

Unveiling Co-evolutionary Patterns in Systems of Cities: A Systematic Exploration of the SimpopNet Model

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Abstract Co-evolutionary processes are according to the evolutionary urban theory at the center of urban systems dynamics. Their empirical observation or within models of simulation remains however relatively rare. This chapter is focused on the co-evolution of transportation networks and cities and applies high performance computing numerical experiments to the SimpopNet co-evolution model in order to understand its behavior. We introduce specific indicators to quantify trajectories of such models for systems of cities, and apply these to exhibit co-evolutionary regimes of the model. This illustrates how the systematic exploration of a simulation model can qualitatively transform the knowledge it provides.

Keywords : *Co-evolution; Networks and Territories; SimpopNet model; Model exploration; Pattern Space Exploration*

1 Introduction

1.1 Exploring models of simulation

The development of new knowledge production practices, in particular the use of simulation models to understand complex systems, has been more and more fostered by the increase in computational possibilities. [Arthur, 2015] has proposed in that sense that these trends would consist in a computational shift of science, moving progressively from analytical-based approaches to simulation-based approaches. The study of complexity is naturally not the only field of science benefiting from these technological advances, as witness for example recent progresses in computer vision thanks to deep learning techniques made efficient by intensive computing [LeCun et al., 2015], or the importance of cloud computing for processing the massive amount of data produced by the LHC detectors [Bird, 2011]. These new methods, tools and practices are however particularly suited to the study of complex systems, because among other reasons their flexibility to take into account numerous interacting heterogeneous agents composing this kind of systems. In the case of socio-technical systems, several examples of such streams of research can be given such as generative social science [Epstein, 2006], geosimulation [Benenson and Torrens, 2004], sociophysics [Galam, 2008] or econophysics [Mantegna and Stanley, 1999]. In that case, models are a crucial piece among other knowledge domains [Raimbault, 2017a] such as theoretical and empirical investigations. All knowledge domains are however complementary and often necessary, and [Raimbault, 2016a] recalls the risks of falling into blind fully computational practices.

The study of urban systems, which are a typical illustration of such complex systems [Batty, 2007], has witnessed a significant gain of knowledge from the “*liberation of modeling and simulation practices*” as [Banos, 2013] puts it. Recent developments around the evolutive urban theory [Pumain, 1997], synthesized in particular in [Pumain and Reuillon, 2017b]. Following [Banos, 2017], these efforts are the archetype of the complementarity of knowledge domains mentioned above, and have acted as a “knowledge accelerator” with a true beneficial interdisciplinary exchange between computer science and geography.

In particular, the development of new methods for model exploration such as Pattern Space Exploration algorithm [Chérel et al., 2015] or the Calibration Profile algorithm [Reuillon et al., 2015], particularly designed for the use of high performance computing, have allowed a qualitative shift in the knowledge that could be extracted from a simulation model. Several illustrations can be given. A set of parameters that are necessary and sufficient to obtain targeted stylized facts for

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the emergence of a system of cities are obtained for the SimpopLocal model [Pumain and Reuillon, 2017a]. [Arduin, 2018] obtains confidence intervals for the estimation of parameters of a non-tractable epidemiological model through the use of the Calibration Profile algorithm. [Brasebin et al., 2017] facilitates urban planning by exploring the feasible space of building envelopes under the constraints of local regulations. [Raimbault, 2018c] indirectly quantifies interactions between networks and territories through the calibration of a simulation model with a genetic algorithm. These results are obtained thanks to the use of the model exploration software OpenMOLE [Reuillon et al., 2013], which is built around three complementary axes: (i) the possibility to embed almost any model as a black box whatever the language in which it is written (as soon as it runs on a linux machine); (ii) the implementation of innovative model exploration and calibration methods; and (iii) a transparent access to high performance computing environments. These features are integrated seamlessly with the use of a specific domain specific language to compose experiment workflows [Passerat-Palmbach et al., 2017].

We consider thus that a considerable gain in knowledge can be observed, from the conceptual or thematic description of a model, to its mathematical formalization, its implementation, its systematic exploration, up to its exploration in depth with the help of specific meta-heuristics. These changes may furthermore be of a qualitative nature, in the sense that the nature of knowledge follows abrupt transitions during the advance of the investigation in this continuum.

The objective of this chapter is to illustrate the impact of these new methods in the case of a model of co-evolution between cities and transportation networks, the SimpopNet model, introduced by [Schmitt, 2014]. Our contribution is significant on the following points: (i) we provide a supplementary proof-of-concept on the role of new simulation practices, tools and methods; (ii) we introduce a set of indicators to study the behavior of simulation models for systems of cities; (iii) we establish the behavior of this particular model, in particular we assess its sensitivity to spatial initial configuration and unveil the different regimes for interactions between cities and networks it can produce.

The rest of this chapter is organized as follows: we first briefly review co-evolutionary models for systems of cities and describe the model studied. We then introduce methodological elements to study such kind of models for systems of cities, describe results of the systematic exploration, and finally discuss the implication of these.

1.2 Co-evolution within systems of cities

Co-evolution within system of cities, in the sense of complex intricate dynamics in space and time, is a central feature of the evolutive urban theory [Pumain, 2010]. [Paulus, 2004] has for example applied this concept to the study of economic trajectories of French urban areas. Evolutionary economic geography has also developed an extensive literature using this concept for spatial economic systems [Schamp, 2010], for example for the location of firms and networks [Wal and Boschma, 2011]. We use the definition of this concept proposed by [Raimbault, 2018b], which can be synthesized as the statistical existence of causal relationships within spatio-temporal niches, for which a practical characterization method uses a weak causality based on lagged correlations [Raimbault, 2017b].

Considering more precisely the co-evolution of transportation networks and territories, which is of particular interest because of potential “structuring effects” of transportation infrastructures [Pumain, 2014], some empirical investigations have been proposed by [Bretagnolle, 2003] and [Bretagnolle, 2009] for the French system of cities. The validity of these results was however recently questioned by more thorough data analysis in [Mimeur et al., 2017] and [Raimbault, 2018]. For this reason, models of co-evolution are crucial to gain further insight into this concept.

These kind of models are however rare for cities and transportation networks, as [Raimbault, 2017c] suggested that this could be due to the fact that this object of study is at the crossroad of several disciplines with different interests and underlying questions. We can give a few examples of such models (see [Raimbault, 2018b] for a more thorough review). At microscopic and mesoscopic scales, [Achibet et al., 2014] describes a model of the co-evolution of buildings and roads, whereas [Raimbault, 2018] develops a morphogenesis model coupling multi-modeling of road network growth with a reaction-diffusion model for population density. At the scale of systems of cities, [Baptiste, 2010] proposed a reinforcement co-evolution model. [Blumenfeld-Lieberthal and Portugali, 2010] has focused on topological breakdown of the network of cities. The SimpopNet model introduced by [Schmitt, 2014], is to the best of our knowledge the only co-evolution model in the perspective of the evolutive urban theory.

This last model was however not systematically explored, and the question remains if it actually produces patterns of co-evolution at an aggregated level. This makes it a good candidate for our approach. We will in the next section briefly recall the structure of this model.

1.3 Description of the SimpopNet model

We reformulate here the SimpopNet model [Schmitt, 2014], following the notations for the formalization of the interaction model introduced by [Raimbault, 2018c], since a certain number of parameters and processes are similar. Cities grow following a specification for their populations $\mu_i(t)$ such that

$$\mu_i(t+1) - \mu_i(t) = \mu_i(t) \cdot \frac{d_G^{\gamma_G}}{N} \sum_j \frac{V_{ij}}{\langle V_{ij} \rangle} \quad (1)$$

where the potential V_{ij} is of the form

$$V_{ij} = \mu_j / d_{ij}^{\gamma_G} \quad (2)$$

such that $V_{ii} = 0$, γ_G is a parameter for the distance decay (which gives indeed a level of hierarchy as a function of distance) and d_G a shape parameter for the decay function which gives the typical distance of interaction.

The network grows at each time step through a process that can be seen as a potential breakdown (as described by [Raimbault, 2018b]):

1. two cities are chosen, the first according to populations with a hierarchy γ_N (i.e. with a probability proportional to $\mu_i^{\gamma_N}$) and the second following interaction forces $\mu_i \mu_j / d_{ij}^{\beta}$ with the same hierarchy γ_N ;
2. a link is then created if the network is not efficient enough given a threshold parameter θ_N , i.e. if $d_{ij} / d_{ij}^{(N)} > \theta_N$;
3. the links created at a date t have a speed $v(t)$, which will depend on current transportation technologies;
4. a creation of new intersections to yield a planar graph is done, but only for links with a similar speed.

In order to study a stylized version of the model, we consider a configuration such that $v(t > 0) = v_0$ and $v(0) = 1$ (the initial model considers three values for speed that correspond to the reality of transportation technologies between 1830 and 2000). Indeed, the initial precision in the parametrization of dates and speeds makes it a hybrid model, and should correspond to an application on a real spatial configuration. In a synthetic configuration as used in the model, these parameters have a sense only if we know the behavior of simulated dynamics, and in particular the role of the spatial configuration, i.e. if we are able to differentiate effects linked to the dynamics from effects linked to the initial spatial configuration.

2 Methods

2.1 Generation of synthetic setup configurations

An important aspect for studying the behavior of such a simulation model is the role of the initial spatial configuration in emerging patterns observed. We therefore apply the methodology developed by [Cottineau et al., 2017], which allows to extend the sensitivity analysis of a model to spatial meta-parameters (in our case a meta-parameter is a parameter allowing to generate an initial configuration upstream of the model).

A synthetic system of cities is constructed the following way (see [Raimbault, 2016b] for the notion of synthetic data, calibrated at the first and the second order). A fixed number N of cities is uniformly distributed in space, under the constraint of a minimal distance between each, and their population is attributed following a rank-size law which parameters P_m and α can be adjusted (the distribution of city sizes in the original model corresponds to $\alpha \simeq 0.68$ with $R^2 = 0.98$).

A skeleton of network is created by progressive connection (similar to a percolation algorithm): the algorithm connects cities two by two by closest neighbour in terms of euclidian distance, and then iteratively selects randomly a cluster and connects it perpendicularly to the closest link outside the cluster. The network is then extended by the creation of local shortcuts, through a repetition n_s times of the random selection of a city with a probability proportional to populations, and its connection to a random neighbour in a radius r_s under conditions of a maximal degree d_s . The final network is then made planar.

This process creates networks that visually correspond (in terms of the order of magnitude of the number of loops, and their spatial range) to the initialization of the model, knowing that a single instance of the network does not allow to determine distributions of topological parameters for which a more precise calibration could be done. We show in Fig. 1 examples of synthetic setups compared to the original model setup.

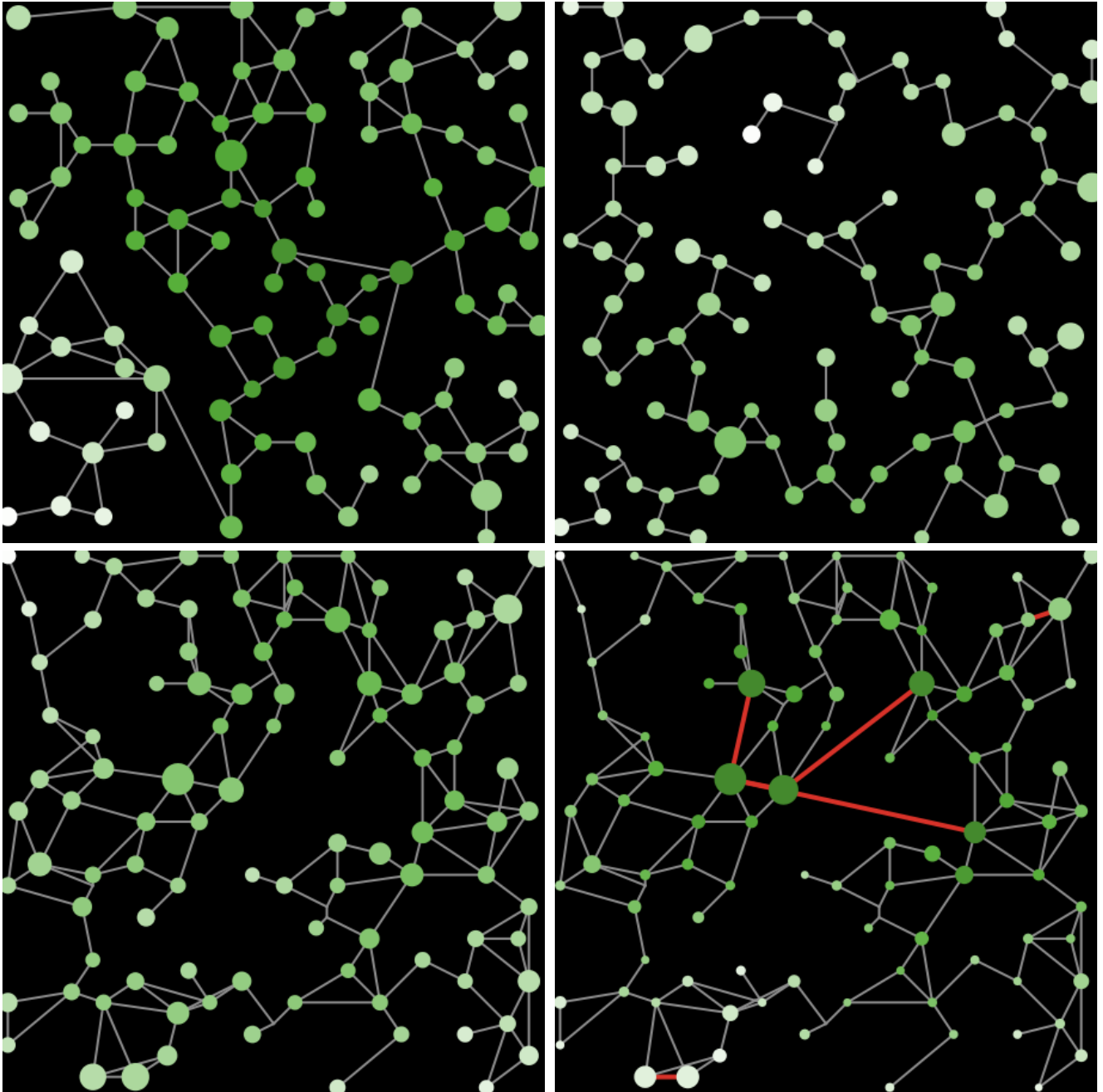


Fig. 1 Examples of model setup. (*Top Left*) Unique stylized setup provided in the original implementation of the model [Schmitt, 2014]; (*Top Right*) Example of a synthetic setup (generator parameters $N = 100$, $\alpha = 0.8$, $P_m = 1.57e5$, $n_s = 10$, $r_s = 7$, $d_s = 5$) with a network close to a tree, obtained with a very low number of shortcuts; (*Bottom Left*) Example of a synthetic setup (generator parameters $N = 100$, $\alpha = 0.8$, $P_m = 1.57e5$, $n_s = 70$, $r_s = 8$, $d_s = 5$) with a higher number of local connections; (*Bottom Right*) Outcome of the model after $t_f = 100$ time steps on the second synthetic configuration. City size gives the population and color the closeness centrality.

2.2 Indicators for trajectories of systems of cities

2.2.1 Context

A crucial aspect of the study of simulation models is the definition of relevant indicators, particularly in the case of synthetic models where it is not possible to produce outputs that are directly linked to data for example. Very general stylized facts, as aiming at producing an urban hierarchy or a network hierarchy, are relatively limited. Moreover, the hierarchy is mechanically produced by most models including aggregation processes. We therefore need more elaborated indicators to understand the dynamics of the system. These indicators must in particular give elements of answer to the following questions:

- types of systems of cities produced by the model;
- change in time of the organization of the system of cities;
- typical profiles of trajectories;
- ability to “produce some co-evolution”.

In order to concentrate on the ability of the model to produce trajectories that are both diverse and complex, and for example its ability to produce bifurcations that would manifest as inversions in ranks, and also its ability to capture different aspects of co-evolutionary dynamics, we propose a set of indicators, including for example lagged correlation measures in the spirit of causality regimes introduced by [Raimbault, 2017b], or a correlation measure as a function of distance, to understand the role of spatial interactions in the coupling of trajectories.

2.2.2 Indicators

Given a variable $X_i(t)$ defined for each city and in time (that will be the population or centrality measures for example), we define the following indicators.

Summary statistics

Simple but crucial indicators characterize the distribution of X_i in time:

- hierarchy (slope of the least squares adjustment of X_i as a function of rank) $\alpha(t)$
- entropy of the distribution $\varepsilon(t)$
- descriptive statistics (average $\mathbb{E}[X](t)$ and standard deviation $\hat{\sigma}(t)$)

Rank correlation

The rank correlation between the initial time and the final time, which translates the quantity of change in the hierarchy during the evolution of the system, and is defined by

$$\rho_r = \hat{\rho} [rg(X_i(t=0)), rg(X_i(t=t_f))] \quad (3)$$

where $rg(X_i)$ is the rank of X_i among all values (similar to a Spearman rank correlation).

Diversity of trajectories

The diversity of trajectories $\mathcal{D}[X_i]$ captures a diversity of time series profiles for the considered variable. With $\tilde{X}_i(t) \in [0; 1]$ the trajectories that have been individually rescaled, it is defined by

$$\mathcal{D}[X_i] = \frac{2}{N \cdot (N-1)} \sum_{i < j} \left(\frac{1}{T} \int_t (\tilde{X}_i(t) - \tilde{X}_j(t))^2 \right)^{\frac{1}{2}} \quad (4)$$

The L2-norm can be generalized by any Minkovski distance, as done in [Raimbault et al., 2014]. More elaborated indices for this aspect could imply the use of specific time-series clustering techniques [Liao, 2005].

Shape of trajectories

We quantify the shape of temporal trajectories through the changes in direction of these $\mathcal{C}[X_i]$, that we take as the number of local extrema, detected by a change of sign of the derivative. In the context of such a type of model, which mainly produces monotonous trajectories, this indicator witnesses in a certain way of a “complexity” of trajectories. In the case of more elaborated shapes, measures such as permutation entropy would be better candidates [Scarpino and Petri, 2017].

Distance correlations

We also introduce the correlations as a function of distance, to understand the way the effect of distance is translated at the macroscopic scale. The profile of this function, regarding interaction distance parameters included in the model, will translate the tendency of the model to lead to the emergence of one level of interaction or the other. It is computed as

$$\rho_d = \hat{\rho}[(X(\mathbf{x}_k), Y(\mathbf{x}_{k'}))] \quad (5)$$

where X_i, Y_i are the two variables considered and (k, k') the set of couples such that $\|\mathbf{x}_k - \mathbf{x}_{k'}\| - d \leq \varepsilon$ with ε a tolerance threshold (in practice taken to regroup couples by distance deciles).

Lagged correlations

Lagged correlations between the variations of variables, to identify causality patterns between variables X and Y . The patterns $\hat{\rho}_\tau$ for all variables, and for τ lag or anticipation, must be understood in the sense of potential regimes, explored by [Raimbault, 2017b].

$$\rho_\tau = \hat{\rho}[\Delta X(t - \tau), \Delta Y(t)] \quad (6)$$

2.2.3 Variables

These indicators are used in our case on the following variables:

- populations $\mu_i(t)$,
- closeness centralities

$$c_i(t) = \frac{1}{N-1} \sum_{i \neq j} \frac{1}{d_{ij}(t)}$$

which capture the position within the urban system,

- accessibilities

$$X_i = \frac{1}{\sum_k \mu_k} \sum_{i \neq j} P_j \exp(-d_{ij}(t)/d_G)$$

which capture the insertion within the urban system.

They capture both city trajectories, network trajectories, and the coupling of both with accessibility. The application of above operators to these state variables will thus inform on trajectories of cities, trajectories of the network and trajectories of their coupling, whereas operators based on correlations will inform on interactions between the two aspects.

3 Results

3.1 Model implementation

We modified and extended the NetLogo implementation of the model provided by [Schmitt, 2014], to include in particular (i) methods for the synthetic setup; (ii) indicators described above; (iii) methods for the inclusion within OpenMOLE experiments. The modified code with exploration scripts are available on the open git repository of the project at <https://github.com/JusteRaimbault/CityNetwork/tree/master/Models/Reproduction/SimpopNet>.

3.2 Experience plan

Given an initial spatial configuration (i.e. a value of meta-parameters for the initial city system and network generator), we establish the behavior of indicators by exploring a grid of the parameter space. The number of parameters being relatively and the objective being a first grasp of the model behavior, in particular if it is able to produce co-evolution dynamics, we do not use more elaborated exploration methods. The parameters are $(d_G, \gamma_G, \gamma_N, \theta_N, v_0)$ and the meta-parameters $(N_S, \alpha_S, d_S, n_S)$. We take also the meta-parameters into account in order to understand the sensitivity of the model to space.

We explore a grid of 16 configurations of meta-parameters (see Table 1 for all values), 324 configurations of parameters (such that $d_G \in [0.001, \dots, 0.016]$ by 0.005, $\gamma_G \in [0.5, \dots, 2.5]$ by 1.0, $\gamma_N \in [0.5, \dots, 2.5]$ by 1.0, $\theta_N \in [1.0, \dots, 21.0]$ by 10.0 and $v_0 \in [10.0, \dots, 110.0]$ by 50.0), and 30 random replications, what corresponds to 155520 simulations. They are executed on a computation grid with the intermediary of OpenMole. Simulation results are available at <http://dx.doi.org/10.7910/DVN/RW8S36>.

3.3 Convergence

Since the model is stochastic, it is important to control the convergence of indicators, that will be more or less easy depending on their variability. To quantify the variability of an indicator X regarding stochasticity, we use a measure similar to the one used by [Raimbault, 2018a], given by $v[X] = \hat{\mathbb{E}}[X] / \hat{\sigma}[X]$ with basic estimators for the expectancy and the standard deviation. On the full set of replications, we obtain for all indicators given previously, a median for the ratio $v[X]$ estimated within the 30 replications, estimated on all parameter values, which takes a minimal value of 3.94, for the average accessibility at final time, what witnesses a low stochastic variability. We can furthermore use this value to estimate the level of convergence: it corresponds to a 95% confidence interval around the mean of relative size 0.18 (under the assumption of a normal distribution of the average), i.e. a good convergence. This aspect is crucial for the robustness of results, as this experiment shows that working with this number of repetitions and aggregate averages is consistent.

3.4 Sensitivity to spatial initial conditions

We quantify the sensitivity to spatial initial conditions by using the definition of the relative measure of sensitivity, given by [Cottineau et al., 2017]. This measure is for two phase diagrams f_1, f_2 and d euclidian distance,

$$\tilde{d} = 2 \cdot \frac{d(f_1, f_2)}{(\text{Var}[f_1] + \text{Var}[f_2])} \quad (7)$$

Table 1 gives values of \tilde{d} for the 16 configurations of meta-parameters. These are given in comparison to an arbitrary reference configuration (first column). The hierarchy within the initial system of cities appears as the stronger determinant of variability, since all configurations with $\alpha_S = 1.5$ give values larger than 1.7, what witnesses a very strong sensitivity relative to this hierarchy.

Then, the number of cities plays a non negligible secondary role, giving the stronger effects of space. Thus, it is crucial to keep in mind this role of the initial configuration during the analysis of phase diagrams. To stay within the same spirit than the model that was initially proposed, we will however comment a phase diagram for a given spatial configuration. The study of the extended model with integration of meta-parameters to which it is sensitive at their full extent is however beyond the reach of this first analysis.

Table 1 Sensitivity to space of the SimpopNet model. Each column corresponds to an instance of the phase diagram, for which meta-parameters are given, with the relative distance to an arbitrary reference diagram. As inputs we have the meta-parameters N_S, α_S, d_S, n_S and as outputs of simulations the distance \tilde{d} .

N_S	40	40	40	40	40	40	40	40	80	80	80	80	80	80	80	80
α_S	0.5	0.5	0.5	0.5	1.5	1.5	1.5	1.5	0.5	0.5	0.5	0.5	1.5	1.5	1.5	1.5
d_S	5	5	10	10	5	5	10	10	5	5	10	10	5	5	10	10
n_S	10	30	10	30	10	30	10	30	10	30	10	30	10	30	10	30
\tilde{d}	0	0.05	0.26	0.21	1.79	1.80	1.79	1.72	0.44	0.36	0.42	0.42	2.25	2.23	2.24	2.21

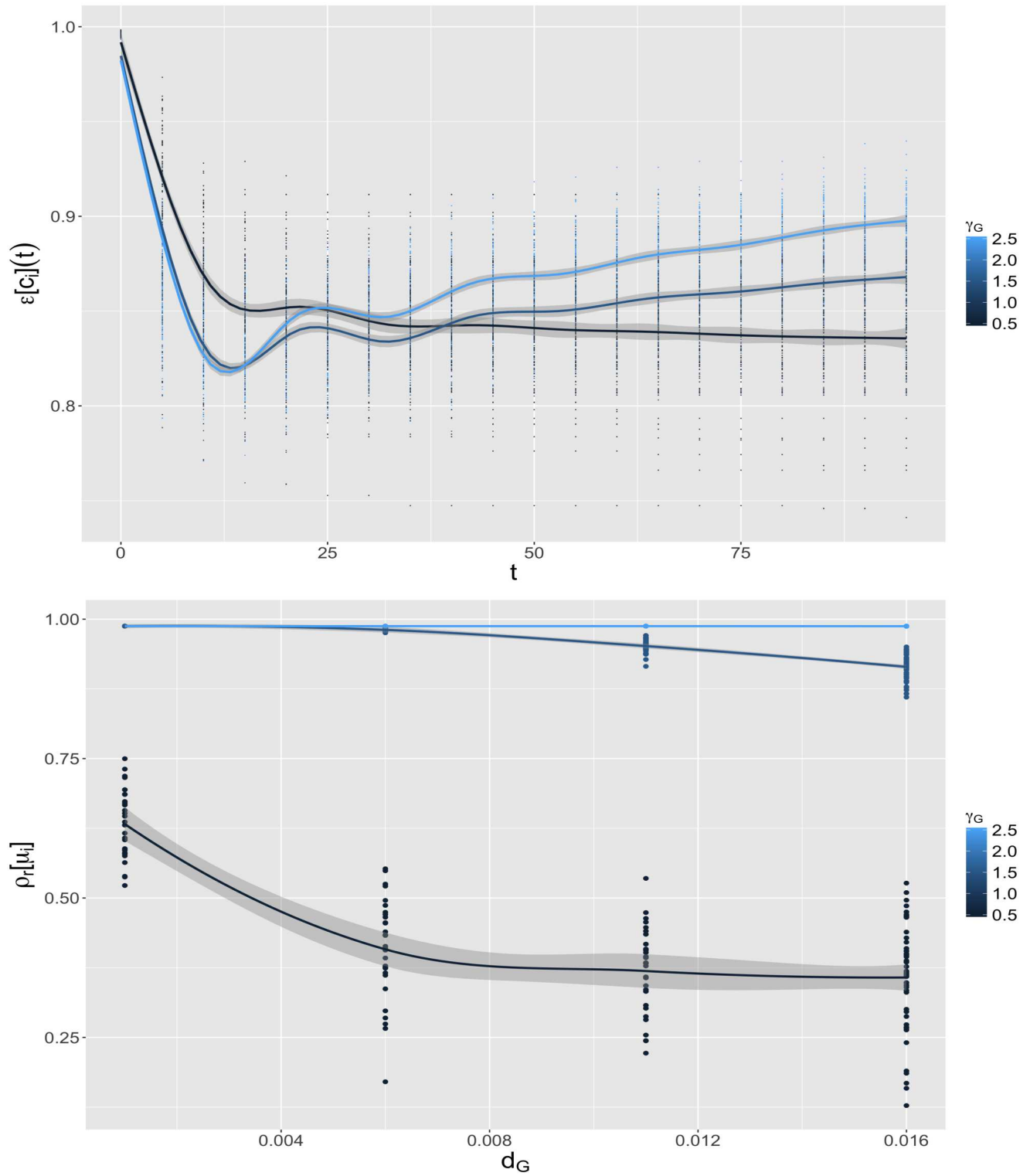


Fig. 2 Model behavior for the spatial configuration $N_S = 80, \alpha_S = 0.5, d_S = 10, n_S = 30$. (Top) Temporal trajectories of the entropy for closeness centralities, for $\gamma_N = 2.5, \nu_0 = 110, d_G = 0.016, \theta_N = 11$, as a function of γ_G (color); (Bottom) Rank correlation for population, as a function of d_G and of γ_G (color), for $\theta_N = 11, \gamma_N = 2.5$.

3.5 Model behavior

The Fig. 2 reports the behavior of the model according to a selection among the diverse indicators given above. We comment a particular spatial configuration which corresponds to a low hierarchical system with a network having only local shortcuts, given by meta-parameters $N_S = 80$, $\alpha_S = 0.5$, $d_S = 10$, $n_S = 30$, which are the values giving configurations that are the most similar to the one of the original model. More exhaustive plots for this parameter configuration are available in [Raimbault, 2018b] (Appendix A.7).

The values taken by the entropy for centralities (first panel of Fig. 2), as a function of time, for $\gamma_N = 2.5$ and $v_0 = 110$, exhibit different regimes depending on d_G and γ_G . A low hierarchy leads to an entropy stabilizing in time, what corresponds to a certain uniformization of distances. On the contrary, a strong hierarchy produces a regime with a minimum, and then an increase of disparities in time. More hierarchical interactions produce more hierarchical systems on the long terms, what could have been naturally expected, but with a transient behavior in which the system goes through a point with a maximum of equality between cities in terms of centralities. This confirms that taking into account dynamics in systems of cities is crucial for their understanding.

This variety of behaviors can be found again with the rank correlation ρ_R , that we show here for the population variable, as a function of d_G . It has a low sensitivity to θ_N and γ_N (see [Raimbault, 2018b], Appendix A.7), but strongly varies as a function of d_G and γ_G as shown in Fig. 2 (second panel): interactions at a higher distance induce systematically a larger number of changes in the hierarchy of populations. These can occur when the hierarchy of distance is low. To summarize, the increase of the range of interactions will diminish the inertia of trajectories of the system of cities, whereas the increase of their hierarchy will increase it. This is relatively credible from a thematic point of view: longer and uniform interactions have more chances to make individual trajectories change.

The behavior of correlation indicators is shown in Fig. 3. Concerning the effect of distance on correlations between variables, i.e. the evolution of ρ_d , it is interesting to note that an increase of d_G systematically diminishes the levels of correlation, what corresponds to the complexification that we previously showed. As expected, $\rho_d[d]$ decreases as a function of distance, and exhibits non zero values for the correlation between population and centrality for a high hierarchy γ_G , what shows that simultaneous adaptation regimes are rare in this model.

3.6 Causality regimes

Finally, by studying ρ_τ (Fig. 3, bottom panel), we observe that causality regimes in the sense of [Raimbault, 2017b] are relatively restrained (see [Raimbault, 2018b], Appendix A.7, for the confirmation for a broader range of parameters). The population is systematically caused by the centrality, but there exists no regime in which we observe the contrary. This is a logic of an effect of reinforcement of hierarchy by centrality. This exploration does not provide a configuration with circular causalities, and thus not a co-evolution properly speaking as we defined in the statistical sense.

3.7 PSE algorithm

The last conclusion is crucial regarding the thematic questions that one can ask to the model, and was obtained with a limited experiment (simple grid sampling). However, because precisely of non-linearities, such simple sampling may miss regions of the parameter space in which dramatic changes occurs in the phase diagram of the model, as [Chérel et al., 2015] showed on toy models and on the Marius model. We apply here therefore the Pattern Space Exploration algorithm, which is precisely designed to unveil such unexpected behavior, what can be abstracted as a sampling of the image space of the model instead of its parameter space.

We use here the following indicators as targets on which the algorithm must find diverse patterns. Given all couples of variables (X, Y) and for $\tau > 0$ and $\tau < 0$, we consider $\max_\tau \rho_\tau[X, Y]$ and $\min_\tau \rho_\tau[X, Y]$, and report the one with the largest absolute value which absolute value is larger than correlation at the origin, and 0 otherwise. This adaptation of the method of [Raimbault, 2017b] has been proposed by [Raimbault, 2018] for a similar models, for which simultaneous correlations are high as a consequence of model structure. The algorithm was run on 100 islands, with 500 parallel instances, and stopped at generation 16000.

The Fig. 4 gives the results as a scatterplot of diversity targets of the algorithm. Several regimes are located on the axis, corresponding to one-directional relations between the variables. We obtain however a point cloud within positive correlations for both negative and positive delays for population and centrality, what actually witnesses a co-evolution (circular causality

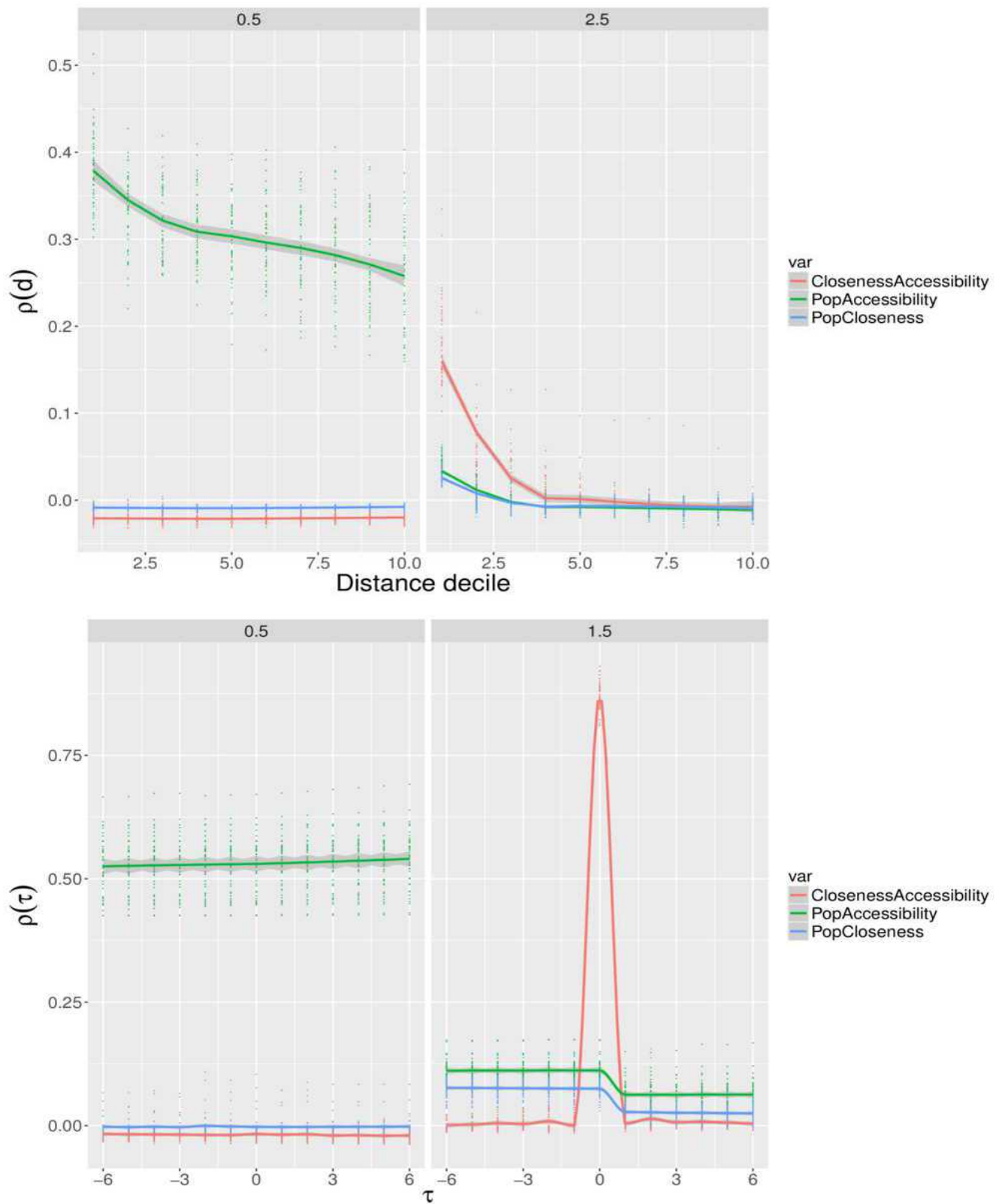


Fig. 3 Correlations in the model for the spatial configuration $N_S = 80, \alpha_S = 0.5, d_S = 10, n_S = 30$. (Top) Correlations as a function of distance, for couples of variables (color), for $\gamma_N = 2.5, \theta_N = 21, v_0 = 10$, and for d_G (columns) and γ_G (rows) variables; (Bottom) Lagged correlations for the same parameters.

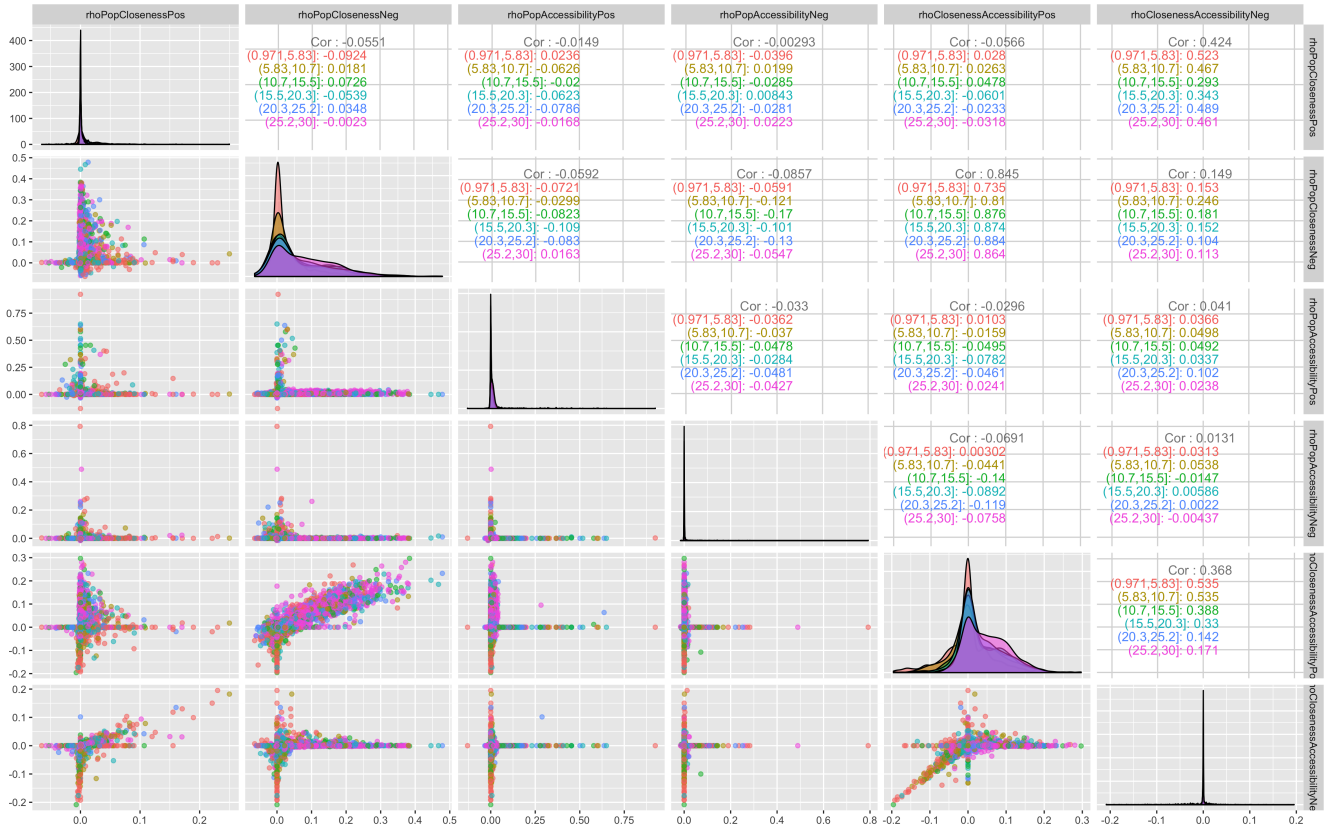


Fig. 4 Feasible space of lagged correlation obtained with the PSE algorithm. We give as a scatterplot the six objectives of the algorithm. Color level gives θ_N , which does not seem to be a simple driver of correlation values.

between the two). We have a similar pattern in negative correlations for centrality and accessibility, the point cloud being however more constrained on the diagonal, what may due to a direct repercussion of one variable on the other as they are structurally linked. We also observe points with a positive correlation between population and centrality for positive delays and negative delays, what corresponds to a direct circular causality, and between population and centrality and centrality and accessibility. This analysis reveals thus that the model is actually able to produce co-evolutive regimes in the sense of [Raimbault, 2018b].

Although the algorithm seems to have converged (less patterns discovered after generation 10000), a more thorough investigation of the role of stochasticity would be needed since several points have few repetitions, to ensure the robustness of these results. These remain out of the scope of this proof-of-concept exploration, in which we show how a qualitative change can occur in knowledge about a model when using specific exploration methods.

4 Discussion

First of all, some thematic observations about the question of interactions between networks and territories can be formulated.

This model could be a useful tool to study the “tunnel effect”, which is as we recall is the absence of interaction of an infrastructure traversing a territory with it [Raimbault, 2018c]. Indeed, the rules allowing variable values for $v(t)$ and the non-planarity mechanism (when a new link is constructed, it does create intersections only with links of similar speed), allows the introduction of this effect. This remains however exogenous since explicitly specified in model rules, on the contrary to the interaction model of [Raimbault, 2018c] with feedback of flows, in which the variations of parameters capture an endogenous tunnel effect. The introduction of specific indicators to measure it would be an interesting development direction in the case of this model.

This model could be calibrated on real systems, but the use of the interaction model without the endogenous Gibrat term would be difficultly adaptable to an application of the model on real data because of the values for calibrated for endogenous

growth for example by [Raimbault, 2018c]. The application to a real system would thus require to study the complete model first.

In comparison, the co-evolution model introduced by [Raimbault, 2018] seems to be less constrained for network dynamics and to produce more varied interaction regimes. We can not however compare the two in such different contexts. Future work to better understand the role of co-evolution in urban systems shall require multi-modeling approaches [Cottineau et al., 2015] and more systematic model benchmarks.

Regarding the modeling side, this work provides a supplementary proof-of-concept of the importance of the use of new tools and methods to extract knowledge from simulation models, since we indeed showed that the conclusion on the ability of the SimpopNet model to produce co-evolutive regimes would not have been obtained without the use of the PSE algorithm.

5 Conclusion

This chapter has illustrated the systematic exploration of a simulation model for the co-evolution of cities and transportation networks. Our contribution covers several dimensions, including a proof-of-concept of the importance of new model exploration tools and methods, a set of indicators to study similar models for systems of cities, and thematic knowledge about the model such as its sensitivity to spatial initial conditions and its ability to produce co-evolutive regimes.

Acknowledgements Results obtained in this paper were computed on the vo.complex-system.eu virtual organization of the European Grid Infrastructure (<http://www.egi.eu>). We thank the European Grid Infrastructure and its supporting National Grid Initiatives (France-Grilles in particular) for providing the technical support and infrastructure. This work is part of DynamiCity, a FUI project funded by BPI France, Auvergne-Rhone-Alpes region, Ile-de-France region and Lyon metropolis. This work was also funded by the Urban Dynamics Lab grant EPSRC EP/M023583/1.

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