

Orthogonal polarization approach for three dimensional georadar surveys.

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Abstract

This paper presents the results obtained from the combination of co-pole GPR data collected along perpendicular directions. The scope is to demonstrate how this approach can efficiently overcome pitfalls of traditional single orientation surveys and ensure target detection regardless their geometrical and physical properties. This is of highly importance especially when acquiring across targets that show directional dependencies of the preferential scattering components. The work relies on four field examples, each of them illustrating in details the improvements and the advantages a single image resulting from the stack of the two volumes can show, in particular for what concern target imaging.

Keywords: Ground penetrating radar, polarization, 3D surveys, structures inspection.

1. Introduction

Ground penetrating radar technique has proven to be a practical and productive method for non-destructive diagnosis of shallow subsurface ([1], [2], [3]). Commonly, GPR surveys are performed along single bidimensional profiles or sparsely sampled grids. Nevertheless a faster data collection, 2D profiles could lead to incorrect reconstruction of subsurface features, especially when geometry of the investigated targets is complex.

25 Three dimensional acquisitions are more time consuming and expensive than a
26 bidimensional ones ([4]) because it is necessary to acquire a dense and regular grid of
27 traces, with a sample spacing sufficient to prevent spatial aliasing problems ([5]).
28 Fulfilling these constraints guarantees a fully reconstruction of the geometry of any
29 targets. Specific problems that need a 3D approach to be solved are, for example, linear
30 targets ([6], [7], [8]), fault and geological features ([9], [10], [11], [12]), archaeology
31 ([13], [14], [15]), cultural heritage ([16], [17], [18]) and UXO detection ([19], [20],
32 [21]).

33 Major concerns about georadar capabilities are related to the directional sensibility of
34 the EM wavefield. Most GPR systems employ linearly polarized dipole antennae with
35 transmitter emitting an electric field polarized parallel to the long axis of the dipole and
36 a receiver that records only the component parallel to its long axis ([22]). However, it
37 has been noticed that various targets of georadar surveys, such as buried pipes and
38 fractures, have strong polarization dependent scattering characteristics ([23], [24], [25],
39 [26]). Numerous studies have exploited and investigated these features and their
40 relationship with radar imaging (e.g. [7], [27], [28]), showing that to map any
41 subsurface target it is necessary to perform a 3D full polarization georadar survey.

42 In [29], authors presented the possibility of summing georadar data acquired along
43 perpendicular directions to improve target detection. A work from the authors ([30])
44 demonstrated that the combination of data acquired with through a couple of dipoles
45 oriented perpendicular to each other ensures linear target detection regardless relative
46 geometry between transmitters and targets and physical properties of the target.

47 This work demonstrates the effectiveness of the proposed approach in 3D ground
48 penetrating radar applications. Further considerations are focused on final images

49 processing, as the stack process can bring an amplitude range that might masks weaker
50 targets.

51

52 **2. Surveys description and results**

53 The four 3D GPR experiments were all recorded using the Aladdin georadar system (by
54 IDS - Ingegneria dei Sistemi, Italy), which consists in a couple of two 2 GHz dipole
55 antennae (with offset of 6 cm for both configuration) at orthogonal polarization, and the
56 positioning system *PSG* (Pad System for Georadar, U.S. Patent no. US 7,199,748 B2 of
57 Politecnico di Milano, Italy, see [31]). The device used for the presented field
58 experiments and its design is illustrated in Fig. 1.

59 **Figure 1**

60 This configuration guarantees precise matching between the two CMP of the parallel
61 (VV) and perpendicular (HH) orientation, in respect to the survey direction, permitting
62 joint orthogonally polarized scans to be acquired in a single pass. Accurate profile
63 spacing was obtained through *PSG*, a pad whose surface is modelled with parallel tracks
64 that are few millimetres high. The GPR antenna is dragged along the tracks so that
65 parallel and regularly spaced profiles are rapidly executed without varying antenna
66 orientation during the whole survey.

67 The two analysed stacking strategies were the arithmetic mean of the raw data and of
68 the processed ones. Data were processed using a tool developed by Politecnico di
69 Milano running on *Mathworks* MATLAB software.

70 Radar images are shown through depth slices, obtained by plotting the amplitude of the
71 brightest reflector over the specified depth range. Further on, all the presented images
72 are displayed with the same amplitude range and contrast settings so the amplitude

73 response of each component can be compared.

74

75 **2.1. Palazzo Pisani, Venice, Italy.**

76 First survey was carried out in Venice to investigate the geometry of local structural
77 metallic features, so called “fiube”; these elements were used to connect the façade of a
78 building to the floors. The only aid for detecting such targets is the presence of the end
79 of a “fiuba” on the façade (Fig. 2a). Acquisition was performed on the floor (Fig. 2b, the
80 white arrow represents survey direction and starting profile) and parameters for both
81 configuration are given in Table 1.

82 **Table 1**

83 To obtain a square mesh, data were interpolated to a 0.8 cm step-increment grid.

84 **Figure 2**

85 Processing consisted in five steps ([5]), described in Table 2.

86 **Table 2**

87 Raw stack was computed after the alignment process, while the processed one after data
88 envelope.

89 Images from single azimuth processing are shown in Fig. 3a (HH configuration) and
90 Fig. 3b (VV configuration). Two “fiube” are detected (see sketched representation of
91 targets in Fig. 4) and the comparison shows the different sensitivity of the antenna
92 orientation to linear targets. Target oriented perpendicular to the survey direction (target
93 marked A in Fig. 4) is clearly visible in the HH acquisition (Fig. 3a), while almost
94 invisible in the VV one (Fig. 3b, except for a 3D scattering effect at the end of the bar).
95 Concerning the inclined fiuba (target B in Fig. 4), its representation is visible in both
96 configurations with a lower response.

97 **Figure 3**

98 **Figure 4**

99 Final images coming from the azimuthal stack are presented in Fig. 3c (raw) and Fig. 3d
100 (processed).

101 As can be seen, results confirm what was expected, that is a precise reconstruction of
102 targets regardless their orientation.

103 There are no noticeable differences between the two results, except that Fig. 3d
104 (envelope stack) is a little more degraded, as a consequence of the higher noise of the
105 HH image (Fig 3a). This aspect is related to the difference in antenna pattern between
106 the two configurations.

107 For this reason, a stacking strategy based on pixels amplitude comparison was
108 computed. The concept is the following: if a target is clearly visible there is no need to
109 adding up the complementary polarization contribute. Starting from the computation of
110 the absolute value of the amplitude difference between corresponding pixels, a threshold
111 value is chosen to set if these pixels should be included in the algorithm or not. Only the
112 couples whose absolute difference is less than or equal to the threshold are stacked,
113 while the maximum of the two pixels is taken if their difference exceeds it. In case of
114 degraded data, this approach averages and lowers noisy regions of the image, as noise is
115 less sensitive to wave polarization. For linear targets, for which antenna orientation has
116 a strong impact, this scheme ensures that the optimum condition will always be
117 selected. These features highly improve the signal to noise ratio and, consequently,
118 image resolution. Another benefit is a better target shape reconstruction.

119 The threshold value is varied to take into account the amount of pixels that will be
120 stacked. Fig. 5 represent the final image obtained applying a threshold starting from a

121 value of 0 (the maximum values are always taken) up to 0.7 (close to the average of the
122 entire images).

123 **Figure 5**

124 If one consider a threshold of 0.3 (Fig. 5d), that means that pixels are stacked if and
125 only if their difference in amplitude is less than or equal to 0.3, the following
126 considerations can be made:

- 127 • Noise is highly mitigated, compared to the HH image (Fig. 3a).
- 128 • Inclined target is represented with a better resolution and higher intensity,
129 compared to the VV image (Fig. 3b) and the stack of the raw data (Fig. 3c).

130 The primary advantage of a threshold approach, in situations where there are no
131 essential differences between the two techniques, is the possibility to easily manage the
132 amplitude range of the final image and the amount of noise that can occur.

133

134 **2.2. Donizetti Theatre, Bergamo, Italy.**

135 Another example, taken from a survey on the Gaetano Donizetti Theatre in Bergamo
136 (Fig. 6a), was aimed to detect the presence of metallic supports to the letters of the
137 marble inscription on top of the façade (Fig. 6b).

138 **Figure 6**

139 All profiles were acquired oriented from the top of the façade to the ground (black
140 arrow in Fig. 6b).

141 Acquisition parameters are listed in Table 3.

142 **Table 3**

143 As before, a 0.8 spacing square mesh was created. Processing scheme, detailed in Table
144 4, included also a background removal after the traces alignment, in order to reduce the

145 effect of the marble slabs.

146 **Table 4**

147 Raw data stack was computed before the background removal step.

148 Fig. 7a and Fig. 7b describe single azimuth results (HH and VV, respectively).

149 **Figure 7**

150 **Figure 8**

151 Some remains of the slabs are still present (see the vertical and inclined sticks of the N
152 letter), but the anchorage system of the inscription is clearly identified. Referring to the
153 sketch in Fig. 8, two of the three bars (targets A and B) are oriented crossline to the
154 survey line, while the other one (target C) is parallel to it. The azimuthal stack presented
155 in Fig. 7c (raw) and Fig. 7d (processed) demonstrates the benefits of displaying all
156 linear targets independently from their orientation in a single image. Comparing the two
157 figures, one can see that stack of the enveloped data (fig. 7d) produce a more clean and
158 focused image, in particular nearby the vertical oriented bar.

159 Further on, the stack highlights the curved shape of the bar B marked in Fig. 8 with a
160 dotted circle. This aspect does not appear in the HH image (Fig. 7a), while in the VV
161 one (Fig. 7b) there are some traces of the stroke oriented nearly parallel to the antenna.

162 Essentially, this feature is hardly detectable looking only through single azimuth
163 volume. The amplitude related stack (Fig. 9), following the considerations made
164 previously in Subsec. 2.1, shows improvements in decreasing the remnants of the
165 background signal and reconstruction of the three metallic supports.

166 **Figure 9**

167 In this case, best results are obtained with a threshold value around 0.3-0.4 (Fig. 9d -
168 9e).

169

170 **2.3. Underfloor heating system, Milan, Italy.**

171 A buried heating coil was investigated to analyse the effect of polarization on water
172 filled plastic pipes. In Fig. 10 is pictured the acquired area before cement application,
173 showing the presence pipes of different length, orientation and path. The white arrow in
174 Fig. 10 represents survey geometry and the first acquired profile.

175 **Figure 10**

176 Table 5 describes survey parameters and data volume details. Last profile (n° 113) was
177 acquired near the wall (marked in Fig. 10).

178 **Table 5**

179 The standard processing flow, reported in Table 6, was applied on the acquired profiles.

180 **Table 6**

181 As for the other experiments, raw stack consisted in the arithmetic mean of the two
182 datasets after traces alignment and the processed one after data envelope.

183 The single azimuth results are pictured in Fig. 11a (HH) and 11b (VV).

184 **Figure 11**

185 From a first analysis, there are visible amplitude differences between the HH image
186 (Fig. 11a) and the VV (Fig. 11b) one, with the last leading on the first. This effect is
187 related to the response of conductive targets depending not only on their geometry but
188 also on their length ([22]). Fig. 10 shows that pipes oriented along the survey direction
189 are longer than the others, nearly twice, and so their intensity is almost doubled. The
190 chessboard surrounding pipes is the grid in which they are cast, which is at the same
191 depth and generates a quite homogeneous scattering.

192 Another detail visible in Fig. 11a and 11b is a second pipes mesh just aside of the

193 regular one. This effect is due to the proximity of the targets, the tails of which
194 hyperbola intersecting each other create (feature highlighted in Fig. 12a and 12b) a
195 shifted and delayed version of the real targets. Interpretation and reconstruction are
196 provided in Fig. 12c and 12d.

197 **Figure 12**

198 The two dipoles orientations are not able to follow the curved shape of the pipes, as in
199 Subsec. 2.2.

200 Multiazimuth pictures are shown in figures 11c (raw) and 11d (processed). Stack of the
201 processed data provides a better results, in terms of target continuity and definition
202 (pipes are fully reconstructed), but also enhances the effect of the floor grid. Raw data
203 stack mitigates its response but lose some parts of the target, especially close to the
204 turning points. The same considerations can be made for the synthetic mesh: combining
205 processed data (Fig. 11d) the hyperbola interference effect increases, as the stack does
206 not differentiate it from the real pipes. The stack of the raw data (Fig. 11c) instead has a
207 mitigation effect, due to the arithmetic mean. Analysing the threshold stack (Fig. 13), it
208 is clear that one could obtain an optimum results (e.g. with a threshold value of 0.4, Fig.
209 13e). Differences in the effect of the threshold are evident.

210 **Figure 13**

211 The threshold effect is a noise reduction and an enhancement of the pipes, improving
212 their interpretability. Another benefit is the lowering of the tails-generated mesh. These
213 considerations are in agreement with what was explained in Subsec. 2.1.

214

215 **2.4. Wall inspection, Milan, Italy.**

216 In this case, differences in imaging are due to variations in dielectric properties between

217 bricks and lime mortar. However, they are not as evident as for conductive linear
218 targets.

219 Dataset consists in a volume of profiles acquired on a common bricks wall (geometry
220 shown in Fig. 14a and 14b), with parameters detailed in Table 7.

221 **Table 7**

222 As in Subsec. 2.2, background removal was applied to reduce the impact of plastering
223 process (processing described in Table 8). Further on, a data windowing was computed.
224 Raw stack was computed before this step, while processed one after the envelope
225 display.

226 **Table 8**

227 Single azimuth depth slices are presented in figures 14a (HH) and 14b (VV).

228 Differences in details imaging are clear, for the HH (Fig. 14a) configuration better
229 depicts horizontal segmentations of the wall, losing details of the vertical mortar lime.

230 Vertical texture is better identifiable in the VV (Fig. 14b) image. MultiAzimuth stack
231 provides images (Fig. 14c and Fig. 14d) that show some improvements in geometrical
232 reconstructions of the bricks and mortar lime sequence. No great differences are visible
233 between the two stacking techniques, except for the middle region of the image where
234 the raw stack (Fig. 14c) better reconstruct wall texture.

235 **Figure 14**

236 Useful tools to highlight abruptly gray-scale value or colour changes from one pixel to
237 the next are the directional filters, based on the discrete gradient of the image intensity
238 function ([33]). A second order method, Laplacian operator, has been applied on the
239 radar slices to enhance details and sharpness.

240 Single azimuth (Fig. 15a and 15b) confirms the hints made on the original radar images.

241 Effect of azimuthal stack is clearer (Fig. 15c and 15d), in particular if one looks in the
242 middle and right part of the picture.

243 **Figure 15**

244 Single polarization is not able to detect the mortar lime, and so the presence of a brick,
245 while the MultiAzimuth technique permits to obtain a more detailed map of the walls
246 structure.

247 The results show that the combination of MultiAzimuth strategies and image processing
248 technique could resolve complex situation, where the focus is enhancing geometrical
249 texture and features.

250

251 **3. Discussion**

252 The potential of a co-pole 3D multi polarization approach for overcoming difficulties
253 belonging to geometry and polarization has been evaluated and demonstrated with
254 several field surveys. In particular, acquisitions have made clear the advantages brought
255 by the combination of the orthogonal polarization images into a single one, without any
256 loss of attributes and resolution. These advantages lie in the opportunity of having a
257 single image with all buried and detected targets, feature that in a field of application
258 characterized by linear target (therefore ruled by polarization theory) is remarkably a
259 surplus value. Considering the two analysed stacking technique, the field surveys have
260 not shown great difference in stacking raw data and processed ones, leaving the choice
261 to the end user and survey settings. What is to be underlined is a remarkable details
262 augmentation and interpretation facility of the resulting images.

263 The risk of overwhelming weaker target reflections in the final image, due to an
264 excessive large amplitude range, has been overcome performing a stack based on pixel

265 differences, that mitigates the effect of higher amplitude and at the same time decreases
266 noise level. Computationally, the algorithm performs only a pixel by pixels analysis and
267 a comparison.

268 This method has revealed its potentiality in civil diagnosis and could be a useful tool for
269 seismic structural assessment ([34], [35]).

270 **4. Conclusion**

271 As stated at the beginning of the paper, 3D georadar surveys lie on a precise traces
272 positioning, both in crossline and inline direction. The system used in the present work
273 ensures this feature because dipoles emit simultaneously and receive from the same
274 CMP. Obviously, in large areas acquisition antenna arrays are commonly employed
275 ([36]), and so the problem of traces regularity and parallelism between adjacent profiles
276 can originate from the design of the array. In addition, positioning devices such as GPS
277 or Total Station introduce their intrinsic errors together with cumulative ones that must
278 be taken into account when acquiring long profiles ([37], [38]).

279 So, further studies and developments should have to explore the influence that a
280 misplacement of traces and irregular geometry have on the final migrated images ([39]).
281 Secondly, the unanswered question of how many azimuths are needed to ensures that no
282 features might be lost. Because of the time consuming of adding a survey direction,
283 information on its impact is highly necessary for planning a comprehensive experiment
284 without any risk of losing details of the subsurface. The importance of this issue gains
285 more and more weight in case of strongly directional events.

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288

289 **References**

- 290 [1]. Daniels DJ. Ground Penetrating Radar. 2nd ed. London, U.K.: Peter Peregrinus
291 Ltd., 2004.
- 292 [2]. Jol HM editor. Ground Penetrating Radar: Theory and Applications. 1st ed.
293 Amsterdam, The Netherlands: Elsevier; 2009.
- 294 [3]. American Society for Testing and Materials (US). Standard guide for selecting
295 surface geophysical methods, Designation D-6429, Philadelphia, PA; 1999.
- 296 [4]. Lualdi M, Binda L, Zanzi L. Acquisition and processing requirements for high
297 quality 3D reconstructions from GPR investigations. Proceedings of the
298 International Symposium Non Destructive Testing in Civil Engineering NDT-
299 CE; 2003 Sept. 16-19; Berlin, Germany.
- 300 [5]. Yilmaz O. Seismic Data Analysis. 2nd Edition. Tulsa, USA: Society of
301 Exploration Geophysicists; 2001.
- 302 [6]. Van der Kruk J, Wapenaar CPA, Fokkema JT, Van den Berg, P.M. Three-
303 dimensional imaging of multicomponent ground-penetrating radar data.
304 Geophysics 2003; 68(4): 1241-54.
- 305 [7]. Roberts R, Cist D, Kathage A. Full-Resolution GPR imaging applied to utility
306 surveying: Insight from multi-polarization data obtained over a test pit,
307 IWAGPR; 2009 May 27-29; Granada, Spain, p. 126-31.

- 308 [8]. Bernstein R, Oristaglio M, Miller DE, Haldorsen J. Imaging radar maps
309 underground objects in 3-D. *IEEE Computer Applications in Power* 2000; 13(3):
310 20-4.
- 311 [9]. Grasmueck M, Weger R. 3D GPR reveals complex internal structure of
312 Pleistocene oolitic sandbar. *The Leading Edge* 2002; 21(7): 634-39.
- 313 [10]. Lualdi M, Zanzi L. 2D and 3D experiments to explore the potential benefit of
314 GPR investigations in planning the mining activity of a limestone quarry.
315 *Proceedings of the Tenth International Conference Ground Penetrating Radar*
316 *(GPR 2004)* June 21-24; Delft, The Netherlands, p. 613-6.
- 317 [11]. Vanneste K, Verbeek K, Petermans T. Pseudo 3D imaging of a slow-slip-rate,
318 active normal fault using shallow geophysical methods: The Geleen fault in the
319 Belgian Maas River valley. *Geophysics* 2008; 73(1): B1-B9.
- 320 [12]. Carpentier SFA, Green AG, Langridge RM, Boschetti S, Doetsch J, Abächerli
321 AN, et al. Flower structures and Riedel shears at a stepover zone along the
322 Alpine Fault (New Zealand) inferred from 2D and 3D GPR images. *J. Geophys.*
323 *Res.* 2012; 117: B2.
- 324 [13]. Lorenzo H, Novo A, Rial FI, Solla M. Three-dimensional Ground-penetrating
325 radar strategies over an indoor archaeological site: convent of Santo Domingo
326 (Lugo, Spain). *Archaeol. Prospect.* 2010; 17: 213-22.
- 327 [14]. Verdonck L, Vermeulen F, Docter R, Meyer C, Kniess R. 2D and 3D ground-
328 penetrating radar surveys with a modular system: data processing strategies and

- 329 results from archaeological field tests. *Near Surface Geophysics* 2013; 11(2):
330 239-52.
- 331 [15]. Lualdi M, Zanzi L, Sosio G. A 3D GPR survey methodology for archaeological
332 applications. Proceedings of the Eleventh International Conference on Ground
333 Penetrating Radar (GPR 2006) June 19-22; Columbus, Ohio, USA.
- 334 [16]. Binda L, Lualdi M, Saisi A, Zanzi L. Radar investigation as a complementary
335 tool for the diagnosis of historic masonry buildings, *Int. J. of Materials and*
336 *Structural Integrity* 2011; 5(1): 1-25.
- 337 [17]. Binda L, Lualdi M, Saisi A. Investigation strategies for the diagnosis of historic
338 structures: On-site tests on Avio Castle, Italy, and Pišce Castle, Slovenia. *Can.*
339 *J. Civil Eng.* 2008; 35: 555-66.
- 340 [18]. Binda L, Cantini L, Lualdi M, Tedeschi C, Saisi A, Zanzi L. Investigation on
341 structures and materials of the Castle of Avio (Trento, Italy), *Adv. Architect.*
342 2005; 20: 599-610.
- 343 [19]. Lualdi M, Zanzi L. Testing a safe acquisition procedure for an effective
344 application of GPR to security operations. Proceedings of the Symposium on the
345 Application of Geophysics to Engineering and Environmental Problems
346 (SAGEEP) 2005 Apr. 3-7; Atlanta, USA; p. 613-23.
- 347 [20]. Zanzi L, Lualdi M, Braun HM, Borisch W, Triltzsch G. An ultra-high frequency
348 radar sensor for humanitarian demining tested on different scenarios in 3D
349 imaging mode. *Proc. SPIE* 2002 Apr. 15; 4758(1): 240-45.

- 350 [21]. Torrione P, Collins LM. Texture Features for Antitank Landmine Detection
351 Using Ground Penetrating Radar. IEEE Transactions on Geoscience and Remote
352 Sensing 2007; 45(7): 2374-82.
- 353 [22]. Balanis CA. Antenna Theory: Analysis and Design. 1st ed. New York, US:
354 Wiley & Sons, 1982.
- 355 [23]. Roberts RL, Daniels JJ. Analysis of GPR polarization phenomena. J. Environ.
356 Eng. Geophysics 1996; 1(2): 139-57.
- 357 [24]. Fokkema JT, Slob EC, Fokkema E, Beekman S. Material response analysis of
358 georadar reflection data. Near Surface Geophysics 2004; 2(1): 41-7.
- 359 [25]. Radzevicius SJ, Daniels DJ. Ground penetrating radar polarization and
360 scattering from cylinders. Journal of Applied Geophysics 2000; 45(2): 111-25.
- 361 [26]. Sassen DS, Everett ME, Munster CL. Ecohydrogeophysics at the Edwards
362 Aquifer: insights from polarimetric ground-penetrating radar. Near Surface
363 Geophysics 2009; 7(5): 427-38.
- 364 [27]. Tsoflias GP, Van Gestel JP, Stoffa PL, Blankenship DD, Sen M. Vertical
365 fracture detection by exploiting the polarization properties of ground-penetrating
366 radar signals. Geophysics 2004; 69(3): 803-10.
- 367 [28]. Van der Kruk J, Zeeman JH, Groenenboom J, Multicomponent imaging of
368 different objects with different strike orientation. Proceedings of the Ninth
369 International Conference on Ground Penetrating Radar 2002 Apr. 29 – May 2;
370 Santa Barbara, USA; p. 150-5.

- 371 [29]. Lehmann F, Boerner DE, Holliger K, Green AG. Multicomponent georadar data:
372 Some important implications for data acquisition and processing. *Geophysics*
373 2000; 65(5): 1542-52.
- 374 [30]. Lualdi M, Lombardi F. Combining Orthogonal Polarization for Full Linear
375 Target Detection with GPR. Forthcoming 2013.
- 376 [31]. Lualdi M. True 3D Acquisition using GPR over small areas: A cost effective
377 solution. Proceedings of the Symposium on the Application of Geophysics to
378 Engineering and Environmental Problems (SAGEEP) 2011 Apr. 11; Charleston,
379 South Carolina, US; p. 541-50.
- 380 [32]. Zanzi L, Lualdi M. Analysis of Approximations and Aperture Distortion for
381 3DMigration of Bistatic Radar Data with the Two-Step Approach. *EURASIP*
382 *Journal on Advances in Signal Processing* 2010, 2010.
- 383 [33]. Pratt WK. *Digital Image Processing*. 4th ed. New York, US: Wiley & Sons,
384 2007.
- 385 [34]. Valente M. Seismic performance assessment of a non-ductile RC building
386 retrofitted by steel bracing or fiber-reinforced polymers. *Applied Mechanics*
387 *and Materials* 2012; 234: 84-9.
- 388 [35]. Valente M. Seismic strengthening of non-ductile R/C structures using infill wall
389 or ductile steel bracing. *Advanced Materials Research* 2013; 602: 1583-87.
- 390 [36]. Birken R, Miller DE, Burns M, Albats P, Casadonte R, Deming R, et al.
391 Efficient large scale underground utility mapping with a multi-channel ground

- 392 penetrating imaging radar system. Proceeding of the Ninth International
393 Conference on Ground Penetrating Radar 2002 Apr. 29 – May 2; Santa Barbara,
394 USA; p. 186-98.
- 395 [37]. Böniger U, Tronicke J. On the potential of kinematic GPR surveying using a
396 self-tracking total station: Evaluating system cross-talk and latency. IEEE
397 Transactions on Geoscience and Remote Sensing 2010; 48(10): 3792-98.
- 398 [38]. Grasmueck M, Viggiano DA. Integration of ground-penetrating radar and laser
399 position sensors for real-time 3-D data fusion. IEEE Transactions on
400 Geoscience and Remote Sensing 2007; 45(1): 130–7.
- 401 [39]. Groenenboom J, Van Der Kruk J, Zeeman JH. 3D GPR data and the influence of
402 positioning errors on image quality. 63rd EAGE Conference & Exhibition 2001
403 June 11-15, Amsterdam, The Netherlands.