

Strain and Orientation Modulated Bandgaps and Effective Masses of Phosphorene Nanoribbons

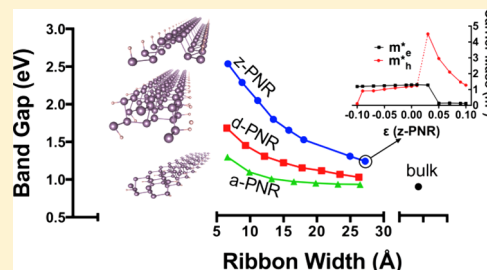
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Supporting Information

ABSTRACT: Passivated phosphorene nanoribbons, armchair (a-PNR), diagonal (d-PNR), and zigzag (z-PNR), were investigated using density functional theory. Z-PNRs demonstrate the greatest quantum size effect, tuning the bandgap from 1.4 to 2.6 eV when the width is reduced from 26 to 6 Å. Strain effectively tunes charge carrier transport, leading to a sudden increase in electron effective mass at +8% strain for a-PNRs or hole effective mass at +3% strain for z-PNRs, differentiating the (m_h^*/m_e^*) ratio by an order of magnitude in each case. Straining of d-PNRs results in a direct to indirect band gap transition at either -7% or +5% strain and therein creates degenerate energy valleys with potential applications for valleytronics and/or photocatalysis.

KEYWORDS: Phosphorene, black phosphorus, nanostructures, band structure, strain effect



One of the most critical and challenging issues facing the electronics industry is the development of alternatives to silicon-based materials so as to enable large improvement in device performance.^{1–3} Considerable efforts have been devoted to 2D materials, such as graphene,⁴ which despite promising charge transport properties is unable to function as a switch in transistor devices due to the lack of an intrinsic bandgap. To ameliorate this problem, several avenues of research have been pursued, including functionalization,⁵ nanostructuring,^{6–9} and substrate engineering.^{10,11} Results to date are inconclusive and so alternative materials are sought.

The recent exfoliation of black phosphorus,^{12,13} which consists of weakly stacked layers of a quasi-planar corrugated half-honeycomb structure, dubbed phosphorene, has garnered huge experimental and theoretical interest due to its relatively large and direct bandgap and good charge carrier mobilities.^{14–18} Presently, several open questions remain: is it possible to synthesize this material at industrial scales? What is the nature of the strongly anisotropic conducting behavior, for example, the drain current is strongly angular dependent.¹² And what are the effects of nanostructuring on the electronic and optical properties of this material?

To resolve this last question and taking inspiration from recent experimental work on the ballistic transportation of graphene nanoribbons,¹⁹ we have investigated the structural and electronic properties of phosphorene nanoribbons (PNRs).^{20,21} Realistic stable nanoribbons were considered, for example, any bonds that are cleaved are passivated with hydrogen. To our knowledge there are two other recent publications on PNRs.^{21,22} The former only considers nanoribbons with no passivating atoms that are not comparable to our system, and the latter only considers a-PNR and z-PNR structures without strain. We show that out of the three lowest

energy cleavage directions, one in particular demonstrates strong quantum size effects that increase the magnitude of the bandgap, and we show that this effect is related to the spatial extent of the valence band edge (VBE) and conduction band edge (CBE) states. The effects of strain on the transport properties of phosphorene were theoretically investigated by calculation of the hole and electron effective masses at the VBE and CBE, respectively. We identify that the charge transport properties, based on the analysis of the effective mass, can be modified by uniaxial straining of the nanoribbons, analogous to the findings for biaxial straining on phosphorene.²³ We demonstrate that both the size of the bandgap and the transport properties (e.g., electron and hole transport) of the PNRs can be extensively modified by (uniaxial) straining, allowing the tuning of the material for several applications, such as solid-state lighting, light-emitting diodes, and flat panel displays. Furthermore, our findings indicate that it is possible to tune the directness of the bandgap by uniaxial straining of a particular nanoribbon structure, and that the resulting direct and indirect bandgaps are degenerate at a given strain, potentially allowing segregation of electrons and/or holes of the same energy by momentum and for valley effects to manifest.

We have performed plane-wave electronic structure calculations within the density functional theory (DFT) using projected augmented wave (PAW) potentials to treat the core electrons. All calculations were performed using the Vienna ab initio Simulation Package (VASP).^{24,25} Unless explicitly stated otherwise, we present results using crystal lattices, geometries,

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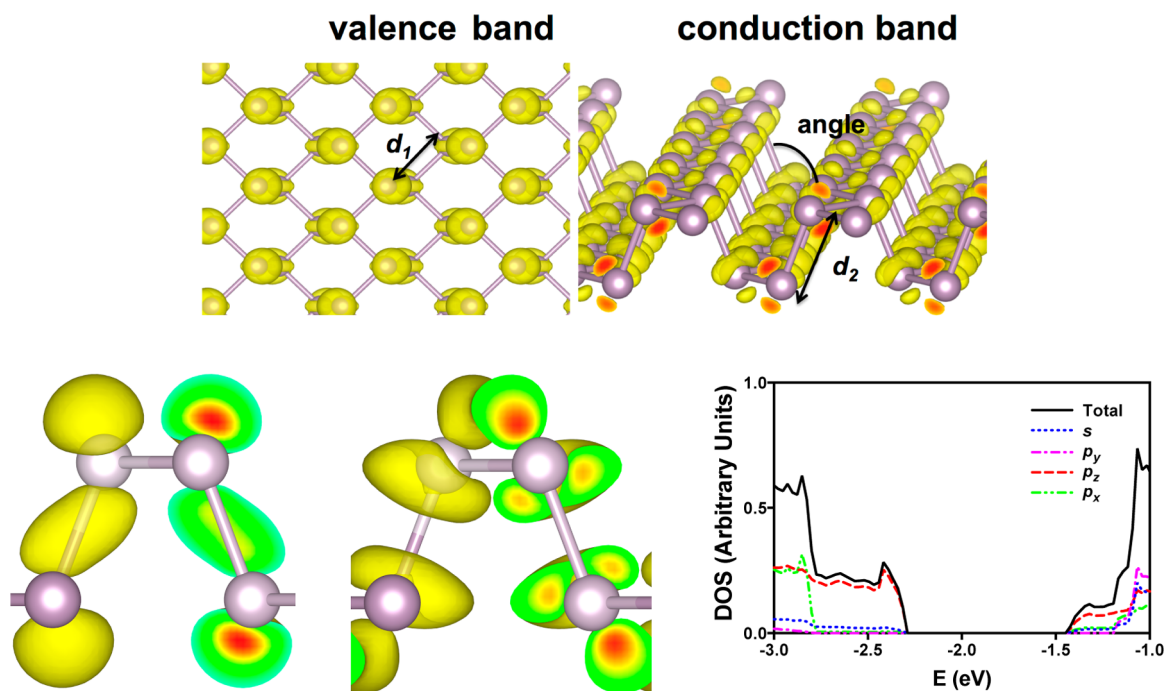


Figure 1. Atomic structure of phosphorene and partial electronic density of valence band edge (top left) and conduction band edge (top right) states (isosurface is set to $0.01 e/a_0^3$). Bottom-left figure shows side view of VBM state; bottom-middle shows the side view of CBM state (isosurface set to $0.003 e/a_0^3$); and bottom-right shows the total and partial DOSs.

Table 1. Structural Parameters, Bond Lengths and Angle, and Bandgap at Γ Point of Phosphorene

	a (Å)	b (Å)	d_1 (Å)	d_2 (Å)	angle (deg)	gap $\{\Gamma(eV)\}$
PBE	3.30	4.58	2.22	2.25	103.8	0.90
HSE06	3.28	4.54	2.20	2.23	104.0	1.55
ref 12	3.35 (PBE)	4.62 (PBE)	N/A	N/A	N/A	0.90 (PBE) 1.1 (HSE)

80 and electronic structures optimized using the Perdew–Burke–
 81 Ernzerhof (PBE) functional.²⁶ Our results for the bulk were
 82 verified using the PBEsol functional²⁷ and the HSE06 hybrid
 83 functional.²⁸ The van der Waals stacking in bulk phosphorus
 84 was treated using the DFT-D2 method of Grimme.²⁹ Kohn–
 85 Sham orbitals are expanded in a plane wave basis set with a
 86 cutoff energy of 400 eV. All systems are relaxed until all forces
 87 are less than 0.01 eV/Å. A Monkhorst–Pack mesh of $8 \times 8 \times 1$
 88 was used for single layer phosphorene, whereas for nanoribbons
 89 the k -point mesh is $7 \times 1 \times 1$. For these k -point meshes, the
 90 error is less than 1 meV per atom. For the calculation of band
 91 structures for the phosphorene sheet, we sample the following
 92 points of high symmetry: Γ , Y, and X, whereas for the ribbon
 93 we simply sample 20 points along the vector in reciprocal space
 94 that corresponds to the ribbon direction in real space. The
 95 vacuum region is set to 20 Å perpendicular to the sheet, with an
 96 additional 20 Å vacuum separating the nanoribbons.

97 Lattice parameter information for the bulk black phosphorus,
 98 calculated for PBE, PBEsol, and HSE06 functionals, are given
 99 in the Supporting Information. From the analysis of the effects
 100 of van der Waals interactions (see Supporting Information), we
 101 clarify that for bulk phosphorus it is not necessary to modify the
 102 proportion of default exchange in order to obtain good
 103 agreement with experiment. For single-layer materials, for
 104 example, phosphorene, van der Waals corrections are not
 105 relevant and so were not included. Our results need only use
 106 the HSE06 functional for an accurate description of the

electronic states of the monolayer. We also note that PBEsol 107
 does not provide an accurate treatment of the crystal structure. 108

The calculated lattice parameters and bandgap at the Γ point 109
 of a single layer phosphorene (Figure 1) are listed in Table 1. 110 fl11
 In the absence of experimental information, we can only 111
 compare results with other simulations. As expected, van der 112
 Waals corrections are insignificant for phosphorene with 113
 equilibrium bond lengths and band gaps nearly the same. 114
 The bandgap from PBE calculations is in line with ref 12, ~ 0.9 115
 eV; however, the bandgap from our hybrid functional is much 116
 higher at 1.55 eV. This difference is due to two factors: the 117
 model structure in ref 12 is from a nonhybrid PBE calculation, 118
 and their hybrid functional uses a reduced exchange 119
 contribution from the default value for the HSE06 functional. 120
 Furthermore, we note that the HSE06 functional accurately 121
 describes the bulk properties of many materials;³⁰ however, we 122
 caution that for nanostructures and surfaces hybrid functionals 123
 are not particularly accurate as they neglect the physically 124
 important enhancement of the self-interaction energy at the 125
 surface.^{31,32} This problem results in an enhancement of exciton 126
 binding energies that is not captured by density functional 127
 approaches. The influence of model structure was subsequently 128
 investigated with the hybrid functional calculation, based on the 129
 PBE structure, yielding a bandgap of 1.30 eV. 130

In comparison with the literature on GW calculations of 131
 phosphorene with bandgaps reported of 1.6 and 2.0 eV.^{18,33} our 132
 results are somewhat lower in magnitude. The underestimation 133

134 reported by DFT is due to the improper treatment of the
 135 Coulomb repulsion. However, direct analysis of the band
 136 structure indicates that the primary difference between GW and
 137 DFT calculations is simply the position of the valence and
 138 conduction band;³³ effective masses would be similar. Our DFT
 139 calculations qualitatively capture the essential features of the
 140 band structure. With the observation that there is an increase in
 141 exciton binding energies for graphene nanoribbons,³² we expect
 142 that the optical quantum size effect for very narrow ribbons will
 143 be less than predicted in our DFT calculations.

144 The energy of exfoliation of a single sheet of phosphorene
 145 was calculated using the PBE+vdW formalism. This exfoliation
 146 energy was found to be 0.339 Jm^{-2} , comparable in magnitude
 147 to that of graphene of 0.344 Jm^{-2} .³⁴

148 The spatial distribution of the conduction and valence states
 149 of phosphorene were plotted, see Figure 1. From inspection,
 150 the valence band is mostly localized toward the exterior of the
 151 sheet, whereas the conduction band is more strongly weighted
 152 toward the interior of the sheet, that is, in between the two
 153 surfaces of the sheet. This behavior reflects the nature of the
 154 DOS, wherein both the valence band maximum (VBM) and
 155 conduction band minimum (CBM) have strong contributions
 156 from the p_z orbitals; the valence band edge is bonding-like
 157 when viewed from the projection into the sheet along the
 158 zigzag direction, and the conduction band edge antibonding-
 159 like, see Figure 1.

160 The band structure of phosphorene is calculated with the
 161 PBE and the HSE06 functionals, obtained using the relevant
 162 (PBE, HSE06) crystal structure. The findings are presented in
 163 Figure 2. The differences between the band structures are

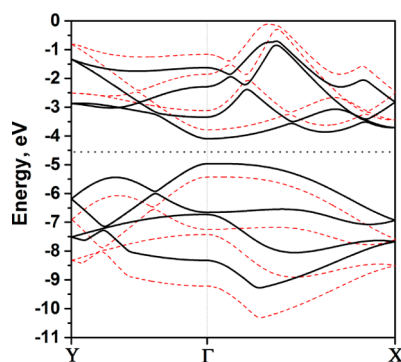


Figure 2. Calculated band structures of phosphorene, PBE structure with PBE functional (black solid line), HSE06 structure with HSE06 functional (red dash line). The zero of the y -axis is the reference level of the electrostatic potential in the middle of the vacuum region. The band structures of the two calculations were aligned using the electrostatic potential in the middle of the vacuum region.³⁵

164 mostly due to a rigid shift upward in energy of the conduction
 165 band states and downward in energy of the valence band states.
 166 Importantly, there are no major qualitative differences in the
 167 dispersion of states across the special k -points.

168 With due consideration of the structure of phosphorene,
 169 there are three evident orientations to form nanoribbons: the
 170 armchair ribbon (a-PNR) along $[100]$, the zigzag ribbon (z-
 171 PNR) along $[010]$, and a diagonal ribbon (d-PNR) along $[110]$
 172 (which is at an angle of 35.7° to the armchair direction), see
 173 Figure 3. The formation of each nanoribbon results in the
 174 breaking of one P–P bond per edge phosphorus atom. In
 175 realistic nanostructures, these edge atoms are highly reactive

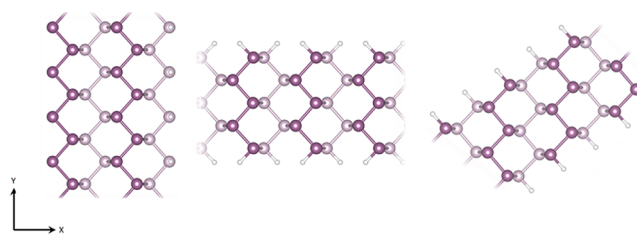


Figure 3. From left to right, z-PNR, a-PNR, and d-PNR. Axis definitions are the same as those shown in Table S1 (Supporting Information).

and will bond with impurities, especially hydrogen. Therefore,
 in our models the edges of the ribbon are passivated with
 hydrogen. In order to check for possible Peierls distortion
 effects that may modify the electronic structure by structural
 distortion,³⁶ we modeled several different lengths of nano-
 ribbon, specifically ribbons of length one, two, and four unit
 cells. No such distortions were observed. The zero temperature
 edge formation energy per unit length (E_{edge}) was calculated
 using

$$E_{\text{edge}} = \frac{1}{2L} \left(E^{\text{ribbon}} - N_{\text{P}} E^{\text{bulk}} - \frac{N_{\text{H}}}{2} E_{\text{H}_2} \right)$$

where L is the length of the nanoribbon, E^{ribbon} is the total
 energy of the nanoribbon, N_{P} is the number of phosphorus
 atoms in the nanoribbon, E^{bulk} is the energy of phosphorene per
 atom, N_{H} is the number of hydrogen atoms, and E_{H_2} is the
 energy of a H_2 molecule. Our results are shown in Table 2.

Thermodynamically these cuts are slightly exothermic for the
 zigzag ribbons, which are stable with respect to depassivation.
 However, for both the armchair and diagonal nanoribbons the
 formation edges are slightly endothermic. The order of stability
 for these nanoribbons is z-PNR > d-PNR > a-PNR. For all the
 systems, the narrower the ribbon, the harder it is to form. We
 emphasize that these formation energies refer to zero-
 temperature; we would expect elevated temperatures to favor
 hydrogen release from the edges due to the entropic factor in
 the Gibbs free energy.

The magnitude of the bandgap in each type of the
 nanoribbon increases as the ribbon's width is reduced, see
 Figure 4. This effect is similar to that observed when forming
 graphene nanoribbons³⁷ and can be attributed to the quantum
 confinement of electrons.

We see that the effect of quantum confinement when cutting
 perpendicular to the armchair direction to form z-PNRs is
 considerably greater than when cutting perpendicular to the
 zigzag direction to form a-PNR. For example, 13.5 \AA wide z-
 PNR has a bandgap of 1.83 eV , while 13.2 \AA wide a-PNR has a
 bandgap of only 1.01 eV . This finding is in line with the fact
 that the band edge states in phosphorene propagate primarily
 along the armchair direction. Furthermore, cutting phosphorene
 to form d-PNR also confines wave functions propagating in the
 armchair direction, although for a given width of ribbon the
 length scale of confinement is greater than when forming a-
 PNR and therefore the confinement effect is reduced. This
 change in bandgap originates from both an increase in energy
 of the conduction band edge, and a reduction in energy of the
 valence band edge. The bandgaps of the a-PNR structures and
 d-PNR structures are all direct, $\Gamma \rightarrow \Gamma$; however, for the z-
 PNR structures the lowest energy bandgap (by $\sim 0.005 \text{ eV}$) is
 indirect, $0.0625 \rightarrow \Gamma$.

Table 2. Number of P–P Rings, Defined as the 6-Atom Unit Cell As Illustrated by the Plane View in Figure 3, Nanoribbon Width, and Formation Energy of Ribbon Edges, for All Three Types of Nanoribbons

z-PNR			a-PNR			d-PNR		
width (rings*)	width (Å)	E_{edge} (meV)	width (rings)	width (Å)	E_{edge} (meV)	width (rings)	width (Å)	E_{edge} (meV)
11	27.2	−54	9	29.8	+55	9	26.3	+2
10	25.0	−54	8	26.5	+52	8	23.5	+2
7	18.0	−51	7	23.2	+55	7	20.7	+2
6	15.8	−49	6	19.9	+53	6	17.8	+3
5	13.5	−46	5	16.5	+55	5	15.0	+4
4	11.1	−45	4	13.2	+58	4	12.2	+6
3	8.8	−43	3	9.9	+59	3	9.3	+7
2	6.7	−32	2	6.6	+62	2	6.5	+10

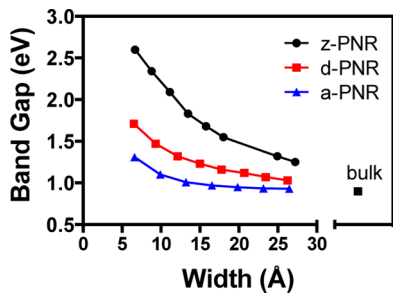


Figure 4. Variation of bandgap with respect to nanoribbon width for z-PNR, a-PNR, and d-PNR. The bulk value is also plotted.

For each type of PNRs, the bandgap was also calculated from the HSE06 functional to further verify the accuracy of the semilocal PBE functional. We found that the HSE06 bandgap was always higher than the PBE prediction. The difference of the band gaps between HSE06 and PBE calculations reduces gradually as the ribbon-width increases, varying from +0.81 eV (6.7 Å wide z-PNR), +0.68 (6.6 Å z-PNR), and +0.82 (6.5 Å d-PNR) to +0.68 eV (bulk).

The effective mass of electrons at the conduction band minimum (m_e^*) and of holes at the valence band maximum (m_h^*) were calculated using

$$m^* = \hbar^2 \left(\frac{\partial^2 E}{\partial k^2} \right)^{-1}$$

where E and k correspond to energy and the reciprocal lattice vector along the nanoribbon. These nanoribbon effective masses were compared to those of the phosphorene sheet, specifically along the equivalent directions as the nanoribbons. The error in the PBE functional effective masses was determined by comparison to effective masses calculated with the HSE06 functional for the case of phosphorene. The PBE functional underestimates by 20.4% along the armchair direction and overestimates the effective mass by 10.8% along the zigzag direction. The effective masses determined by the PBE functional are sufficiently close to those by the HSE06 functional and allow us to be confident in the trends they predict.

A simplistic model, assuming velocity is randomized after each scattering event, gives the charge carrier mobility μ as

$$\mu = \frac{q}{m^*} \tau$$

where τ is the scattering time, q is the charge, and m^* is the effective mass. Changes in effective mass can influence charge carrier transport properties. Further, if there is no change in the

time scale for quasiparticle scattering, then mobility is inversely proportional to the effective mass. However, especially for large strains, the scattering time may be altered which will then influence the mobilities. Detailed investigation of this effect is beyond the scope of this paper. Preliminary calculations on the phonon density of states show little difference for the unstretched and (+7%) stretched a-PNR structures, Supporting Information Figure S4. This would imply that, absent additional electron–phonon effects, the scattering time for unstrained and strained nanoribbons would be similar. Also, in the following discussion we note there are no significant changes in structural parameters associated with the abrupt changes in effective masses. Significant changes in effective masses would be expected to alter charge carrier transport properties.

Effective masses for the majority of the a-PNRs are very similar to those along the analogous armchair direction in phosphorene, where $m_h^* = 0.15m_0$ and $m_e^* = 0.16m_0$ (m_0 is the mass of the electron). For example, in 26.5 Å wide a-PNR, $m_h^* = 0.15m_0$ and $m_e^* = 0.17m_0$. However, for very narrow a-PNR structures the electron transport at the CBE is quenched, for example, in 9.9 Å wide a-PNR $m_e^* = 1.40m_0$. Nanostructuring along this direction can potentially affect n -type conductivity.

Similarly, effective masses along the wider z-PNR structures are comparable to those along the analogous zigzag direction in bulk phosphorene, where $m_h^* = 1.54m_0$ and $m_e^* = 1.23m_0$. For example, in 27.2 Å wide z-PNR, $m_h^* = 1.55m_0$ and $m_e^* = 1.31m_0$. However, for very narrow z-PNR structures, the hole transport at the VBM is quenched, for example, in 8.8 Å wide z-PNR $m_h^* = 5.00m_0$. Nanostructuring along this direction can potentially affect p -type conductivity.

For the d-PNR structures, the effective masses of both hole and electrons are comparable. For 26.3 Å wide nanoribbons $m_h^* = 1.03m_0$ and $m_e^* = 0.60m_0$. Unlike the other nanoribbons, nanostructuring does not strongly modify these values, for example, for the narrowest d-PNR, $m_h^* = 0.73m_0$ and $m_e^* = 0.68m_0$. Nanostructuring along this direction does not especially improve transport of either type of charge carrier.

In general, in terms of truncating the crystal lattice and maximizing charge transport (assuming there is no change in the time scale for electron scattering), a-PNR nanoribbons are best, as effective masses along this direction are smaller than in other directions, which is no doubt due to the strong p_z contributions to the VBE and the CBE. The natural direction for charge transport is through these states, and the greatest overlap between these orbitals is from one side of the sheet to the other, that is, from top to bottom, which corresponds to the armchair direction; therefore a-PNR nanoribbons, which maintain the structure along the armchair direction, are best. The effective masses for a-PNRs compare favorably with those

301 reported for graphene nanoribbons, which are of the order 0.06
302 to $0.21 m_0$.^{39,40}

303 Properties of nanoribbons may be easily modified through
304 the application of uniaxial strain. In order to investigate their
305 response to straining, we applied uniaxial strain along the
306 infinite direction of each type of PNR, calculated the in-plane
307 stiffness, and investigated the effects of straining on bandgap
308 and effective mass in order to provide insight into the charge
309 transport properties. We present results for the widest
310 nanoribbons only but similar trends hold for other nanoribbon
311 widths. We investigate strains up to a magnitude of $\pm 10\%$,
312 which is considerably less than the theoretical ultimate strain of
313 phosphorene and thus is physically realizable.^{41,42} We have
314 calculated the in-plane stiffness, C , of the different nanoribbon
315 structures. Tabulated values are given in the Supporting
316 Information. The a-PNR structures are easiest to compress,
317 the d-PNR structures are the easiest to extend. These results are
318 in line with recent studies on bulk phosphorene that found that
319 the surface tension of phosphorene under a given strain is
320 considerably lower in the armchair direction than in the zigzag
321 direction.⁴³ The values are a factor of 10 less than that reported
322 for graphene structures⁴⁴ and are due to the puckered structure
323 of phosphorene where compression or extension mainly leads
324 to P–P–P bond angle change.

325 We calculated the bandgap and effective masses of a-PNR
326 structures at strains between $\epsilon = -10\%$ and $+10\%$, see Figure 5.

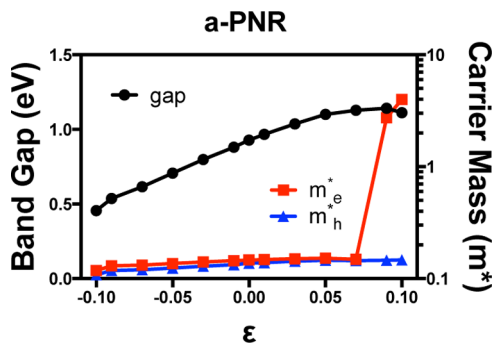


Figure 5. Variation of bandgap (shown in left axis); hole and electronic effective masses (shown in right axis) with respect to strain (ϵ) for the a-PNR.

327 Under no strain, we found that the effective mass of the hole is
328 slightly lower than that of the electron. The effect on the
329 electronic structure of stretching a-PNR between $\epsilon = -10\%$ and
330 $+8\%$ is dominated by the stabilization of the VBM, which has a
331 maxima at the Γ -point and consists of p_z orbitals that are
332 antibonding (out-of-phase) in the armchair direction, see
333 Figure 6. As the a-PNR is stretched and the antibonding p_z
334 orbitals are separated, the VBM is stabilized, lowering in energy.
335 This results in the bandgap increasing from 0.46 eV at $\epsilon =$
336 -10% to 1.16 eV at $\epsilon = +8\%$. The effective mass of this band,
337 m_h^* , also increases as the structure is stretched, rising from
338 $0.11m_0$ at $\epsilon = -10\%$ to $0.15m_0$ at $\epsilon = +10\%$. This can be readily
339 explained as a reduction in overlap between p_z orbitals as a-
340 PNR is stretched. It should also be noted that as the a-PNR is
341 compressed, a competing valence band with its maxima at $[0.5,$
342 $0, 0]$ rises in energy. At strains of $\epsilon \leftarrow 10\%$, there is a dramatic
343 change in the VBM character as the bandgap of a-PNR
344 becomes indirect from $X \rightarrow \Gamma$.

345 Meanwhile, the CBM of unstrained a-PNR consists of p_z
346 orbitals that are nonbonding in the armchair direction. The

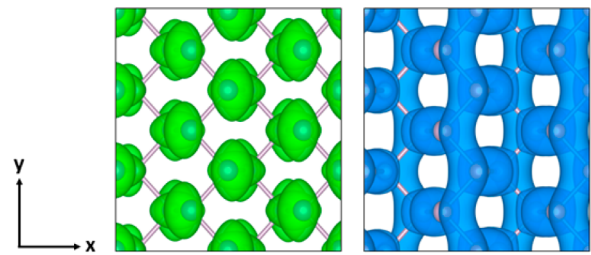


Figure 6. VBM (left) is nonbonding in the zigzag direction, implying that its upon extension the energy does not change. The CBM (right) is bonding in the zigzag direction, meaning that it is destabilized upon extension. Armchair direction is along X, zigzag direction is along Y. Isosurfaces are $0.001 e/a_0^3$.

347 CBM is therefore energetically unchanged as a-PNR is strained
348 between $\epsilon = -10\%$ and $+8\%$, and trends in the bandgap of a-
349 PNR are dominated by the VBM energy. However, as a-PNR is
350 stretched a higher energy conduction band made up of
351 antibonding p_y orbitals reduces in energy and becomes
352 stabilized relative to the CBM. At strains of $\epsilon > +8\%$, this
353 band becomes the CBM and continues to fall in energy as a-
354 PNR is stretched, causing the bandgap to plateau and begin to
355 fall. This new CBM is also extremely flat and nondispersive
356 near the conduction band minimum, see Supporting
357 Information Figure S1, leading to a dramatic increase in m_e^*
358 at strains of $\epsilon > +8\%$, potentially leading to a quenching of
359 charge transport in the conduction band as m_e^* rises to $\approx 4m_0$
360 while m_h^* is unaltered.

361 In summary, stretching a-PNR between $\epsilon = -10\%$ and $+8\%$
362 leads to a steadily increasing hole and electron effective mass
363 m_e^*/m_h^* ratio and bandgap due to orbital separation and the
364 stabilization of the VBM respectively. At strains above 8%, a
365 new CBM emerges and is stabilized as further strain is applied,
366 reducing the bandgap but strongly increasing the electron
367 effective mass. This exceptional increase in the ratio m_e^*/m_h^*
368 means that this structure may readily be tuned for p-type
369 applications (Figure 7).
369 17

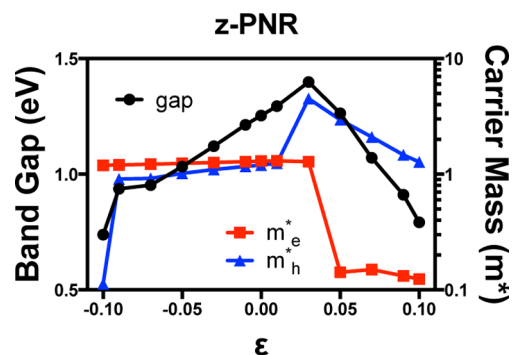


Figure 7. Variation of bandgap (shown in left axis); hole and electronic effective masses (shown in right axis) with respect to strain (ϵ) for the z-PNR.

370 For z-PNR structures, a different behavior is manifested. At
371 zero strain, the effective mass of the hole is slightly less than
372 that of the electron. The p_z orbitals making up the VBM, which
373 is located at $[0, 0.0625, 0]$, are nonbonding in the zigzag
374 direction, so the stabilization of the VBM seen when stretching
375 a-PNR is not seen in z-PNR. Instead, the increase in bandgap
376 seen between -9% and $+3\%$ is attributable to the 376

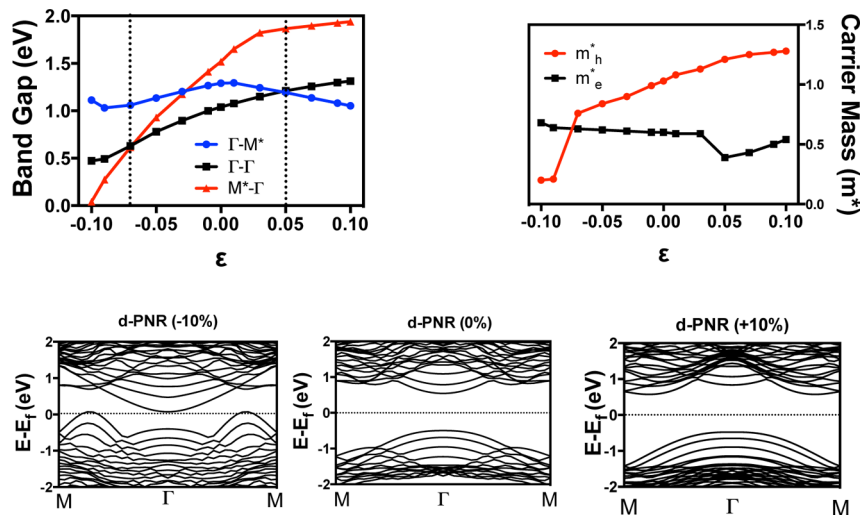


Figure 8. Variation of bandgap (top left) and hole and electronic effective masses (top right) with respect to strain (ϵ) for the d-PNR, both direct transition ($\Gamma \rightarrow \Gamma$ black line with squares), and two indirect transitions ($\Gamma \rightarrow M^*$, blue line with circles, $M^* \rightarrow \Gamma$, red line with triangles). The dashed lines indicate where the transition from a direct to an indirect bandgap occurs. Bottom figures are representative band structures for strains of -10 , 0 , and $+10\%$, respectively.

377 destabilization of the CBM. As can be seen in Figure 6, the
 378 CBM consists of p_z orbitals that are bonding in the zigzag
 379 direction. Therefore, stretching z-PNR destabilizes the CBM
 380 and increases the band gap. However, as z-PNR is stretched
 381 past $\epsilon = +4\%$, a new CBM emerges that consists of p_z orbitals
 382 arranged in an antibonding manner along the zigzag direction.
 383 This band has a greater dispersion along the nanoribbon
 384 direction than the original CBM, see Supporting Information
 385 Figure S3. Extension of z-PNR stabilizes these orbitals and
 386 causes the bandgap to fall. Furthermore, m_e^* falls by an order of
 387 magnitude as strain exceeds $\epsilon = +4\%$. Meanwhile, a new VBM
 388 emerges at the Γ point when $\epsilon > +3\%$, making the bandgap
 389 direct ($\Gamma \rightarrow \Gamma$). We note that the direct bandgap is typically
 390 only a hundredth of an electronvolt higher than the indirect gap
 391 for cases where indirect gaps are lowest in energy. This VBM is
 392 nondispersive, see Supporting Information Figure S2, resulting
 393 in a significant jump in m_h^* when strain exceeds $\epsilon = +3\%$ with
 394 the effective hole mass reaching values of $4.5 m_0$. The sharp
 395 drop in m_h^* and bandgap observed when $\epsilon = -10\%$ can be
 396 attributed to a rising VBM made up of antibonding p_x orbitals.

397 To summarize, compressing z-PNR nanostructures shows a
 398 significant effect on hole effective mass, strongly influencing
 399 hole transport. Conversely, placing z-PNR nanostructures
 400 under tensile strain significantly reduces the electron effective
 401 mass, while strongly increasing the hole effective mass,
 402 potentially quenching hole transport. The ratio of m_h^*/m_e^* is
 403 liable to demonstrate a giant increase after a tensile strain of
 404 4% ; this has significant implications for potential switching
 405 devices. This structure may be tuned for n-type applications.

406 In contrast to the a-PNR and z-PNR structures, the behavior
 407 of the bandgap with respect to external strain for the d-PNR
 408 structures is rather complicated, see Figure 8. The direct
 409 bandgap (which involves a $\Gamma \rightarrow \Gamma$ transition) increases linearly
 410 with increasing tensile strain and conversely decreases with
 411 increasing compressive strain. This behavior is driven by the
 412 behavior of the valence and conduction bands. The conduction
 413 band rises in energy with tension and decreases in energy upon
 414 compression. The constituent p_z orbitals are arranged in an
 415 overall bonding manner along the infinite ribbon direction. The
 416 valence band is mostly composed of p_z orbitals that are mostly

antibonding in character, which extend along the nanoribbon 417
 direction. Therefore, upon extension the valence band slightly 418
 lowers in energy. As d-PNR is stretched between $\epsilon = +0\%$ and 419
 $+10\%$, the energy of the conduction band at point M^* (0.276 , 420
 0.276 , 0) falls, reducing the $\Gamma \rightarrow M^*$ gap. When $\epsilon = +5\%$, the 421
 CBM moves to M^* and the bandgap of d-PNR becomes 422
 indirect ($\Gamma \rightarrow M^*$). The $\Gamma \rightarrow M^*$ gap continues to decrease 423
 with tensile strain, falling to 1.05 eV at $\epsilon = +10\%$. While the 424
 energy of the valence band at the Γ -point only slightly alters, 425
 the energy of the valence band at M^* rises as d-PNR is 426
 compressed. This behavior is related to the buckled nature of 427
 the material and the bonding nature of the p_z orbitals at that 428
 point. As the nanoribbon is compressed, the distance between 429
 the top and bottom layers increases, which destabilizes the 430
 bonding orbitals leading to a rise in their energy. Consequently 431
 this manifests at the valence band edge when $\epsilon = -7\%$, the 432
 VBM moves from Γ to M^* , and the bandgap of d-PNR 433
 becomes indirect ($M^* - \Gamma$). As d-PNR is further compressed, 434
 the bandgap falls and eventually begins to exhibit metallic 435
 character at $\epsilon = -10\%$. 436

It follows from the above discussion that there are critical 437
 strain values where the Γ - and M^* -point energies are equal. For 438
 the valence band, the critical strain value is around -7% , 439
 whereas for the conduction band it is around $+5\%$. This 440
 behavior would have potential applications for valleytronic 441
 devices, which make use of the fact that quasiparticles with the 442
 same energy, but residing in different parts of the reciprocal 443
 space, have different momenta and thus are less susceptible to 444
 phonon scattering.⁴⁵ 445

The effective masses of the electron and hole in the d-PNR 446
 were also calculated, as shown in Figure 8. Under no external 447
 strain, the effective mass of the electron is significantly less than 448
 that of the hole, which is in contrast to the other two 449
 nanoribbon structures studied. When under compressive strain, 450
 the effective mass of the electron slightly increases; however, 451
 there is a significant decrease in the effective mass of the hole, 452
 especially when the bandgap undergoes a transition from direct 453
 to indirect at -9% . Initially $m_h^* = 1.03m_0$, but falls to $0.20m_0$ 454
 when compressive strain is -9% . When the nanoribbon is 455
 under a tensile strain, hole masses slowly increase to $1.28m_0$ at 456

457 strain +10%, while m_e^* slowly decreases to $0.39m_0$ at +3% strain
458 before increasing again to $0.54m_0$ for a strain of +10%. This
459 behavior is due to the onset of the direct–indirect transition.
460 To summarize, compressing d-PNR improves hole effective
461 masses, and for large compressive and tensile strains the direct
462 to indirect transition strongly reduces the gap, which also
463 coincides with a strong decrease in the hole effective mass.
464 Upon tension, the electron effective mass remains smaller than
465 the hole mass, even when the direct–indirect transition occurs
466 at a tension of +5%.

467 From the above analysis of the behavior of the effective
468 masses, it is clear that putting both a-PNR and z-PNR
469 structures under tensile strain is optimal for tuning phosphor-
470 ene nanoribbons for p-type (hole-dominated transport for the
471 a-PNR) and n-type (electron dominated transport for the z-
472 PNR) devices. However, if maximized charge transport of both
473 types of carrier is desired, then nanoribbons should be placed
474 under compressive strain. The d-PNR structures demonstrate
475 an interesting direct to indirect transition for both compression
476 and extension, which modify the optical properties, but based
477 on analysis of the band structure, we determine that at critical
478 strains it is possible to achieve degenerate energy valleys at
479 different k -points. Nanostructuring of the material in this
480 direction would be of interest for valleytronic applications.
481 Overall, for effective masses the a-PNR structures are best as
482 those possess the lowest masses.

483 It is interesting to compare the effects of straining all three
484 nanoribbons to that of straining two-dimensional phosphor-
485 ene.⁴³ While the effects of uniaxial strain on phosphorene
486 manifest as changes in the electronic structure in all directions
487 of the 2D reciprocal space, the pseudo one-dimensional nature
488 of nanoribbons means that the Brillouin zone can only be
489 sampled in one direction. For example, the direct to indirect
490 bandgap transition observed when stretching phosphorene is
491 not observed when stretching a-PNR. This is because a new
492 CBM emerges between Γ and Y in the reciprocal space when
493 stretching phosphorene, which cannot be sampled in the one-
494 dimensional Brillouin zone of the a-PNR structure.

495 In summary, we have performed density functional theory
496 simulations on a realistic model for passivated phosphorene
497 nanoribbons, a one-dimensional nanostructure that demon-
498 strates the anisotropy of the phosphorene lattice. We found that
499 gradient-corrected functionals are sufficient to calculate
500 effective masses. We show that in order to describe correctly
501 the electronic properties of bulk black phosphorus, it is
502 essential to include van der Waals effects.

503 Three types of nanoribbon were constructed and modeled,
504 all of which involved the breaking of one P–P bond per edge
505 phosphorus atom, the armchair, diagonal, and zigzag. All three
506 types of nanoribbon display quantum size effects that modify
507 the position of the valence and conduction band edges with
508 decreasing width, allowing tuning of the bandgap. In particular,
509 the z-PNR structures show strong quantum size effects with a
510 large change in bandgap over the ribbon widths. Nano-
511 structuring to very narrow widths does change the effective
512 mass of carriers. Nanostructuring of a-PNR increases the
513 electron effective mass by an order of magnitude. Nano-
514 structuring of z-PNR increases the hole effective mass by a
515 factor of 3. Carrier effective mass in d-PNR structures are
516 insensitive to nanostructuring. Such phenomenon can be
517 effectively utilized for electron–hole separation, for example,
518 in photocatalysis.

The response of the nanoribbons to strain was also
519 determined. Strain was found to change the relative energy
520 and nature of electronic states within the nanoribbons, leading
521 to changes in the bandgap and effective masses. The effect of
522 strain on the bandgap can be understood by looking at the
523 bonding character of the band edges along the direction of
524 straining. Meanwhile, when nanoribbons are stretched or
525 compressed passed critical strains, competing bands rise or
526 fall in energy and assume band edge positions, leading to
527 dramatic shifts in m_h^* and m_e^* . Remarkably, for a-PNR
528 structures upon surpassing the critical strain of +9% the
529 effective mass of the electron is increased by a factor of 30 while
530 leaving the hole effective mass unchanged. Similarly, for z-PNR,
531 straining to +4% results in a giant increase in m_h^*/m_e^* , a
532 behavior that has great potential for switching devices. 533

534 Furthermore, straining d-PNR can lead to two direct to
535 indirect bandgap transitions as the valence band is stabilized
536 (under compression) and the conduction band is destabilized
537 (under extension) at a special k -point M^* , which is widely
538 separated from the Γ -point. There is the possibility that d-PNR
539 structures may be engineered upon straining, so that two
540 energetically degenerate valleys with electrons of widely
541 different momentum are able to coexist at the same energy.
542 These materials are thus of interest for valleytronic applications.

543 Phosphorene is a material that possesses great potential for
544 electronic and optical devices. We demonstrate that electronic
545 properties can be tuned by fabrication of nanoribbons. We
546 show in particular that strain can improve charge transport
547 properties with tension potentially improving the electron
548 transport of a-PNR structures and hole transport properties of
549 z-PNR structures. Furthermore, the optical properties of d-
550 PNR structures can be tuned and further experimental
551 investigation of these structures would be of great interest. 551

■ ASSOCIATED CONTENT

 552

📄 Supporting Information

 553

554 Comparison of structural parameters and electronic structure
555 for black phosphorus obtained using PBE, PBESol, HSE06,
556 PBE+Grimme, and HSE06+Grimme functionals. Effective
557 masses and bandgaps of phosphorene nanoribbons for strain
558 values are tabulated. Stiffness constants of three types of PNR
559 are also tabulated. Analysis of band behavior when a-PNR and
560 z-PNR structures are strained. This material is available free of
561 charge via the Internet at <http://pubs.acs.org>.

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Notes

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