.5	e
7	10 836.058 173	6	0.5	1.54E-02	−0.000 767	+	e	X1/2	6	1	−0.5	0.5	e
8	12 544.207 270	6	0.5	1.35E-02	−0.000 767	+	e	X1/2	7	1	−0.5	0.5	e
9	14 224.430 238	6	0.5	1.21E-02	−0.000 767	+	e	X1/2	8	1	−0.5	0.5	e
10	15 876.704 811	6	0.5	1.10E-02	−0.000 767	+	e	X1/2	9	1	−0.5	0.5	e
11	17 500.987 446	6	0.5	1.01E-02	−0.000 767	+	e	X1/2	10	1	−0.5	0.5	e
12	19 097.209 871	6	0.5	9.41E-03	−0.000 767	+	e	X1/2	11	1	−0.5	0.5	e
13	20 665.275 246	6	0.5	8.83E-03	−0.000 767	+	e	X1/2	12	1	−0.5	0.5	e
14	22 205.053 904	6	0.5	8.35E-03	−0.000 767	+	e	X1/2	13	1	−0.5	0.5	e
15	23 716.378 643	6	0.5	7.94E-03	−0.000 767	+	e	X1/2	14	1	−0.5	0.5	e
16	25 199.039 545	6	0.5	7.59E-03	−0.000 767	+	e	X1/2	15	1	−0.5	0.5	e
17	26 652.778 266	6	0.5	7.30E-03	−0.000 767	+	e	X1/2	16	1	−0.5	0.5	e
18	28 077.281 796	6	0.5	7.05E-03	−0.000 767	+	e	X1/2	17	1	−0.5	0.5	e
19	29 472.175 632	6	0.5	6.84E-03	−0.000 767	+	e	X1/2	18	1	−0.5	0.5	e
20	30 837.016 339	6	0.5	6.66E-03	−0.000 767	+	e	X1/2	19	1	−0.5	0.5	e
21	32 171.283 479	6	0.5	6.50E-03	−0.000 767	+	e	X1/2	20	1	−0.5	0.5	e
22	33 474.370 850	6	0.5	6.38E-03	−0.000 767	+	e	X1/2	21	1	−0.5	0.5	e
23	34 745.577 033	6	0.5	6.27E-03	−0.000 767	+	e	X1/2	22	1	−0.5	0.5	e
24	35 984.095 189	6	0.5	6.19E-03	−0.000 767	+	e	X1/2	23	1	−0.5	0.5	e
25	37 189.002 091	6	0.5	6.13E-03	−0.000 767	+	e	X1/2	24	1	−0.5	0.5	e
26	38 359.246 347	6	0.5	6.09E-03	−0.000 767	+	e	X1/2	25	1	−0.5	0.5	e
27	39 493.635 791	6	0.5	6.07E-03	−0.000 767	+	e	X1/2	26	1	−0.5	0.5	e

i : State counting number.

\bar{E} : State energy in cm $^{-1}$.

g_i : Total statistical weight, equal to $g_{\text{ns}}(2J + 1)$.

J : Total angular momentum.

τ : Lifetime (s $^{-1}$).

g_J : Landé g -factor

+ / −: Total parity.

e/f : Rotationless parity.

State: Electronic state.

v : State vibrational quantum number.

Λ : Projection of the electronic angular momentum.

Σ : Projection of the electronic spin.

Ω : $\Omega = \Lambda + \Sigma$, projection of the total angular momentum.

emp/calc: e=empirical (SPCAT), c=calculated (Duo).

In order to avoid the numerical noise associated with the small dipole moment matrix elements (Li et al. 2015), we followed the suggestion of Medvedev et al. (2016) and represented the *ab initio* dipole moment using an analytical function. To this end, the following Padé form due to Goodisman (1963) was used:

$$\mu(r) = \frac{z^3}{1+z^7} \sum_{i \geq 0} a_i T_i \left(\frac{z-1}{z+1} \right), \quad (5)$$

where $z = r/r_e$, $T_i(x)$ are Chebyshev polynomials and a_i are expansion parameters obtained by fitting to 352 *ab initio* dipole moment values covering $r = 0.7\text{--}9 \text{ \AA}$. With 18 parameters, we were able to reproduce the *ab initio* dipole with an rms error of 0.07 D for the whole range, with best agreement in the vicinity of the equilibrium of the order of $10^{-5}\text{--}10^{-6}$ D. The vibrational transition moments computed using the quintic splines interpolation implemented as default in DUO and this Padé expression are shown in Fig. 4, where they are also compared to the empirical values, see Lee et al. (2006) and references therein, where available. They are also listed in Table 10. The spline-interpolated dipoles produce an artificial plateau-like er-

ror of $10^{-6}\text{--}10^{-7}$ D as expected (Li et al. 2015). The analytical form improves this by shifting the error to $10^{-10}\text{--}10^{-11}$ D. However, the transition dipole moment values appear to be very sensitive to such functional interpolation, at least within $10^{-5}\text{--}10^{-6}$ D, which is also the absolute error of our interpolation scheme. To illustrate this, Fig. 4 also shows vibrational transition dipole moments, computed using fits with different expansion orders, ranges, weightings of the data, etc. From all these combinations, we then selected the set that gives the closest agreement with the transition dipole moments obtained using the spline-interpolation scheme. This set is also in the best agreement with the empirical transition dipole moments.

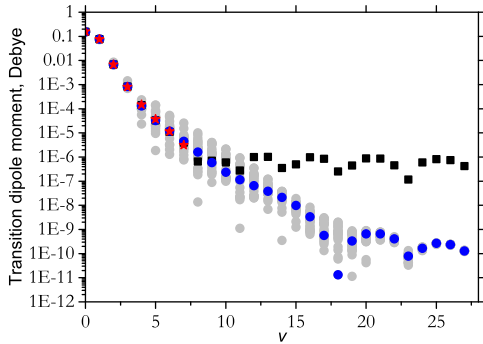
In intensity (line list) calculations, we used a dipole threshold of 1×10^{-9} D, i.e. all vibrational matrix elements smaller than this value were set to zero to avoid artificial intensities due to the numerical error.

Our final DUO input, which defines our final PEC, SOC and DMC as well as other input parameters selected, is given in the supplementary data.

Table 9. Extract from the transitions file of the $^{14}\text{N}^{16}\text{O}$ line list.

f	i	A_{fi} (s^{-1})	$\tilde{\nu}_{fi}$
14 123	13 911	1.5571E-02	10159.167959
13 337	13 249	5.9470E-06	10159.170833
1483	1366	3.7119E-03	10159.177466
9072	8970	1.1716E-04	10159.177993
1380	1469	3.7119E-03	10159.178293
14 057	13 977	1.5571E-02	10159.179386
10 432	10 498	4.5779E-07	10159.187818
12 465	12 523	5.4828E-03	10159.216008
20 269	20 286	1.2448E-10	10159.227463
12 393	12 595	5.4828E-03	10159.231009
2033	2111	6.4408E-04	10159.266541
17 073	17 216	4.0630E-03	10159.283484
5808	6085	3.0844E-02	10159.298459
5905	5988	3.0844E-02	10159.302195
13 926	13 845	1.5597E-02	10159.312986

f : Upper state counting number;
 i : Lower state counting number;
 A_{fi} : Einstein-A coefficient in s^{-1} ;
 $\tilde{\nu}_{fi}$: transition wavenumber in cm^{-1} .

**Figure 4.** Vibrational transition dipole moments (D) from the $v = 0$ ground state of $^{14}\text{N}^{16}\text{O}$: empirical (Lee et al. 2006, stars) and *ab initio* calculated using the quintic splines (squares) and Padé-type expansion (circles).

2.5.2 Hybrid line list

The final lists were produced by combining the SPCAT frequencies and DUO Einstein coefficients. To this end, we used the advantage

of the two-file structure of the ExoMol format (Tennyson et al. 2016c), with .states and .trans files. We simply replaced the DUO energies in the states file with the corresponding SPCAT values. The corresponding coverage of SPCAT and DUO is summarized in Table 13. The correlation based on the Hund's case (a) quantum numbers (J , v , Ω and parity) was straightforward. The DUO energies extend significantly beyond the SPCAT data range. In order to prevent possible jumps and discontinuities when switching between these data sets, the DUO energies were shifted to match the SPCAT energies at the points of the switch. For example, in case of $^{14}\text{N}^{16}\text{O}$, the maximum vibrational excitation considered by SPCAT v_{max} is 29 (the switching point), therefore all DUO energies for $v = 29 \dots 51$ were shifted such that DUO $v = 29$ energy value coincides with those by SPCAT for all J s. The same strategy was used to stitch the SPCAT and DUO energies at $J = 99.5$ (the chosen threshold for SPCAT); the DUO values for $J = 99.5 \dots 185.5$ were shifted to match the corresponding $J = 99.5$ value of SPCAT for each v , Ω and parity individually.

The SPCAT energies of the isotopologues are even more limited in terms of the vibrational coverage; $v_{\text{max}} = 9$ ($^{15}\text{N}^{16}\text{O}$ and $^{14}\text{N}^{18}\text{O}$) and 4 ($^{14}\text{N}^{17}\text{O}$, $^{15}\text{N}^{17}\text{O}$ and $^{15}\text{N}^{18}\text{O}$). As for the main isotopologue, we used the corresponding DUO energies to top-up the corresponding line list to the same thresholds as for $^{14}\text{N}^{16}\text{O}$. The better representation of the data from the parent isotopologue helped us to improve the accuracy of the DUO prediction for $v \leq 29$. By comparing the SPCAT and DUO energies of $^{14}\text{N}^{16}\text{O}$ in this range, the corresponding residuals were propagated (for each rovibronic state individually) to correct the corresponding DUO energies for the other five isotopologues (see, e.g. Polyansky et al. 2016). The energies for $v \geq v_{\text{max}}$ were then given by

$$E_{J,\pm,v,\Omega}^{\text{iso}} = E_{J,\pm,v,\Omega}^{\text{Duo-iso}} + E_{J,\pm,v,\Omega}^{\text{SPCAT-parent}} - E_{J,\pm,v,\Omega}^{\text{Duo-parent}},$$

where ‘Duo-iso’ refers to the DUO energies of one of the five isotopologues for a given set of J , \pm , v and Ω , while ‘Duo-parent’ and ‘SPCAT-parent’ indicate the corresponding energies of the parent isotopologue computed by DUO and SPCAT, respectively. The line lists do not include the hyperfine structure of the energy levels and transitions.

Table 10. Transition dipole moments of NO. The total uncertainties are given in parenthesis. The *ab initio* values are obtained using the *ab initio* DMC interpolated with the quintic splines and Padé expression as in equation (5).

Band	‘Exp’	Ref.	Splines	Padé
0–0	0.1595 (15)	Amiot (1982)	0.155	0.155
1–0	$10^{-2} \times 7.6931$ (14)	Coudert et al. (1995)	7.649	7.646
2–0	$10^{-3} \times 6.78$ (20)	Mandin et al. (1997)	6.865	6.890
3–0	$10^{-4} \times 7.975$ (23)	Lee et al. (2006)	8.372	8.379
4–0	$10^{-4} \times 1.4804$ (45)	Lee et al. (2006)	1.396	1.300
5–0	$10^{-5} \times 3.683$ (17)	Lee et al. (2006)	3.319	3.244
6–0	$10^{-5} \times 1.136$ (06)	Lee et al. (2006)	1.100	1.182
7–0	$10^{-6} \times 3.09$ (47)	Bood et al. (2006)	3.959	4.458
3–1	$10^{-2} \times 1.19$ (12)	Mandin et al. (1998)		1.194
2–1	0.109 (38)	Dana et al. (1994)		0.108
7–6	$10^{-1} \times 1.89$ (11)	Drabbels & Wodtke (1997)		1.965
21–20	$10^{-1} \times 3.176$ (82)	Drabbels & Wodtke (1997)		3.015
21–19	$10^{-1} \times 1.077$ (27)	Drabbels & Wodtke (1997)		1.047
21–18	$10^{-2} \times 3.68$ (16)	Drabbels & Wodtke (1997)		3.220
21–17	$10^{-2} \times 1.09$ (16)	Drabbels & Wodtke (1997)		1.239

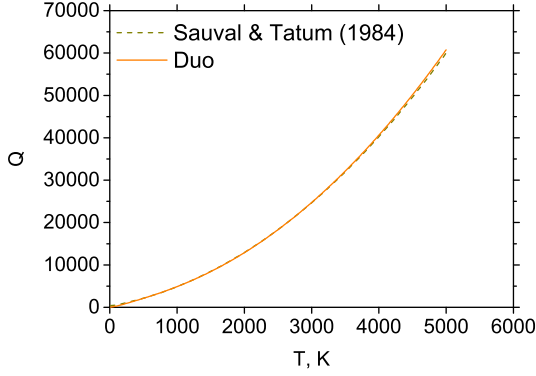


Figure 5. Comparison of the calculated partition function (solid line) and that modelled by Sauval & Tatum (1984, dashed line) up to 5000 K.

Table 11. Partition functions of NO: HITRAN values (TIPS; Gamache et al. 2000, provided only between 70 and 3000 K) obtained using parameters from Sauval & Tatum (1984) and DUO values.

T (K)	HITRAN	Sauval & Tatum	DUO
70	189.75	492.80	193.53
100	293.36	585.91	296.51
300	1160.75	1296.85	1159.66
1000	4877.73	4874.19	4877.53
1500	8403.66	8470.16	8424.34
2000	12 812.56	12 951.71	12 887.04
2500	18 135.16	18 343.44	18 311.46
3000	24 382.24	24 673.57	24 726.00
4000		40 270.57	40 622.12
5000		59 994.10	60 769.42

3 RESULTS

3.1 Partition function

The partition function is given by

$$Q(T) = g_{\text{ns}} \sum_{i=0}^n (2J_i + 1) \exp\left(\frac{-c_2 \tilde{E}_i}{T}\right), \quad (6)$$

\tilde{E}_i is the energy term value (cm^{-1}); c_2 is the second radiation constant (K cm); and g_{ns} is the nuclear statistical weight. This was calculated from the new line list using the in-house program EXOCROSS (Yurchenko 2017) up to a temperature of 5000 K in increments of 1 K. Tabulations of this form are given in the supplementary material for all six of the isotopologues considered.

The computed partition function compares well to the values by Sauval & Tatum (1984), above their lower temperature limit of 1000 K, as shown in Fig. 5. Slight disagreement at higher temperatures may be due to the fact that only the ground electronic state of NO has been considered in the DUO calculations, since excited states will have a larger contribution at high temperatures. Looking at the log-plot comparison, disagreement below $\log(T) = 3.0$ corresponds to temperatures lower than 1000 K, for which the Sauval and Tatum model is not valid (see also Table 11, where the partition functions for temperatures are compared).

The partition function was also represented using the following functional form (Vidler & Tennyson 2000)

$$\log_{10} Q(T) = \sum_{n=0}^{10} a_n (\log_{10} T)^n. \quad (7)$$

Table 12. Expansion coefficients for the partition function of $^{14}\text{N}^{16}\text{O}$ given by equation (7). Parameters for other isotopologues can be found in the supplementary material.

Expansion coefficient	
a_0	1.076 140 9513
a_1	-0.168 197 2157
a_2	1.581 096 4843
a_3	-4.566 269 7659
a_4	9.492 028 9544
a_5	-10.949 175 7465
a_6	7.375 619 0305
a_7	-2.982 963 0362
a_8	0.713 193 7052
a_9	-0.092 896 0661
a_{10}	0.005 082 1171

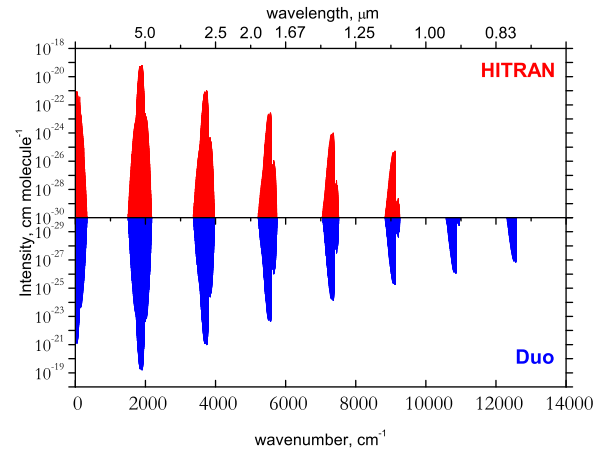


Figure 6. Log-scale comparison of absorption intensities (cm molecule^{-1}) at $T = 296$ K of the HITRAN data base (Rothman et al. 2013, red) and this work (blue). Each intensity ‘column’ represents a vibrational band.

This expression was used to least-squares fit 11 expansion coefficients, a_0, \dots, a_{10} , to the DUO partition function. An example of expansion parameters for $^{14}\text{N}^{16}\text{O}$ are presented in Table 12. These parameters reproduce the temperature dependence of partition function of NO within 0.3 per cent for most of the data, however it increases to just 0.4 per cent at $T = 4000$ K and 1.1 per cent at $T = 5000$ K. This is still a very small error, and thus the fit can be said to reliably reproduce the partition function. Expansion parameters for all six species are included into the supplementary material.

3.2 Intensities

The absorption line intensities were obtained using (Bernath 2005)

$$I = \frac{1}{8\pi c \tilde{\nu}^2} \frac{g_{\text{ns}}(2J'+1)}{Q(T)} A_{if} \exp\left(\frac{-c_2 \tilde{E}''}{T}\right) \left[1 - \exp\left(\frac{c_2 \tilde{\nu}}{T}\right)\right], \quad (8)$$

where I is the line intensity (cm molecule^{-1}), c is the speed of light (cm s^{-1}), $Q(T)$ is the partition function, \tilde{E}'' is the lower state term value, c_2 is the second radiation constant (K cm) and g_{ns} is the nuclear statistical weight.

Absorption intensities were calculated using EXOCROSS and the lines are presented as stick spectra. Fig. 6 compares the computed

Table 13. A summary of the ExoMol isotopologue line lists (number of lines and states) and summary of the SPCAT data (number of states and v_{\max}). $J_{\max} = 185.5$ (ExoMol) and $J_{\max} = 99.5$ (SPCAT). v_{\max} (ExoMol) = 51. ‘Abund’ refers to terrestrial isotopic abundances. N_{296} gives the number of NO transitions in our line lists at 296 K after applying the HITRAN intensity cut-off. $N_{\text{Trans.}}$ are the corresponding numbers of lines in HITRAN 2012 (Rothman et al. 2013, neglecting hyperfine structure).

Isotopologue	Abund	N_{States}	ExoMol		SPCAT		HITRAN	
			$N_{\text{Trans.}}$	N_{296}	N_{States}	v_{\max}	N_{296}	$N_{\text{Trans.}}$
$^{14}\text{N}^{16}\text{O}$	0.995	21 688	2281 042	8274	11 940	29	93 622	6369
$^{14}\text{N}^{17}\text{O}$	0.000 379	22 292	2378 578	3067	1990	4		
$^{14}\text{N}^{18}\text{O}$	0.002 05	22 848	2471 705	3853	3980	9	679	679
$^{15}\text{N}^{16}\text{O}$	0.003 63	22 466	2408 920	4233	3980	9	699	699
$^{15}\text{N}^{17}\text{O}$	0.000 001 38	23 106	2516 634	1290	1990	4		
$^{15}\text{N}^{18}\text{O}$	0.000 007 46	23 698	2619 513	1790	1990	4		

absorption intensities to intensities from HITRAN at 296 K (Rothman et al. 2013) up to a wavenumber of 15 000 cm^{-1} . It can be seen that the absorption intensities calculated in this work are in excellent agreement with those of the HITRAN data base, as they are of the same strength and wavenumber; this work is more comprehensive, as absorption intensities are calculated up to 40 000 cm^{-1} whilst the HITRAN data base employs a cut-off wavenumber of approximately 10 000 cm^{-1} . It should be noted that the HITRAN data is reasonably complete at $T = 296$ K for $^{14}\text{N}^{16}\text{O}$, but not for other isotopologues (see Table 13). HITRAN also contains a huge number of extremely weak (at 296 K) transitions (down to 10^{-95} cm molecule^{-1}). Many of the strong lines are with the hyperfine structure resolved. After excluding the weak lines (using the HITRAN cut-off algorithm; Rothman et al. 2013) and averaging over the hyperfine components, we have obtained about 6400 transitions ($T = 296$ K). This can be compared to 8274 lines in our $^{14}\text{N}^{16}\text{O}$ line list at 296 K (using the same HITRAN cut-off). This and other comparisons are summarized in Table 13.

Comparison of band structure is presented in Fig. 7, again comparing this work to the HITRAN data base. The pure rotational band is present in the far-infrared region, the fundamental band is the mid-infrared region and the first and second vibrational overtones are present in the near-infrared region. Branch structure is visible, with the extent of the *P*-branch increasing with each successive overtone, whilst the *R*-branch becomes more dense, as expected (Hollas 2004). The fundamental band is the strongest, while the band intensity decreases with each successive overtone as expected.

3.2.1 Isotopologue intensity comparison

For comparison purposes, intensities were calculated using the same procedure for the $^{15}\text{N}^{18}\text{O}$ isotopologue; the fundamental vibrational band is compared to the same region of the NO spectrum in Fig. 8. Since the reduced mass μ is less for the $^{15}\text{N}^{18}\text{O}$ isotopologue, it follows that the vibrational frequency and band origin is decreased. As a consequence, the absorption intensities are slightly weaker, since the *Einstein A* coefficients are proportional to the wavenumber cubed. This can be seen in Fig. 8, as the $^{15}\text{N}^{18}\text{O}$ band is shifted to a lower wavenumber, and intensities are slightly weakened.

3.3 Cross-sections

Fig. 9 shows absorption cross-sections computed at temperatures of 300, 500, 1000, 2000 and 3000 K using EXOCROSS for the wavelength range up to 0.2 μm . A Gaussian line profile was specified, with a half width at half-maximum (HWHM) of 1 cm^{-1} . The intensities drop with the wavenumber (overtones) exponentially as

they should (Li et al. 2015) up to 40 000 cm^{-1} (the upper bound in our line lists), after that plateau-like structures start forming at very small intensities ($<10^{-40}$ cm molecule^{-1}). The latter indicates the artefacts in our dipole at very high vibrational excitations. Transitions with wavelength less than 0.25 μm , indicated by the shaded area in equation (9), are not included in the NO line lists.

Absorption cross-sections of $^{14}\text{N}^{16}\text{O}$ with a Doppler profile were computed from the HITEMP data base for $T = 3000$ K, in the range 0–14 000 cm^{-1} and compared to cross-sections generated using the $^{14}\text{N}^{16}\text{O}$ ExoMol line list, see Fig. 10. There is a good general agreement in strength and wavenumber between the two spectra. Again, it should be noted that this work is more extensive, as the HITEMP data base employs a cut-off wavenumber of approximately 10 000 cm^{-1} , as does the HITRAN data base.

3.4 Radiative lifetimes

The radiative lifetime of an excited state, τ_i , can be computed in a straightforward manner from the state and transition files (Tennyson et al. 2016a) by

$$\tau_i = \frac{1}{\sum_{f<i} A_{if}}, \quad (9)$$

where A_{if} is the *Einstein A* coefficient, and i and f indicate the initial and final states, respectively. Lifetimes were calculated by the program EXOCROSS. The computed lifetimes are plotted in Fig. 11 as a function of wavenumber (cm^{-1}); lifetimes for all states are plotted in grey, whilst lifetimes for the $v = 0-3$ states are highlighted by coloured triangles. Lifetimes for states for which all downwards transitions are considered are given as part of the enhanced ExoMol states file (Tennyson et al. 2016c) as illustrated in Table 8.

4 DISCUSSION AND CONCLUSION

The line list called NO_{NAME} for the ground state of the NO isotopologue $^{14}\text{N}^{16}\text{O}$ was constructed using a hybrid (variational/effective Hamiltonian) scheme. The line list contains 21 688 states and 2409 810 transitions in the wavenumber range 0–40 000 cm^{-1} , extending to maximum quantum numbers $J = 184.5$ and $v = 51$. Line lists were also constructed for the five isotopologues: $^{14}\text{N}^{17}\text{O}$, $^{14}\text{N}^{18}\text{O}$, $^{15}\text{N}^{16}\text{O}$, $^{15}\text{N}^{17}\text{O}$ and $^{15}\text{N}^{18}\text{O}$ in the same range and containing similar numbers of states and transitions.

Initial energy levels in the line lists were calculated by a fit of *ab initio* results using experimental energies. Refinement of the energy levels returned an rms of 0.015 cm^{-1} , which corresponds to a fit that is accurate to 0.02 cm^{-1} for 80 per cent of the data, whilst

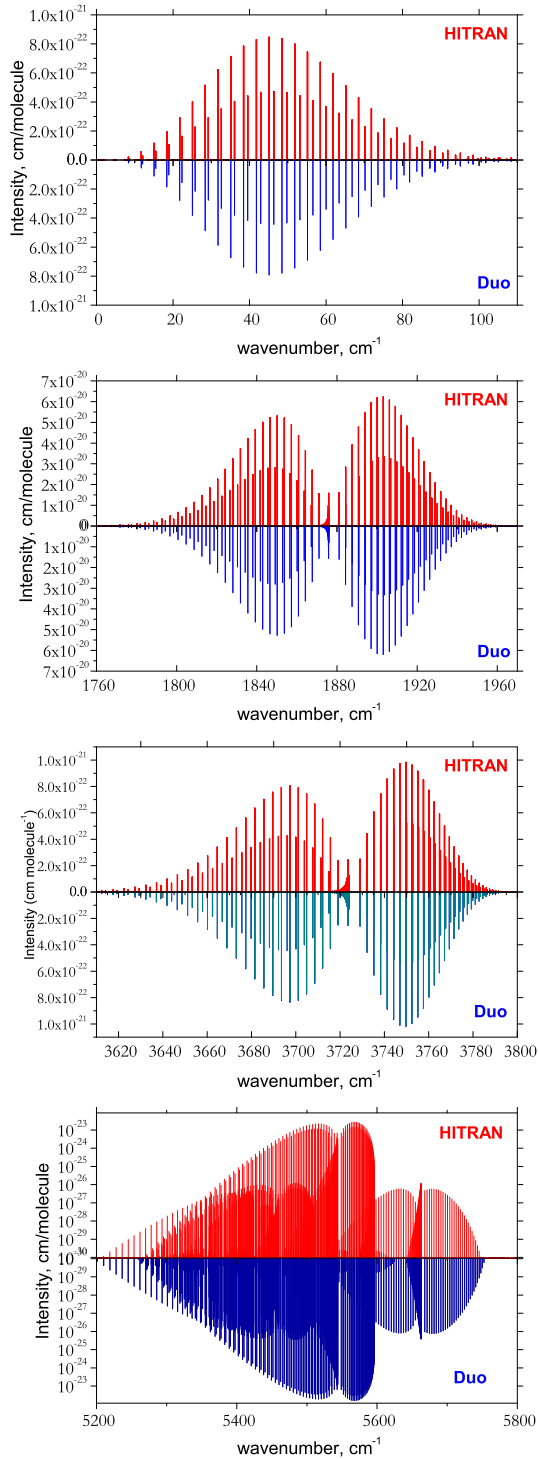


Figure 7. Stick spectra comparison of HITRAN absorption intensities (cm molecule^{-1} , red) and absorption intensities calculated in this work (blue), at a temperature of 296 K: pure rotational band, fundamental vibrational band, first vibrational overtone band and second vibrational overtone band. Intensity strength and wavenumber positions are in excellent agreement.

the worst residual is 0.13 cm^{-1} . These were then replaced by semi-empirical energies, where available. The accuracy of the energy levels propagates through to the computed line lists; comparison of intensities from this work and the HITRAN (Rothman et al. 2013) data base for the $^{14}\text{N}^{16}\text{O}$ isotopologue at 296 K show excellent

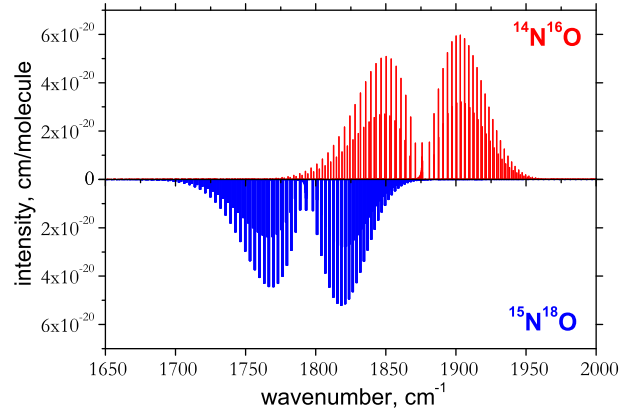


Figure 8. Stick spectrum comparison of the $^{15}\text{N}^{18}\text{O}$ fundamental vibrational band (red) and the $^{14}\text{N}^{16}\text{O}$ fundamental vibrational band (blue) in the $5.3 \mu\text{m}$ region at 296 K. Note that the $^{15}\text{N}^{18}\text{O}$ band is shifted to lower wavenumbers, and intensities are slightly weakened.

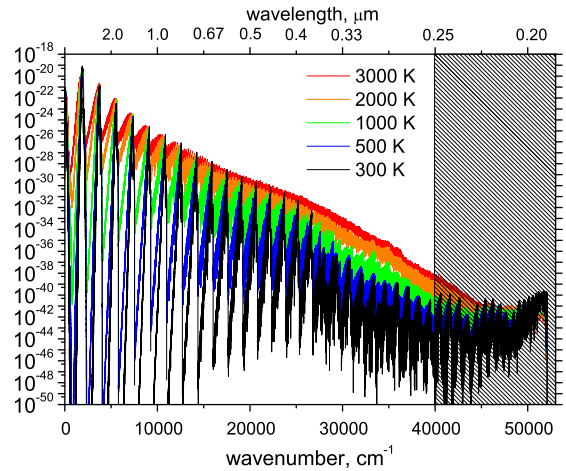


Figure 9. Absorption spectrum of the ground state of $^{14}\text{N}^{16}\text{O}$ as a function of temperature. The temperatures considered are 300 (bottom), 500, 1000, 2000 and 3000 K (top). Cross-sections are calculated with a Gaussian profile and $\text{HWHM} = 1 \text{ cm}^{-1}$. The higher temperature profiles will be useful in characterizing the spectra of terrestrial exoplanets and brown dwarfs.

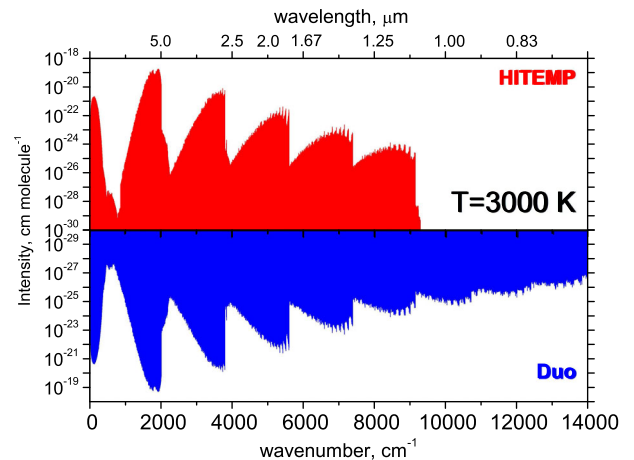


Figure 10. Comparison of absorption cross-sections ($\text{cm}^2 \text{ molecule}^{-1}$) with a Doppler line profile at 3000 K of the HITEMP data base (Rothman et al. 2010, red) and this work (blue).

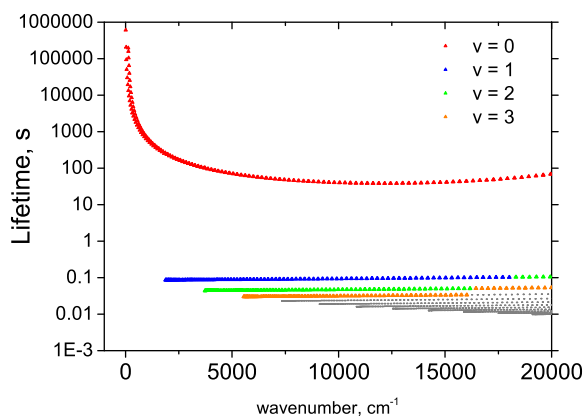


Figure 11. A log-plot of $^{14}\text{N}^{16}\text{O}$ radiative lifetimes against state energy. Lifetimes for states with $v = 0-3$ are indicated by triangles while lifetimes for higher vibrational states are indicated by circles.

agreement both in strength and position of lines. Because most of the DUO energies were replaced with the semi-empirical ones, the fit was mostly done to improve the accuracy of intensities via better quality of the corresponding wavefunctions. Only highly excited states ($J > 100.5$ and $v > 29$ for $^{14}\text{N}^{16}\text{O}$) were taken from the DUO calculations, shifted at the stitching points to avoid discontinuities. Thus, our $^{14}\text{N}^{16}\text{O}$ line positions can be considered of experimental accuracy for $v \leq 22$, which is then expected to degrade gradually when extrapolated to $v = 22 \dots 51$. The difference between SPCAT and DUO at $v = 29$ (the stitching point) is 2.47 cm^{-1} , after which we rely on the DUO extrapolation. It should be noted, however, that the impact from the energies in the extrapolated region is marginal for practical applications due to the low absorption intensities of the corresponding transitions. For the example, the overtones with $v' > 29$ fall into the wavenumber region above $40\,000 \text{ cm}^{-1}$, which is fully excluded from the line list. We keep the corresponding energies anyway for the sake of completeness.

The partition function $Q(T)$ was calculated for the $^{14}\text{N}^{16}\text{O}$ isotopologue, and compared to that computed by Sauval & Tatum (1984); there is good agreement above 1000 K, below which the Sauval and Tatum model is not valid. Slight disagreement at high temperatures is likely due to the fact that only the ground state of NO is considered in this work, since excited states will have a larger contribution to the partition function at high temperatures. An idea for future work is to compute line lists for the excited states, and to model the interaction between these states, in order to improve the accuracy of the line list at high rotational and vibrational energy levels.

Lifetimes were calculated for all energy levels considered. Absorption cross-sections have been calculated for temperatures ranging from 300 to 5000 K. The absorption spectrum at 3000 K is in excellent agreement with but much more extensive than the same spectrum calculated from the HITEMP data base (Rothman et al. 2010), illustrating that the line list is also accurate at high temperatures. The absorption spectra will be applied in the characterization of high-temperature astronomical objects such as exoplanet atmospheres, brown dwarfs and cool stars. The NO spectra may also be useful in the remote sensing of high-temperature events in the Earth's atmosphere such as lightning and vehicle re-entry from orbit. Our calculations also provide Landé g -factors for each state; a comparison of these values with observed (Ionin et al. 2011) Zeeman splitting of NO states in weak magnetic fields was carried out

by Semenov, Yurchenko & Tennyson (2017), and found very good agreement.

The six NO line lists are the most comprehensive available; they extend up to a wavenumber of $40\,000 \text{ cm}^{-1}$, compared to the upper limit of $10\,000 \text{ cm}^{-1}$ in both the HITRAN and HITEMP data bases (Rothman et al. 2010, 2013). These line lists can be downloaded from the CDS, via <ftp://cdsarc.u-strasbg.fr/pub/cats/J/MNRAS/>, or <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/MNRAS/>, or from www.exomol.com. On the ExoMol website, we also provide a script to convert the line list into the native HITRAN format.

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