

# Displacement prediction of step-like landslide by applying a novel kernel extreme learning machine method

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## Abstract

Landslide displacement prediction is an essential component for developing landslide early warning systems. In the Three Gorges Reservoir area (TGRA), landslides experience step-like deformations (i.e. periods of stability interrupted by abrupt accelerations) generally from April to September due to the influence of precipitation and reservoir scheduled level variations. With respect to many traditional machine learning techniques, two issues exist relative to displacement prediction, namely the random fluctuation of prediction results and inaccurate prediction when step-like deformations take place. In this study, a novel and original prediction method was proposed by combining the Wavelet Transform (WT) and Particle Swarm Optimization-Kernel Extreme Learning Machine (PSO-KELM) methods, and considering the landslide causal factors. A typical landslide with a step-like behavior, the Baishuihe landslide in TGRA, was taken as a case study. The cumulated total displacement was decomposed into trend displacement, periodic displacement (controlled by internal geological conditions and external triggering factors respectively), and noise. The displacement items were predicted separately by multi-factor PSO-KELM considering various causal factors, and the total displacement was obtained by summing them up. An accurate prediction was achieved by the proposed method, including the step-like deformation period. **The performance of the proposed method was compared with the multi-factor Extreme Learning Machine (ELM), Support Vector Regression (SVR), Backward Propagation Neural Network (BPNN), and single-factor PSO-KELM. Results show that the PSO-KELM outperforms other models, and the prediction accuracy can be improved by considering causal factors.**

**Keywords:** Step-like landslides, Displacement prediction, Kernel Extreme Learning Machine, Three Gorges Reservoir

## 27 **1. Introduction**

28 Landslides are a common natural hazard, which cause fatalities and economic damages worldwide (Petley  
29 2012). In the Three Gorges Reservoir Area (TGRA) of China, thousands of landslides are threatening the  
30 surrounding environment. It is timely and significant to carry out accurate landslide displacement prediction, which  
31 is an essential component of developing early warning systems for landslides (Casagli et al. 2010; Intrieri et al.  
32 2013).

33 Since Saito proposed the empirical formula for landslide prediction (Saito 1965), numerous landslide  
34 prediction models have been developed (Fukuzono 1985; An et al. 2016; Carlà et al. 2016; Carlà et al. 2017; Conte  
35 et al. 2017; Zhou et al. 2017). They can be grouped into two categories: physical models and data-based models.  
36 The data-based models are more popular than physical models (Corominaset al. 2005) because of simple process  
37 and accurate prediction. Recently, a variety of Machine Learning (ML) models have been applied in landslide  
38 spatial and temporal prediction, such as Artificial Neural Network (ANN) (Du et al. 2013; Liu et al. 2016), Support  
39 Vector Machine (SVM) (Wu et al. 2016; Zhu et al. 2017), Decision Tree (Krkač et al. 2017; Ma et al. 2017),  
40 Extreme Learning Machine (ELM) (Cao et al. 2016; Vasu and Lee 2016; Huang et al. 2017), and so on.

41 Previous studies suggest that the ML models have achieved good performances in landslide displacement  
42 prediction. However, two deficiencies may limit its application: i.e. the fluctuation of prediction results and the  
43 inaccurate prediction in strong deformation period. For example, ELM randomly generates the connection weight  
44 between the input and hidden layers, which leads to the varied outputs, even if the inputs are totally the same  
45 (Huang et al. 2004; Yang et al. 2017). To address these limitations and improve the stability and accuracy of  
46 prediction, the Kernel Extreme Learning Machine (KELM) model, proposed by Huang et al in 2012, is applied to  
47 predict landslide displacement in this study. Simultaneously, the Particle Swarm Optimization (PSO) algorithm  
48 was utilized to optimize the parameters of KELM. The combination of these two methods are expected to increase  
49 the prediction accuracy.

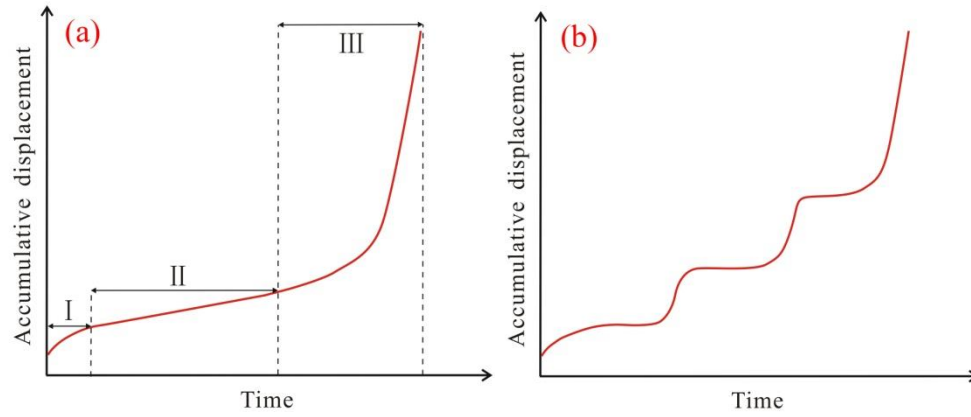
50 Landslide displacement is controlled by many factors and can be considered being constituted by several  
51 components. For example, the long-term deformation trend is controlled by the internal geological conditions,  
52 while the short-term deformation fluctuation is caused by external triggering factors (Glade et al. 2005; Du et al.

53 2013), such as seasonal weather variations. The key of prediction, especially in strong deformation periods, is to  
54 establish accurate response relationship between causal factors and landslide deformation. Consequently,  
55 displacement time series should be decomposed and predicted separately with consideration of different causal  
56 factors in modelling.

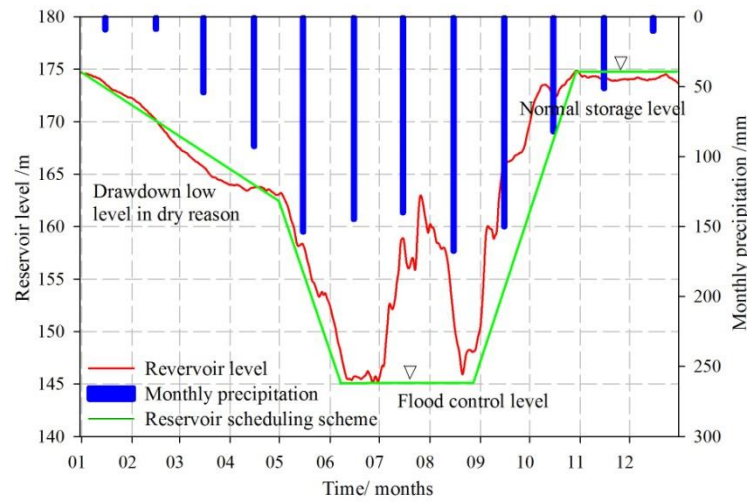
57 In this study, a hybrid ML model for landslide displacement prediction was proposed with the consideration of  
58 causal factors. The Baishuihe landslide in the TGRA was taken as a case study. It has a typical step-like kinematic  
59 behavior, which means that long stable periods are interrupted by periodic abrupt accelerations. Based on the  
60 analysis of landslide step-like deformation, its displacement was decomposed into trend component, periodic  
61 component and noise by wavelet transform (WT). The precipitation, reservoir level and previous displacements  
62 were adopted as the causal factors of periodic displacement, while the previous displacements were used as the  
63 causal factors of trend displacement. The PSO-KELM was applied to predict both the trend and periodic  
64 displacements with respective to causal factors, and the total forecast displacement was the summation of the  
65 predicted displacements. To verify the performance of the proposed model (multi-factor PSO-KELM), the  
66 single-factor PSO-KELM and multi-factor Extreme Learning Machine (ELM), Support Vector Regression (SVR),  
67 and Backward Propagation Neural Network (BPNN) models were executed and compared.

## 68 2. Displacement analysis of step-like landslides

69 According to the creep deformation theory (Saito 1969), landslides approaching failures experience three  
70 consecutive stages (Fig. 1a): an initial deceleration (primary creep), a steady deformation (secondary creep) and  
71 eventually a hyperbolic acceleration which can lead to collapse. However, because of the influence of external  
72 triggering factors, landslides often show different deformation patterns. In the TGRA, under the influence of  
73 periodic precipitation and reservoir water level oscillations (Fig. 2), most landslides deform sharply from April to  
74 September every year. Then, when the triggers cease, typically from October to April, they become steady again  
75 (Miao et al. 2014). Consequently, the resulting cumulated displacement against time shows a step-like curve (Fig.  
76 1b).



77  
78 **Fig. 1:** (a) Standard creep curve of landslide (I: decelerating creep stage; II: steady-state creep  
79 stage, and III: accelerating creep stage); and (b) Step-like landslide evolution curve



80  
81 **Fig. 2** Monthly precipitation and reservoir water level variation in the TGRA (2012)

82 The deformation evolution of step-like landslide is jointly affected by internal geological conditions and  
83 external triggering factors. The displacement controlled by internal geological conditions shows approximately  
84 monotonically increase in larger time scale (Fig. 1a), while the displacement induced by periodic rainfall and  
85 reservoir scheduling shows sudden increases in small time scale (Fig. 1b). These two components of the total  
86 displacement are defined as trend displacement and periodic displacement, respectively. At the same time, the  
87 system error always exists during deformation monitoring process. The cumulated displacement time series can be  
88 decomposed as follows:

89

$$D = T + P + N \quad (1)$$

90 Where  $D$  is the original total cumulated displacement,  $T$  is the trend displacement,  $P$  is the periodic  
91 displacement and  $N$  is the noise from system error of monitoring.

### 92 **3. Displacement prediction model and methodology**

#### 93 **3.1. Wavelet Transform**

94 Wavelet Transform (WT) is an effective analysis method for the signal process, which provides good  
95 localization in both time and frequency domains (Daubechies 1990). The WT can be divided into two classes,  
96 continuous wavelet transformation (CWT) and discrete wavelet transformation (DWT). Compared to the CWT,  
97 which requires complex computation and massive data, the DWT requires less time and is easy to be implemented,  
98 the definition is shown as follows:

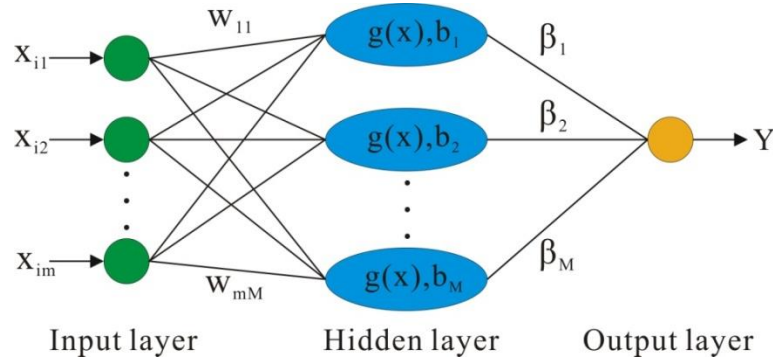
$$99 \quad DWT_y(m, n) = 2^{-\frac{m}{2}} \int_{-\infty}^{+\infty} s(t) \sigma^*(2^{-m}t - n) dt \quad (2)$$

100 Where  $m$  is the scaling constant and  $n$  is the translating constant which is an integer;  $s(t)$  is a signal time  
101 series and  $\sigma^*(x)$  is the complex conjugate function.

102 The DWT algorithm proposed by Mallat (1989) has been widely used. It applies high-pass and low-pass filters  
103 to extract approximation and detail sequence from the original signal. The approximation sequence represents the  
104 low-frequency component, which contains trend information. The detail sequence represents the high-frequency  
105 component, which contains periodic information. In addition, a proper wavelet function is also important for WT.  
106 There are many wavelet functions, such as the Haar (1910), Meyer (1990), Daubechies (1992) and so on. In this  
107 study, Daubechies, which is smooth, orthogonal and compactly supported, was adopted to decompose landslide  
108 displacement time series.

#### 109 **3.2. Kernel extreme learning machine**

110 Extreme learning machine (ELM) (Huang et al. 2006) is a novel ML model with feed-forward neural network  
111 training. Because of the excellent generalization ability and fast learning speed, ELM has been adopted in various  
112 fields recently (Lima et al. 2015; Barzegar et al. 2016; Yang et al. 2017). The main characteristic of ELM is that  
113 some parameters, such as the connection weight between the input and hidden layers, are generated randomly. The  
114 basic network structure of ELM is shown in Fig. 3.



**Fig. 3** The network structure of ELM

115 For  $N$  arbitrary samples  $(x_i, y_i)$ , where  $x_i = [x_{i1}, x_{i2}, \dots, x_{im}]^T \in R^m$ ,  $y_i \in R$ . The output of ELM is defined as  
 116 follows:

119 
$$f(x) = \sum_{i=1}^N \beta_i h(w_i \cdot x_i + b_i) \quad (3)$$

120 Where  $N$  is the number of hidden neurons;  $\beta_i = [\beta_1, \beta_2, \dots, \beta_N]$  is the output weight connecting the hidden  
 121 nodes and the output nodes;  $w_i = [w_{1i}, w_{2i}, \dots, w_{mi}]$  is the weight vector connecting the hidden nodes and the input  
 122 nodes;  $b_i = [b_1, b_2, \dots, b_n]$  is the threshold of the hidden nodes;  $h(x)$  is a future mapping of hidden nodes. As the  
 123 input weight  $w$  and the hidden layer threshold  $b$  are determined randomly, the goal of network training is to  
 124 find the best output weight  $\beta$ , which can be calculated by the least square method:

125 
$$\beta^* = H^+ Y \quad (4)$$

126 Where  $H^+$  is the Moore-Penrose generalized inverse of the hidden layer output matrix  $H$  (Huang et al. 2006).

127 In order to overcome the randomness of ELM, and improve its generalization capability and stability, Huang  
 128 et al. (2012) extended ELM into kernel learning and proposed kernel-based ELM. Based on orthogonal projection  
 129 method and ridge regression theory, the output weight  $\beta$  can be calculated by adding a positive constant  $1/C$  as:

130 
$$\beta = H^T (1/C + HH^T)^{-1} Y \quad (5)$$

131 Hence, the output function of ELM is expressed as follows:

132 
$$f(x) = h(x) H^T (1/C + HH^T)^{-1} T \quad (6)$$

133 The kernel matrix for the ELM can be utilized to replace  $h(x)$ . Then, the output function of KELM can be

134 written as follows:

$$135 \quad f(x) = \begin{bmatrix} K(x, x_1) \\ \mathbf{M} \\ K(x, x_N) \end{bmatrix}^T (1/C + HH^T)^{-1} T \quad (7)$$

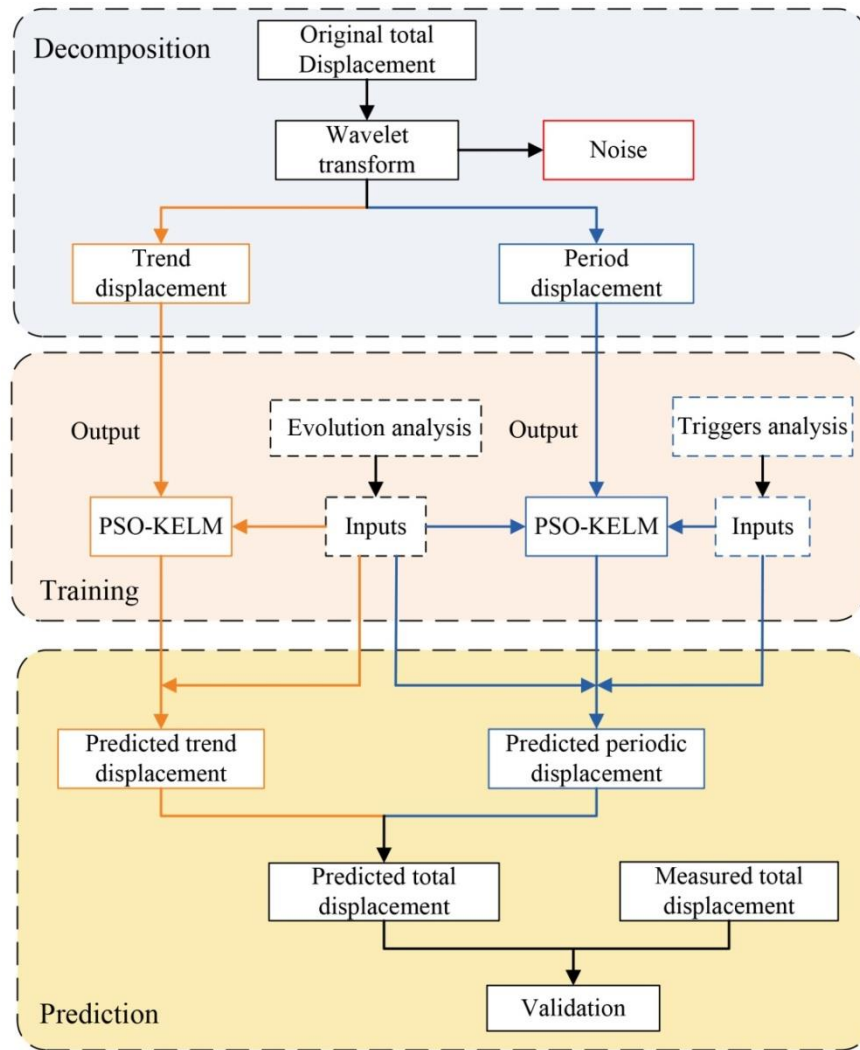
136 Where  $K(x, x_i)$  is the kernel function. In this study, the radial basis function was applied as the kernel  
137 function.

### 138 3.3. Particle Swarm Optimization

139 The particle swarm optimization (PSO) algorithm was proposed by Eberhart and Kennedy (1995). It is a  
140 population-based stochastic optimization method and has been developed rapidly in recent years. Inspired by the  
141 feeding behavior characteristic of bird flock, PSO was applied to solve the optimization problem. In PSO algorithm,  
142 the particle is described by three basic features, namely position, speed and fitness value. Each particle represents a  
143 solution for the target problem. PSO achieves the search of optimal solution through the pursuit of optimal fitness  
144 value, which is obtained by calculating the objective function of target problem. In addition, the motion direction  
145 and the distance of the particles are determined by the speed feature. The search process of PSO is implemented  
146 through a loop iteration. In the loop iteration, PSO seeks the global best solution by adjusting the trajectory of each  
147 individual toward its own best location and the best particle of the entire swarm (Eberhart and Kennedy 1995).  
148 Considering that the performance of KELM will be affected by its parameters, PSO was adopted to seek  
149 appropriate parameters.

### 150 3.4. The proposed model and performance evaluation

151 As analyzed in Section 2, the step-like displacement of the studied landslide is composed of trend  
152 displacement, periodic displacement and noise. The displacement components are affected by different factors. In  
153 this proposed model, the noise was removed from the original total displacement at first; then, the total  
154 displacement (after denoising) was decomposed into two displacement components (see Section 4.3 for details).  
155 Considering the different mechanisms of trend and periodic displacements, they were separately modeled using the  
156 PSO-KELM, and the total displacement was obtained by adding them together. The flowchart of the proposed  
157 method is shown in Fig. 4.



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**Fig. 4** The proposed prediction method for the step-like landslide displacements

160

In order to assess the model performance, four statistical indices were used, namely the root mean square error

161

(RMSE), absolute percentage error (APE), mean absolute percentage error (MAPE) and relation coefficient (R).

162

Larger R and smaller RMSE, APE and MAPE indicate higher prediction performance. The formulas of the four

163

indices are shown as follows:

164

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (\hat{D}_i - D_i)^2} \quad (8)$$

165

$$APE = \left| \frac{\hat{D}_i - D_i}{D_i} \right| \quad (9)$$

166

$$MAPE = \frac{1}{N} \sum_{i=1}^N \left| \frac{\hat{D}_i - D_i}{D_i} \right| \quad (10)$$



167

$$R = \frac{\sum_{i=1}^N (D_i - \bar{D})(\hat{D}_i - \bar{\hat{D}})}{\sqrt{\sum_{i=1}^N (D_i - \bar{D})^2} \sqrt{\sum_{i=1}^N (\hat{D}_i - \bar{\hat{D}})^2}} \quad (11)$$

168

where  $N$  is the number of cumulated displacement values;  $D_i$  is the observed cumulated displacement

169

values;  $\hat{D}_i$  is the predicted cumulated displacement values;  $\bar{D}$  is the mean of observed values;  $\bar{\hat{D}}$  is the mean of

170

predicted values.

## 171 4. Case study: the Baishuihe landslide

### 172 4.1. Geological conditions

173

Baishuihe is located in the county of Zigui, Hubei province ( $31^{\circ}01'34''\text{N}$ ,  $110^{\circ}32'09''\text{E}$ ), 56 kilometers away

174

from the Three Gorges Dam (Fig. 5). The landslide is fan-shaped in plane with a main sliding direction of  $20^{\circ}$  NE.

175

The area of Baishuihe is about  $0.42\text{km}^2$ , with the maximum length and width of 780m and 700m, respectively (Fig.

176

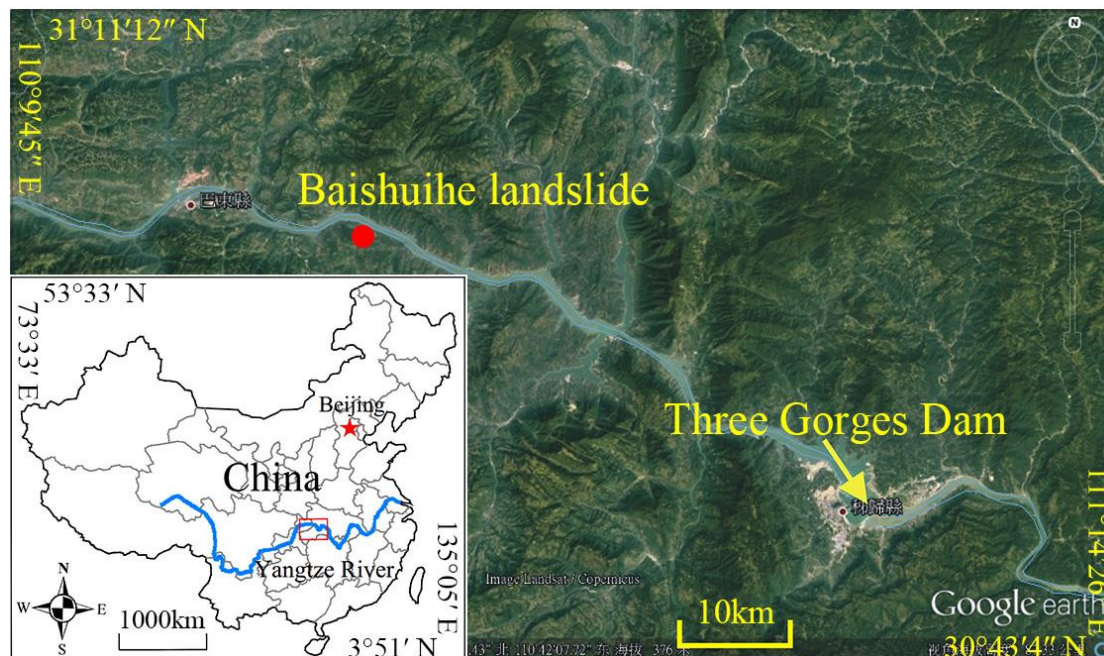
6). The average depth of sliding mass is approximately 30m with an estimated volume of  $12,600\text{m}^3$ . The landslide

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elevation extends from 75m to 390m, and the slope is gentle in the middle part and steep in both the front and rear

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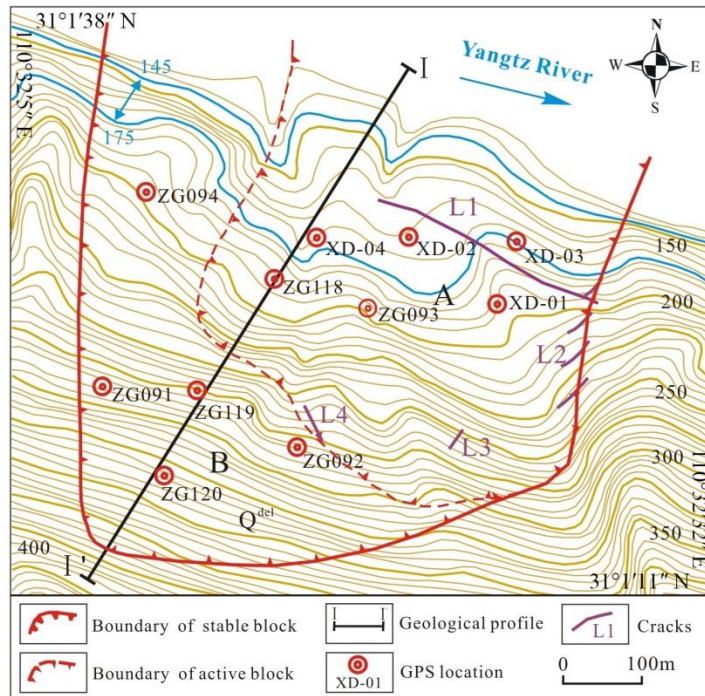
part (Fig. 7).



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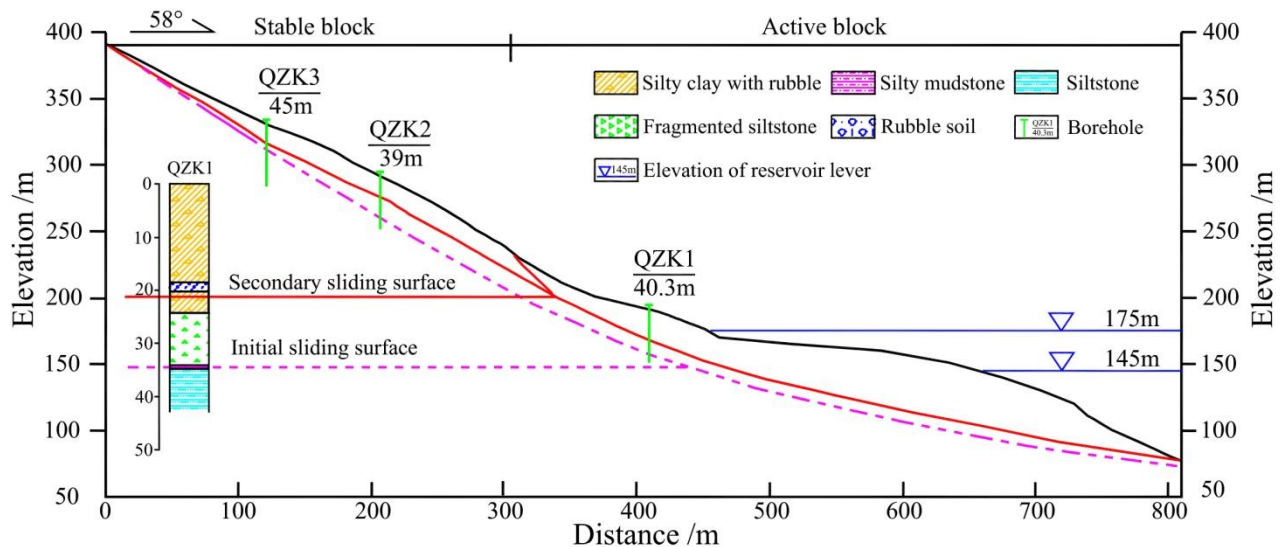
**Fig. 5** The location of Baishuihe landslide (Satellite image from Google Earth)



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**Fig. 6** Topographical map of the Baishuihe landslide (modified from Li et al. 2010)

183 The main materials of Baishuihe landslide are quaternary deposits, which contain silty clay and fragmented  
 184 rubble with a loose and chaotic structure. The bedrock underlying the landslide is composed of silty mudstone sand  
 185 muddy siltstones of the Jurassic Xiangxi Formation (Chen et al. 2010; Miao et al. 2014; Yabe and Hayasaka 1920),  
 186 with the dip direction ranging from 15° to 20° and the dip angle from 32° to 36° (Fig. 7).



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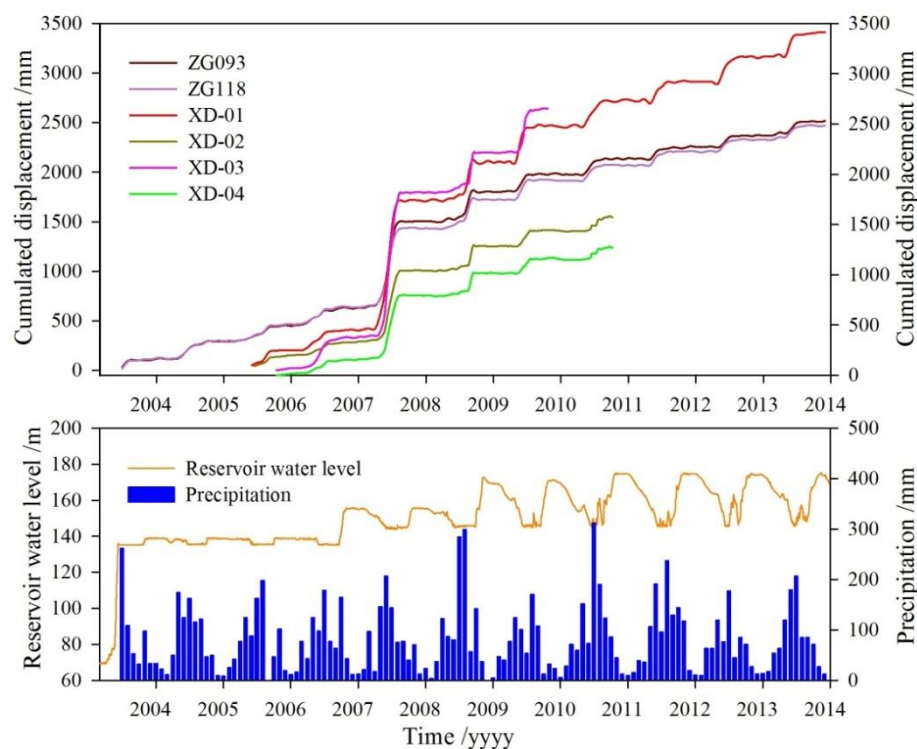
**Fig. 7** Geological profile I-I' of the Baishuihe landslide (modified from Li et al. 2010)

#### 189 4.2. Deformation characteristic analysis

190 The depth of the sliding zone was identified through boreholes and inclinometers. As shown in Fig.7, there are  
 191 two sliding surfaces, namely initial sliding surface and secondary sliding surface, occurring at different depths. The

192 depth of the secondary sliding surface varies from 12m to 21.5m, while the initial sliding surface is deeper than  
193 30m. A possible explanation for the formation of the secondary sliding surface is that a complete failure along the initial  
194 sliding surface would have required much more energy due to the large volume and complex geological conditions of the  
195 Baishuihe landslide.

196 According to field investigation and monitoring data analyses, the Baishuihe landslide can be divided into two  
197 blocks, the active block and the relatively stable block. The cumulated displacement of the active block is found as  
198 much as 3,500mm from the year 2003 to 2014 (Fig. 8). The stable block is deforming very slowly and the  
199 cumulated displacement is approximately 20mm. Apparently, the deformation velocity varies spatially. The  
200 deformation of the eastern part is stronger than the western part, while the front part experiences larger deformation  
201 than the rear part.



202  
203 **Fig. 8** The monitoring data of the Baishuihe landslide

204 Since the first impoundment of the Three Gorges Reservoir in June 2003, there were many deformation  
205 indications found on Baishuihe landslide. In the early stage of impoundment, the reservoir water level rose from  
206 75m to 145m, the Baishuihe landslide deformed gradually and several cracks developed in the front part of the  
207 landslide (Table 1, Fig. 6 and 8). In 2007, when the reservoir level firstly reached 156m and dropped from 156m to  
208 145m from February to August, combining the influence of the heavy precipitation of 518.2mm in July, the



209 landslide deformed greatly and the cumulated displacement reached 1711.4mm (Fig. 8).

210

Table 1 The main macroscopic deformation phenomena in the Baishuihe landslide

Time		Rainfall (mm)	Reservoir Water level(m)	Deformation velocity (mm/d)	Description of main deformation indications
Year	Month				
2003	7~9	228.8	135(±0.2)	1.8~2.1	Generated the tensile crack <i>L1</i> with direction of 320°, width of 5~20mm and length of 5~300m (Fig. 9a); generated the shear crack <i>L2</i> with direction of 10°~40°, width of 5~15mm and length of 5~20m (Fig. 9b).
2005	8~10	178.4	135.5(±0.5)	1.8~3.0	Generated the shear crack <i>L3</i> with direction of 50°, length of 50m and width of 10~20mm (Fig. 9c); generated the tensile crack <i>L4</i> with direction of 300°, length of 50m and width of 10~20mm (Fig. 9d);
2007	5~8	518.2	148.5~146	0.3~50.9	The landslide deformed the most in this year. All the cracks developed greatly (Fig. 9); a series of cracks developed in the rear and formed the landslide boundary. Some small cracks developed in the west part of the landslide.
2009	5~7	120.2	155.9~145.5	2.2~6.7	The cracks kept developing, especially in the eastern and front part of the landslide.



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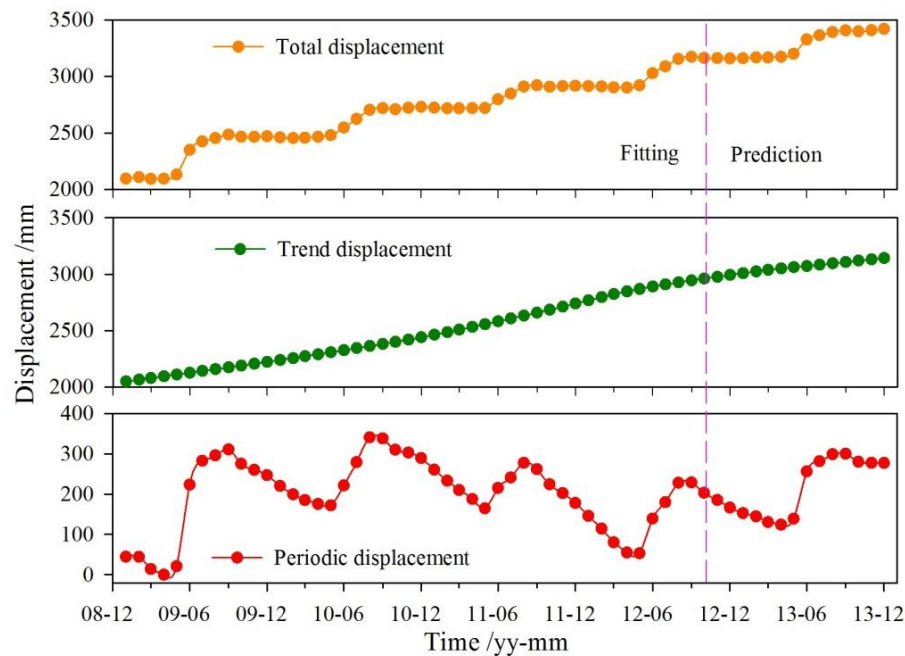
Fig. 9 Deformation indications on Baishuihe landslide

213 As a typical landslide with step-like deformation, the displacement of Baishuihe was increasing from April to  
214 September each year under the joint influence of heavy precipitation and drawdown of the reservoir water level.  
215 However, from October to April in the following year, while the reservoir level was stable (175m) and the  
216 precipitation was gentle, the landslide was in a stable state, experiencing small displacement.

217 **4.3. Decomposition of displacement time series**

218 The step-like deformation of landslide is a complex, dynamic and nonlinear system (Eid 2014). According to  
219 the deformation analysis in Section 4.2, Baishuihe landslide is a retrogressive landslide under combined influence  
220 of precipitation and reservoir level. The GPS monitoring station XD-01 in the front part was selected to establish  
221 the landslide forecasting model, since its monitoring data showed the highest cumulated displacement (Fig. 8). In  
222 the TGRA, the reservoir level has been regularly fluctuating between 145m and 175m since 2009 (Fig. 8). Hence,  
223 the monitoring data after 2009 was adopted for modelling.

224 Noise is unavoidable for the surface deformation monitoring by GPS and should be removed at first. Wavelet  
225 transform is an effective denoising method, and the automatic one-dimensional denoising method in the wavelet  
226 toolbox of *MATLAB* was used to remove the system noises from the original displacement sequence. In the  
227 frequency domain, the low-frequency component represents the trend displacement, while the high-frequency  
228 component represents the periodic displacement. The DWT with the function of Daubechies 4 was applied to  
229 divide the total cumulated displacement into the trend and periodic displacement (Fig. 10). The DWT process is  
230 performed in the wavelet toolbox of *MATLAB* as well.



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**Fig. 10** Displacement decomposition result of XD-01

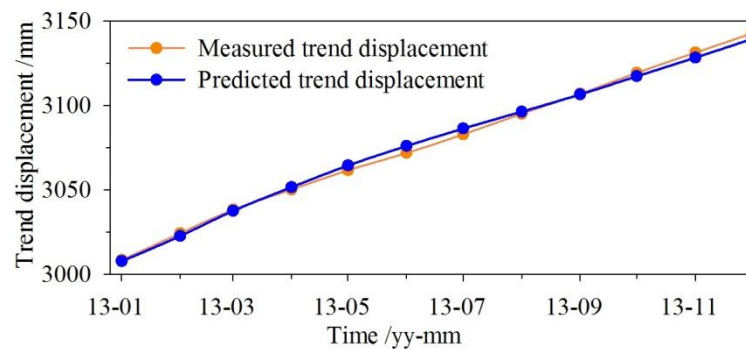
233 In addition, the ML models are more sensitive to the data ranging from 0 to 1. Therefore, all the data should be  
234 normalized into the desired range using the following formula before modelling:

235 
$$\bar{x} = \frac{x - x_{min}}{x_{max} - x_{min}} \quad (12)$$

236 Where,  $\bar{x}$  are the normalized values,  $x$  are the original values,  $x_{max}$  is the maximum value of a sequence,  
 237  $x_{min}$  is the minimum value of a sequence.

238 **4.4. Prediction of trend displacement**

239 The trend displacement is controlled by internal geological conditions. As shown in Fig. 10, the trend  
 240 displacement of the landslide is a smooth and monotonically increasing sequence, which is similar to the secondary  
 241 stage of the standard creep curve (Fig. 1a). Therefore, we can infer that Baishuihe landslide is in a steady  
 242 deformation state in large time scale. The PSO-KELM was applied to predict the trend displacement of Baishuihe  
 243 landslide. In the modelling of trend displacement, the monthly displacement from January 2009 to December 2012  
 244 was used to train, while the monthly displacement from January to December in 2013 was used for testing. The  
 245 trend displacement over the past 1, 2, 3 months was used as inputs (Zhou and Yin 2014; Cao et al. 2016). Some  
 246 samples of the data used in the modelling are shown in Table 2. The optimal parameters of KELM were searched  
 247 with PSO, whose results were  $C = 133.5672$  and  $\gamma = 49.8025$ , where  $C$  is the regularization coefficient and  $\gamma$   
 248 is the parameter of Kernel function. As shown in Fig. 11, the PSO-KELM achieved a good performance in trend  
 249 displacement; the results of RMSE, MAPE and R were 2.397, 0.001 and 0.998, respectively.



250 **Fig. 11** The predicted and measured values of the trend displacement  
 251

252 **Table 2** Some data samples used in the modelling of trend displacement

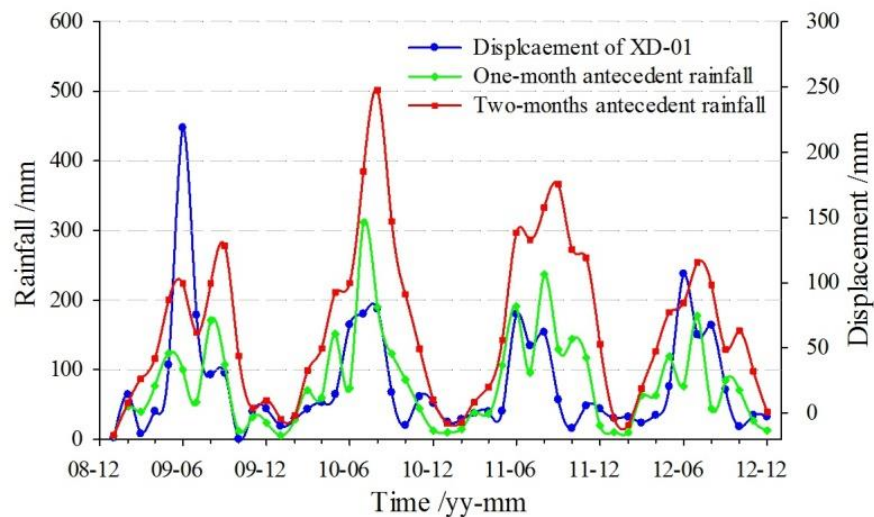
Time	Input 1	Input 2	Input 3	Output	Notes
Jan 2013	0.8332	0.8477	0.8626	0.8770	Inputs 1-3 are the trend displacement over the past 1, 2 and 3 month respectively.
Feb 2013	0.8477	0.8626	0.8770	0.8914	
Mar 2013	0.8626	0.8770	0.8914	0.9042	
Apr 2013	0.8770	0.8914	0.9042	0.9152	Output is the trend displacement of the current month;
May 2013	0.8914	0.9042	0.9152	0.9256	The displacement data is normalized into the range of [0,1];
Jun 2013	0.9042	0.9152	0.9256	0.9351	

253 **4.5. Prediction of periodic displacement**

254 **4.5.1 Causal factor analysis and input decision**

255 For the periodic displacement component, which shows small-scale fluctuations, external triggering factors  
256 are considered. As stated in Section 4.2, heavy precipitation and fluctuation of reservoir level are the main factors  
257 triggering the deformation of Baishuihe landslide from April to September.

258 The Baishuihe landslide is located in a rainy area where landslide deformation easily occurs. Rainfall  
259 infiltration may increase the sliding force which promotes landslide evolution: on the one hand, rainfall infiltration  
260 in landslides will increase the weight of the sliding mass; on the other hand, the accumulation of rainwater on  
261 the sliding surface will reduce the shear strength of sliding soil. Previous studies suggest the cumulated precipitation  
262 over the previous two months has a close relationship with landslide deformation (Keefer et al. 1987; Cao et al. 2013;  
263 Cao et al. 2016; Krkač et al. 2017; Bogaard and Greco 2018). In this study, the shapes of the precipitation of the  
264 one-month and two-months antecedent rainfall were coincident with the monthly displacement in general (Fig. 12).  
265 Therefore, the one-month and two-months antecedent rainfall were adopted as inputs to reflect the effect of  
266 precipitation (Table 3).



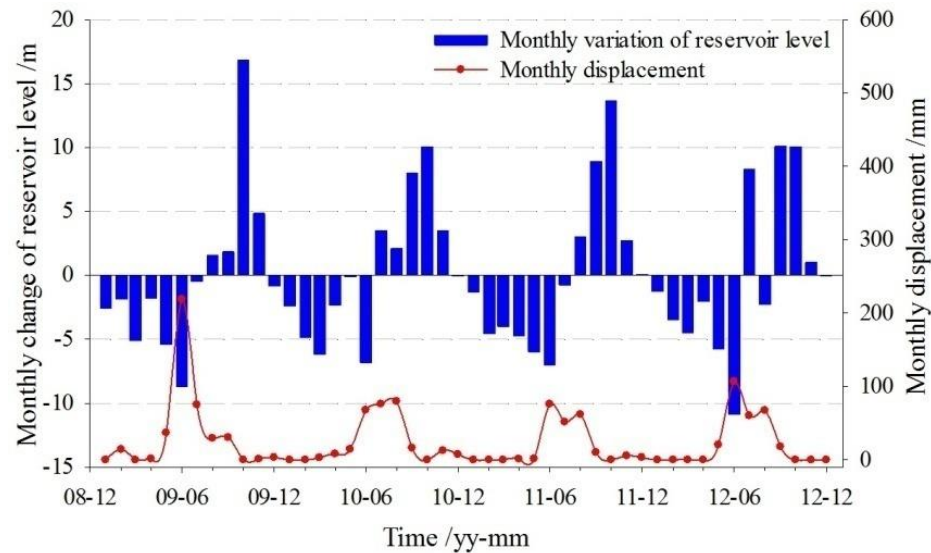
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**Fig. 12** The relationship between antecedent rainfall and the displacement of XD-01

269 The macroscopic deformation of the Baishuihe landslide occurred at the beginning of the TGRA  
270 impounding in 2003 (Table 1 and Fig. 8). The influence of the reservoir level fluctuation on landslide deformation  
271 mainly took place during the water level decline period (Fig. 13); the faster the reservoir level was descending, the  
272 greater the landslide deformed (Tang et al. 2015; Sun et al. 2017). For example, in May 2009, the landslide



273 deformed 36mm when the reservoir level dropped 5.3m; under the similar precipitation condition in June 2009, the  
 274 landslide displacement was 218mm when the reservoir level dropped 8.7m (Fig. 13). Moreover, landslide  
 275 deformation varies with different elevations of reservoir level as well (Ren et al. 2015; Zhou et al. 2016). Hence,  
 276 the variation rate and average elevation of reservoir level in the current month were applied as inputs to represent  
 277 the effect of reservoir scheduling on landslide deformation (Table 3).



278  
 279 **Fig. 13** Relationship between the displacement and reservoir water level variation

280 The current kinematic state of a landslide is another important factor for its dependence from external factors  
 281 (Crozier 1986). Under varied evolution states, the response of landslide deformation to external triggering factors is  
 282 totally different. For example, when the landslide is under stable conditions, even a strong precipitation may only  
 283 cause slight deformation. In contrast, when the landslide is under an unstable evolution state, a slight precipitation  
 284 may break the equilibrium of the original system and cause a sharp acceleration (Glade et al. 2005). Therefore, the  
 285 displacement over the past 1, 2 and 3 months were adopted as inputs to represent the current evolution state (Zhou  
 286 and Yin 2014) (Table 3).

287 **Table 3.** Inputs for periodic displacement modelling

Factors	Inputs 1-7
Precipitation	Input 1: the one-month antecedent rainfall
	Input 2: the two-months antecedent rainfall
Reservoir level	Input 3: the variation speed of reservoir level of the current month
	Input 4: the average elevation of reservoir level in the current month
Evolution state	Input 5: the displacement over the past 1 month
	Input 6: the displacement over the past 2 month
	Input 7: the displacement over the past 3 month



288 **4.5.2 Modelling and prediction of periodic displacement**

289 Based on the deformation analysis of Baishuihe landslide, seven causal factors were taken as inputs, and the  
 290 periodic displacement was considered as the output. As with the modelling of trend displacement, the monthly  
 291 displacement from January 2009 to December 2012 was used to train, and the monthly displacement from January  
 292 to December in 2013 was used for testing. Some samples of the data used in the modelling of periodic  
 293 displacement are shown in Table 4. The forecasting model of periodic displacement was established with the  
 294 application of PSO and KELM. Furthermore, in order to compare the prediction performance of multi-factor  
 295 PSO-KELM, four other methods were adopted to predict the periodic displacement, namely the single-factor  
 296 PSO-KELM, multi-factor ELM, multi-factor SVR, and multi-factor BPNN. The parameters and inputs of these  
 297 methods are shown in Table 5.

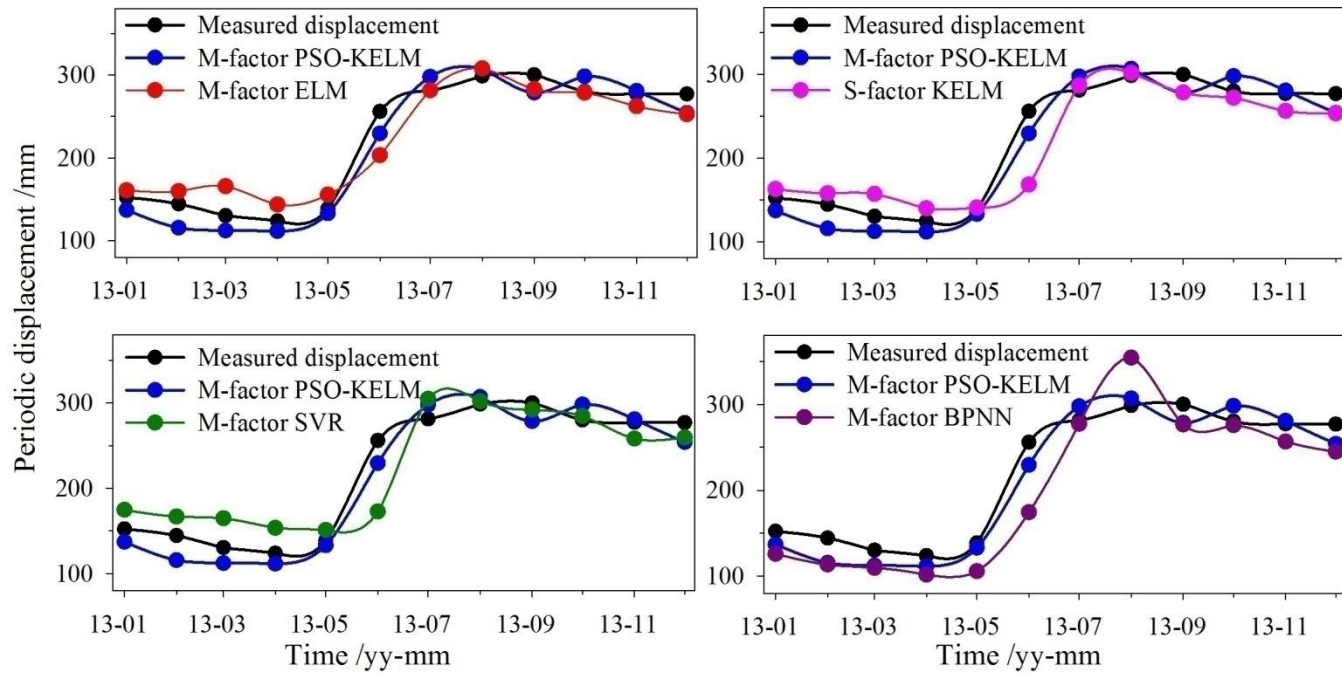
298 Table 4 Some data samples used in the modelling of periodic displacement

Time	Input 1	Input 2	Input 3	Input 4	Input 5	Input 6	Input 7	Output	Notes
Jan 2013	0.0274	0.9248	0.2519	0.0251	0.5960	0.5450	0.4890	0.4480	The detail information of inputs is shown in Table 3;
Feb 2013	0.0411	0.7715	0.1822	0.0274	0.5450	0.4890	0.4480	0.4240	
Mar 2013	0.1578	0.6259	0.2370	0.0411	0.4890	0.4480	0.4240	0.3830	Output is the periodic displacement of the current month;
Apr 2013	0.1898	0.5674	0.3019	0.1578	0.4480	0.4240	0.3830	0.3640	
May 2013	0.3729	0.4058	0.0548	0.1898	0.4240	0.3830	0.3640	0.4080	The data was normalized into the range of [0,1].
Jun 2013	0.5683	0.0556	0.1745	0.3729	0.3830	0.3640	0.4080	0.7520	

299 Table 5 The description and parameters of the five methods

Model	Description	Parameter	Notes
Multi-factor PSO-KELM	PSO-KELM model with consideration of causal factors. Inputs: input 1 ~ 7.	$c = 985.4135$ $\gamma = 0.6240$	$c$ is the regularization coefficient; $\gamma$ is the parameter of Kernel function.
Single-factor PSO-KELM	PSO-KELM model without consideration of triggering factors. Inputs: input 5 ~ 7.	$c = 133.5672$ $\gamma = 49.8052$	
Multi-factor ELM	ELM model with consideration of causal factors. Inputs: input 1 ~ 7.	$n = 15$	$n$ is the number of neurons in hidden layer.
Multi-factor SVM	SVM model with consideration of causal factors. Inputs: input 1 ~ 7.	$p = 115.0016$ $g = 0.0281$	$p$ is the penalty factor; $g$ is the parameter of kernel function.
Multi-factor BPNN	BPNN model with consideration of causal factors. Inputs: input 1 ~ 7.	$m = 20$ $a = 0.9$ $r = 0.05$	$m$ is the number of neurons in hidden layer; $a$ is the momentum; $r$ is the learning rate.

300 As shown in Fig. 14 and Table 6, the predicted values of the five models show high agreement with the  
 301 measured values. However, the single-factor PSO-KELM, multi-factor ELM, SVR, and BPNN did not perform  
 302 well during the step-like deformation period. The performance criteria indicates that the multi-factor PSO-KELM  
 303 achieved the best performance with RMSE, MAPE and R values of 18.104, 0.083 and 0.983, respectively.



**Fig. 14** The predicted and measured values of periodic displacement (M-factor means multi-factor, and S-factor means single-factor)

304  
305  
306

307

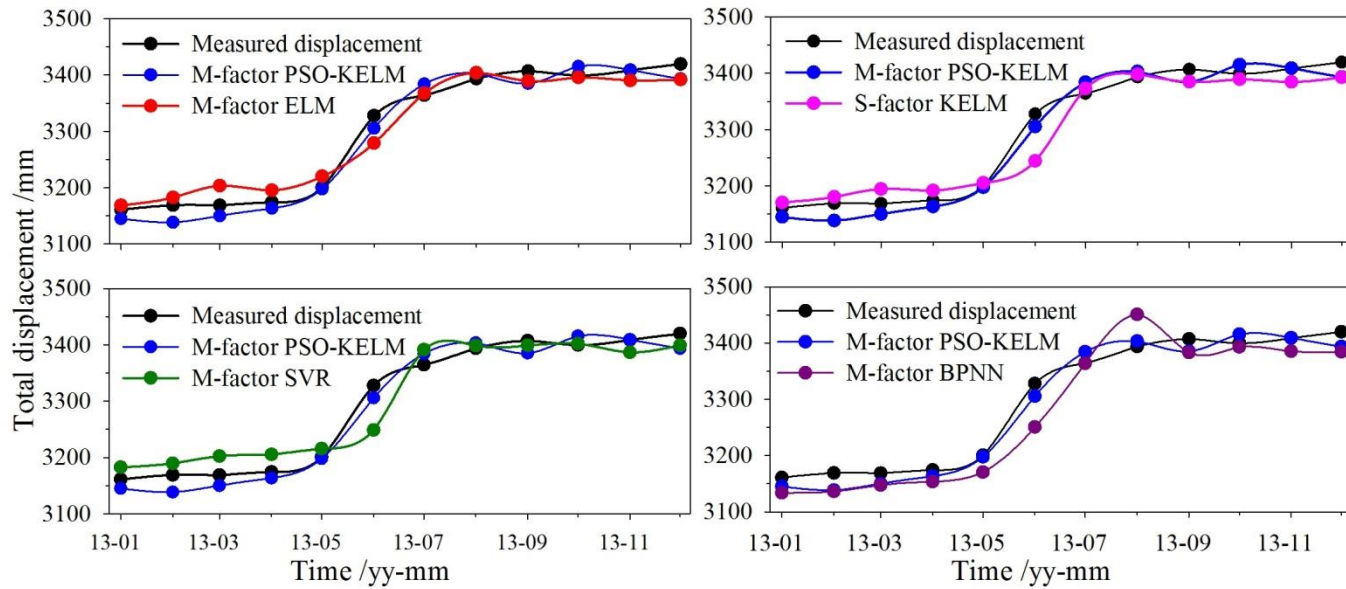
Table 6 The prediction accuracy of periodic displacement

Models	RMSE	MAPE	R
Multi-factor PSO-KELM	18.104	0.083	0.983
Single-factor PSO-KELM	29.572	0.095	0.918
Multi-factor ELM	22.761	0.096	0.958
Multi-factor SVR	32.087	0.125	0.906
Multi-factor BPNN	34.515	0.147	0.943

#### 308 4.6. Prediction of total displacement

309 The predicted total displacement was obtained by adding the predicted trend and periodic displacements  
 310 together. As stated in Section 4.4, the time series of trend displacement is smooth and can be easily predicted, so it  
 311 was predicted applying the same model of PSO-KELM. As shown in Fig. 15, the predicted total displacement of  
 312 multi-factor PSO-KELM shows the best agreement with the measured total displacement, while the RMSE, MAPE  
 313 and R are 18.418, 0.494% and 0.991, respectively (Table 7). Furthermore, during the step-like deformation,  
 314 multi-factor PSO-KELM shows excellent prediction performance as well. For example, jointly affected by heavy  
 315 precipitation and decreasing of reservoir level, Baishuihe landslide deformed sharply in June 2013, and the  
 316 multi-factor PSO-KELM achieved precise prediction by establishing the accurate response relationship between  
 317 triggering factors and deformation, the APE of the predicted value is only 0.670% (Fig. 16). The four compared  
 318 methods also performed well most of the time, but all of them achieved less accurate prediction in the crucial

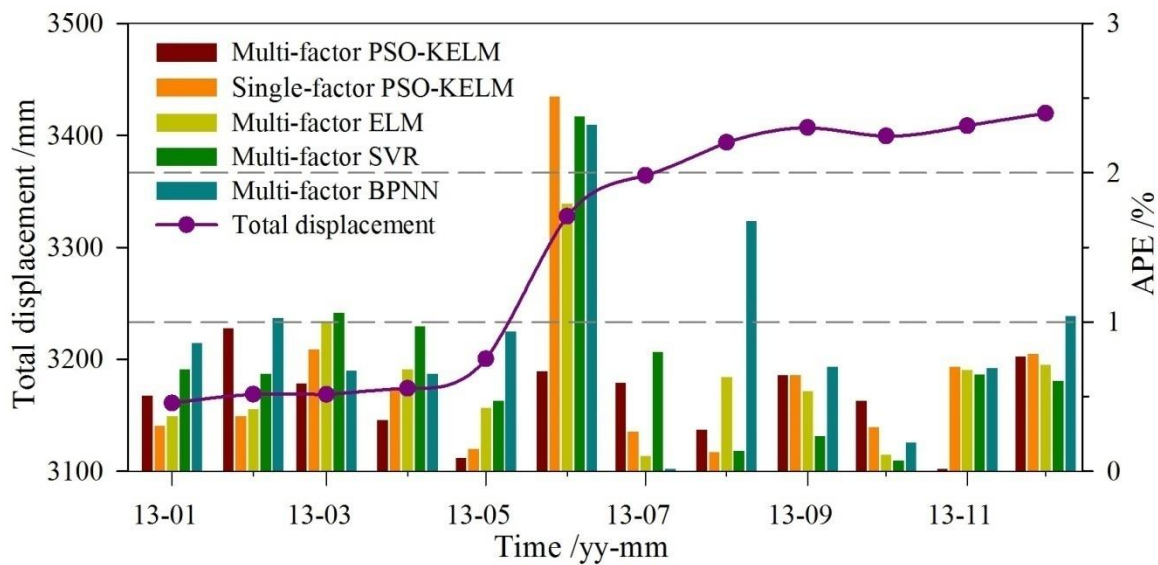
319 period of step-like deformation. For the predicted displacement of June, the APE of signal-factor PSO-KELM and  
 320 multi-factor ELM, SVR, BPNN are 2.511%, 1.463%, 2.448% and 2.323%, respectively (Fig. 16).



321  
 322 **Fig. 15** The predicted and measured values of total displacement (M-factor means multi-factor, and  
 323 S-factor means single-factor)

324 **Table 7** The prediction accuracy of total displacement

Models	RMSE	MAPE	R
Multi-factor PSO-KELM	18.418	0.494%	0.991
Single-factor PSO-KELM	29.125	0.626%	0.969
Multi-factor ELM	22.709	0.574%	0.984
Multi-factor SVR	31.910	0.777%	0.965
Multi-factor BPNN	35.628	0.899%	0.971



325  
 326 **Fig. 16** The error comparison of the five methods

## 327 **5. Discussion**

### 328 **5.1. Early warning application**

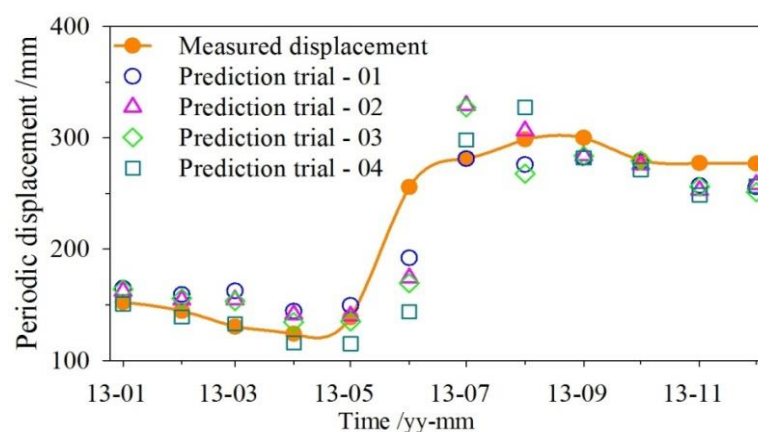
329       Landslide prediction is an important component of early warning system which is essential for landslide  
330 prevention and mitigation (Sassa et al. 2009; Intrieri et al., 2013; Mazzanti et al., 2015; Intrieri and Gigli 2016). ML  
331 methods and in general all data-based predictive models (such as those cited in the introduction section) use past  
332 monitoring data as the foundation for their forecast. To monitor a phenomenon's parameter, a longer time series  
333 (preferably at least 1 year) allows to better express its whole variability and complete range of behaviors, such as  
334 seasonal oscillations, level of noise and trend. A slope collapse is usually an unprecedented event characterized by  
335 peaks in deformation rate and acceleration. It typically represented by the maximum values in the time series. If  
336 ML methods do not have a precedent history of such events to train with, it is not possible to forecast them and  
337 therefore to provide a time of failure. **Furthermore, the output of such models is not a time (of failure) but a**  
338 **displacement value, underlying that their purpose is not directly to provide an estimation of the moment of collapse**  
339 **of a landslide.**

340       Nonetheless, the predictive capacities of models such as the PSO-KELM can still be useful in an early  
341 warning perspective. In fact, predicted displacements can be used to set warning thresholds (Crosta and Agliardi  
342 2012) and to recognize when the landslide undergoes an unpredicted acceleration that can therefore be considered  
343 anomalous and trigger the necessary early warning procedures. **For example, such models can detect anomalous**  
344 **displacements relatable with the initiation of the tertiary creep stage (Fig. 1a). At that point, time of failure**  
345 **forecasting methods (Saito, 1969; Fukuzono, 1985; Mufundirwa et al., 2010) could be run in parallel until either**  
346 **the collapse occurs or the landslide reaches a new equilibrium.** The same application was envisaged by Carlà et al.  
347 (2016) and Miao et al. (2018) using similar approaches. Such method permits to overcome the setting of thresholds  
348 based only on expert judgement but has a major drawback of requiring a long time series of monitoring data.

### 349 **5.2. Performance of PSO-KELM and future developments**

350       **By comparing the multi-factor ELM, SVR and BPNN, it is found that the prediction capacity of ELM is better**  
351 **than SVR and BPNN, that is agreed with the previous scientific literature (Lian et al. 2014; Cao et al. 2016; Huang**  
352 **et al. 2017).** However, in the application on landslide displacement prediction, one drawback of the ELM is that the  
353 prediction results vary with its random connection weight between the input and the hidden layer. As shown in Fig.

354 17, although the inputs and parameter of the ELM are the same, 4 sets of predicted periodic displacements are  
355 different, especially in the step-like deformation period. ELM can achieve accurate predictions, but inaccurate  
356 predictions occur sometimes, with the risk of misleading the decisions of disaster managers. In order to avoid the  
357 random factor within the prediction process, kernel learning was introduced into ELM, and the KELM was  
358 proposed. In this study, the hybrid model of PSO-KELM was applied in landslide displacement prediction.  
359 Moreover, compared the prediction results of the multi-factor PSO-KELM and ELM (Fig. 15 and 16), we can find  
360 that the PSO-KELM has a stronger prediction capacity.



361  
362

**Fig. 17** The prediction accuracy comparisons between different trials of ELM

363 As shown in Fig. 15 and 16, compared with the multi-factor PSO-KELM, the single-factor PSO-KELM  
364 performed worse in the step-like deformation period. The sharp increase of the displacement plays a significant role  
365 in the evolution process of the step-like landslide, the speed and increase of which are controlled by the triggers  
366 (the precipitation and the reservoir fluctuation). The single-factor PSO-KELM method cannot simulate the  
367 relationship between the deformation and the triggers, that is the reason why the large difference exists. Hence, in  
368 order to achieve accurate prediction in the step-like deformation period, the triggering factors should be considered.

369 Landslide displacement prediction can be implemented accurately by integrating the application of ML  
370 technique and engineering geology. However, the cost of some professional monitoring devices, such as GPS,  
371 clinometers et al. may limit the application of the proposed model. The development of satellite radar  
372 interferometry provides effective methods to solve this tough problem. In future studies, open-access satellite data  
373 (such as Sentinel-1) and advanced InSAR time series processing techniques will be applied to extract landslide  
374 deformation information, which can be used as basic data to achieve economic and effective landslide prediction.

## 375 **6. Conclusions**

376 The Baishuihe landslide in the TGRA has a typical step-like deformation behavior. It experiences sudden  
377 accelerations from April to September under the combined influence of precipitation and reservoir water level  
378 variation, while it is almost stable during the rest of the year. The landslide is under a steady deformation state in  
379 large time scale and deforms retrogressively with the stronger deformation in the eastern and front part.

380 The sequence of the total cumulated displacement can be decomposed into trend displacement and periodic  
381 displacement by wavelet transform, while the noise component was eliminated. The trend displacement shows  
382 approximately monotonically increasing controlled by geological conditions, while the periodic displacement  
383 shows periodic fluctuations induced by triggering factors. The two displacement items were predicted by the  
384 PSO-KELM model with different inputs separately; and the predicted total displacement was obtained from the  
385 summation. The REMS, MAPE and R of the predicted result are calculated as 18.418, 0.494% and 0.991,  
386 respectively. It indicates that the proposed method can achieve excellent performance in displacement prediction.

387 The accurate prediction of periodic displacement is the key to landslide displacement prediction. In this  
388 process, the causal factors (rainfall, reservoir level and landslide evolution state) enable to simulate the response  
389 relationship between the triggering factors and landslide deformation. The prediction accuracy can be improved by  
390 considering the causal factors, especially in case of step-like deformation.

391 The PSO-KELM integrated both the advantages of PSO and KELM algorithm, where KELM has high  
392 prediction performance, and PSO can seek appropriate parameters of KELM. The multi-factor PSO-KELM can  
393 simulate the response relationship between triggering factors and landslide deformation better than the methods of  
394 multi-factor ELM, SVR and BPNN. In addition, the prediction of the PSO-KELM is found stable, that is crucial for  
395 developing a landslide early warning system.

396 Overall, the proposed method, which applies the ML techniques and landslide evolution theory, can achieve  
397 accurate and stable prediction in case of the slow and step-like deformation period. This novel method can be  
398 recommended to conduct landslide displacement prediction in the TGRA and other landslide-prone regions.

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