1	The role of Light in Measuring Ocular Biomechanics
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21 Abstract

22 The cornea is a highly specialised tissue with a unique set of biomechanical properties 23 determined by its complex structure. The maintenance of these mechanical properties is 24 fundamental to maintain clear vision as the cornea provides the majority of the focussing power of the eye. Changes to the biomechanics of the cornea can occur during ageing, 25 26 disease, and trauma or as a result of surgery. Recently there has been increased interest in the mechanical properties of the cornea as knowledge of these properties has significant 27 28 implications for the improvement of current ocular treatments including PRK, LASIK and 29 for the diagnosis and tracking of corneal diseases and therapy such as keratoconus and crosslinking. Biomechanics are also important for the development of artificial corneal 30 31 replacements. This paper describes the use of a novel, non-destructive lateral electronic 32 speckle pattern shearing interferometry (ESPSI). The data generated via this technique gives a full field view of the mechanical response of the cornea under simulated physiological 33 34 loading conditions, and enables strain and displacement to be determined in 3 planes. The 35 technique allows corneal stiffness to be quantified and enables changes and nonhomogeneties that occur due to surgery or disease to be detected. 36

38 Introduction

39 The cornea is a complex highly specialised biological tissue with a unique structure that exhibits both transparency and high tensile strength. It has evolved to allow light to pass 40 41 through and to focus on the retina. It provides a barrier to protect the eye from disease and maintain shape whilst subject to the forces of intraocular pressure (IOP) and those of 42 43 fluctuating cardiac cycle. Advances in static measurement techniques have resulted in a literature describing corneal 44 tissue architecture from a microscopic to a nanoscopic scale. The use of X-rays^[1], scanning 45 electron microscopy^[2], non-linear microscopy techniques^[3], transmission electron 46 microscopy (TEM)^[2] and polarisation sensitive optical coherence tomography^[4] amongst 47 48 others have enabled detailed imaging of the corneal collagen architecture. However, due to the complexity of the structure, its anisotropy and its nonlinear response to loading^[5], it is not 49 possible to understand and/or predict the mechanical behaviour using these methods. 50 51 In comparison to static data, little information currently exists detailing the dynamic 52 behaviour of the cornea and there is still a lack of understanding as to the specific mechanical properties that govern the corneal behaviour and how it deforms under physiological pressure 53 54 changes.

55

56 *Quantification of corneal mechanical properties*

Quantifying the corneal mechanical properties remains challenging, as like other biological materials the cornea exhibits a viscoelastic and non-linear response to loading^[6]. The response can differ dependent on the loading history, magnitude of the applied load, strain rate, maximum strain, nature of loading (continuous or cyclical), recovery time between loading cycles and tissue properties such as hydration levels, temperature, freshness and storage conditions^[7].

63 Several *in vitro* attempts have been made to measure the mechanical response of the cornea to loading and a number of mechanical parameters have been quantified including Young's 64 modulus^[8, 9], shear modulus^[10], and Brillouin modulus^[11]. Young's modulus is commonly 65 66 used assuming that the response of the cornea is governed by the tensile strength of the collagen fibres. However, a large range of values of Young's modulus have been reported 67 varying from 0.1 - 57MPa^[12]. This can in-part be explained by the viscoelastic nature of the 68 cornea, however, there are many drawbacks to some of the techniques currently used such as 69 70 strip extensionerry which affect the reliability of data and its usefulness when considering *in* 71 vivo behaviour.

Common problems with existing techniques include; exposing the cornea to pressure ranges not representative of physiological pressures in magnitude, time base or direction. *In vivo* the cornea is dome like and heterogenous in structure in both x, y and z planes^[13]. Clearly strip extensometry involving isolation of discrete elements from the dome give little reality when related to the mechanical properties of the *in vivo* system.

77

78 *Laser interferometry*

Electronic speckle pattern interferometry (ESPI) and ESPSI are versatile techniques that have
been used within the engineering industry for a number of years to quantify material
properties, detect structural non-homogeneities in composite structures^[14, 15] and predict
failure modes. They have also recently been used for *in vitro* testing of the loading response
of hard biological materials including the femur^[16] and the jaw^[17].

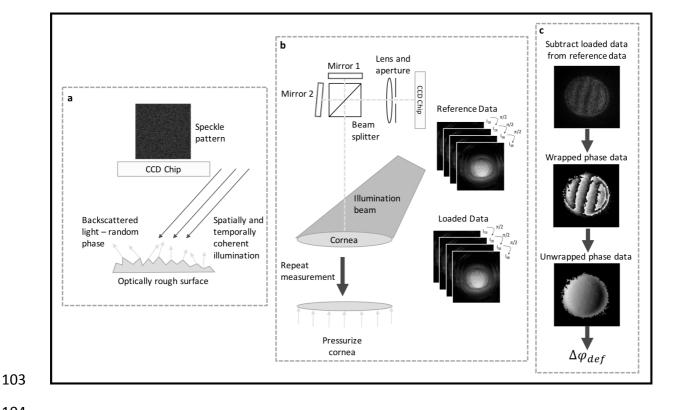
Laser shearing interferometry has many advantages regarding its use as a tool to quantify the mechanical response of corneal tissue, this has been demonstrated in studies where radial shear has been used to show the effect of using different parameters during LASIK surgery such as depth and angles of incisions^[18]. It has also been used to determine the changes in

Young's modulus of the cornea during ageing^[19] and following crosslinking^[20]. It is non-88 89 contact, non-destructive, provides data in real time and is highly sensitive; the sensitivity can 90 be optimized so the cornea is loaded at pressures within the physiological range. It is also a full-field measurement technique therefore the corneal response to loading can be viewed 91 92 across the whole surface, enabling defects, non-homogeneities and irregularities in behaviour (that may be missed using less sensitive, point based techniques) to be identified. 93 94 A specific lateral shearing interferometry technique capable of mapping the strain on the 95 surface of the cornea under hydrostatic loading is discussed in this paper.

- 96 Lateral Electronic Speckle Pattern Shearing Interferometry (ESPSI)
- 97 Lateral sensitivity was selected as opposed to radial that has been used in previous studies,

98 because with radial shear data was not obtained for the central region of the measurement

- 99 (ref) and therefore important information was lost for this area, with lateral shear uniform
- 100 sensitivity is achieved across the entire surface.
- 101 The working principles for lateral ESPSI are summarized in Figure 1. Full details have been
- 102 discussed elsewhere^[21].</sup>



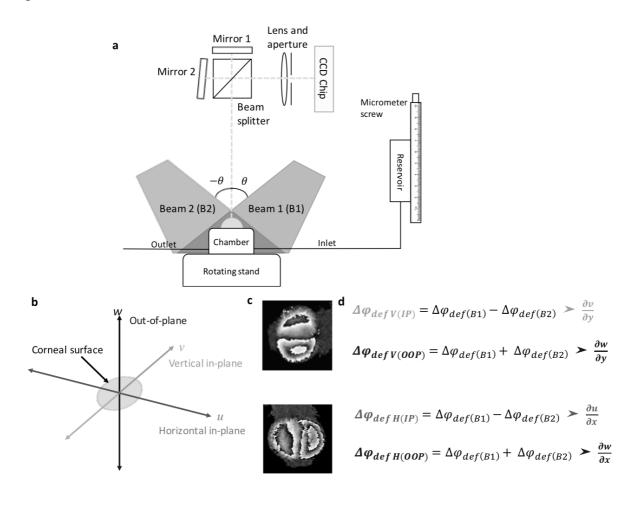


105 Data generated using ESPSI gives the phase change due to deformation ($\Delta \phi_{def}$), this appears 106 visually as a series of interference fringes and relates to the rate of displacement (strain) that 107 has occurred in the object due to loading *via* the following equations^[22]:

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$$\Delta \varphi_{def} = -\frac{2\pi}{\lambda} \left[\frac{\partial u}{\partial x} \delta x(\sin \theta) + \frac{\partial w}{\partial x} \delta x(1 + \cos \theta) \right] \text{(horizontal shear)}$$
110

111
$$\Delta \varphi_{def} = -\frac{2\pi}{\lambda} \Big[\frac{\partial v}{\partial y} \delta y(\sin \theta) + \frac{\partial w}{\partial y} \delta y(1 + \cos \theta) \Big] \text{ (vertical shear)}$$

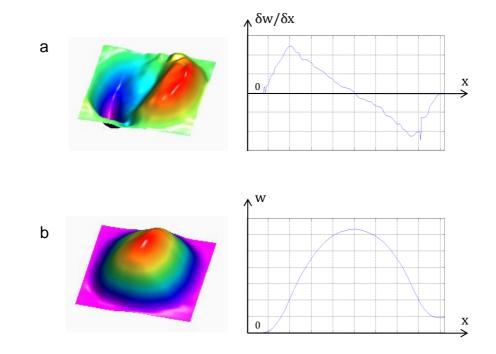
Where λ is the wavelength of the illumination source, θ is the illumination angle, $\frac{\partial u}{\partial x}$ and $\frac{\partial v}{\partial y}$ 113 are the in-plane (IP) strain components for horizontal and vertical shear respectively, $\frac{\partial w}{\partial x}$ and 114 $\frac{\partial w}{\partial v}$ are the out-of-plane (OOP) strain components and δx and δy are the magnitudes of 115 horizontal and vertical shear respectively. To quantify the components of IP and OOP strain a 116 117 specific set-up (Figure 2) has been designed so the object can be illuminated at equal and opposite illumination angles^[23], manipulation of the data gathered from each of these 118 illumination angles allows the IP and OOP strain components to be separated and 119 quantified^[24]. 120



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The test rig (Figure 2) was designed so the object can rotate through 90° allowing the
sensitivity direction to be changed easily from horizontal to vertical without changing the

position of the camera or the illumination source. This enables the specific strain components
to be determined in three planes. Corneal displacement can also be determined in each of the
planes by integration of the phase data an example of this is given in Figure 3.



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130 ESPSI and loading rig set-up

131 The interferometer consisted of a divergent square illumination beam ($\lambda = 532$ nm), shaped with holographic optics (Laser Optical Engineering, LOE Ltd, Derbyshire, UK) to provide 132 133 uniform illumination. A camera (XXXXX) consisting of a 35 mm imaging lens 134 (magnification____) and an externally controlled shearing head able to adjust the magnitude 135 of shear was used to image the samples. Analysis software (Defect Detect LOE Ltd, 136 Derbyshire, UK) was used to capture the images and produce the phase data for each measurement in real time. A wrapped phase data file was generated for each measurement 137 138 set. 139 A stainless steel artificial anterior chamber was used to clamp the corneal samples. The chamber was filled from a tank the height of which was changed via a micrometre screw to 140

141 an accuracy of (0.005mm) measured using a digital gauge (Swiss Precision Instruments,

INC.TM). A pressure transducer was attached at the outlet and positioned at the same height as
the sample to measure the hydrostatic pressure in the chamber to an accuracy of 0.005
mmH₂O. Phosphate buffered saline (PBS, Sigma-Aldrich, UK, ρ = 0.995g/ml at 25°C) was
used to pressurize the samples.
Corneal-scleral buttons were mounted into the chamber and set to an initial pressure of 16

mmHg (217.5 mmH₂O), which is within the average reported IOP for the human eve ^[25, 26], 147 148 for the eye for 30 min prior to recording of the first measurement to allow for any stress 149 relaxation to occur and ensuring that the samples were inflated to their natural curvature. 3-7µm glass spheres (Potters Industries LLC) were randomly distributed onto the sample 150 151 surface to ensure adequate backscattering of light while not interfering with the response of 152 the cornea. The height of the tank was changed by 1-5mm in 0.5mm increments and phase 153 data was recorded at each height. The small pressure change was selected as it is well within the physiological pressure changes experienced by the cornea in-vivo and demonstrates the 154 155 high sensitivity of the technique while reducing the effects of any small changes that could 156 occur in the strain rate or relaxation time during experiments. The measurement process was 157 repeated 4 times at each height to collect data for horizontal and vertical sensitivity for each 158 of the illumination directions.

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160 **Data**

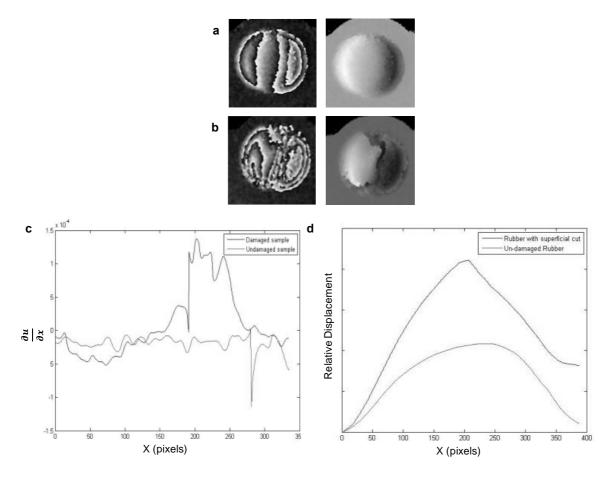
161 *Tests on rubber sample*

To demonstrate the suitability of the technique to detect defects and give an example of the data that can be generated using this method and its validity, initial testing was done on a simulation cornea made from cured rubber latex. Testing was first carried out on an 'undamaged' rubber sample, a superficial cut was then made to the sample and the testing procedure was repeated for the 'damaged' sample. The unwrapped and wrapped phase maps

167 from these tests are given in **Figure 4** along with plots giving the horizontal in-plane strain

168 component alone the central line and the relative displacement change between the two

samples.



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Under a pressure increase of 29.4 Pa the interference fringes on the wrapped interferogram of
the undamaged sample appeared relatively symmetrical in distribution (Figure 4a), this
indicates uniform strain distribution, which is expected due to the isotropy of the sample.
After a superficial cut was introduced the number of fringes on the wrapped interferogram
increased (Figure 4b) and they became non uniform in distribution and direction with a
higher concentration around the area of damage indicating higher strain in this area and nonuniform deformation with some twisting.

178 The in-plane strain component $(\frac{\partial u}{\partial x})$ in the undamaged sample was constant across the 179 sample indicating uniform deformation (**Figure 4c**). In the damaged sample $\frac{\partial u}{\partial x}$ was

- significantly higher in the area of damage indicating higher strain and therefore deformation
 in the region where the cut had been introduced (Figure 4c).
- 182 The in-plane displacement map shows the displacement profile for the central line in the
- sample (Figure 4d). In the undamaged sample the displacement profile is smooth and
- 184 represents uniform bulging (**Figure 4d**), In the damaged sample the displacement is much
- 185 greater with a steeper peak where the damage is (**Figure 4d**), indicating weakening of the

186 sample due to the presence of the damage.

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188 *Tests on cornea*

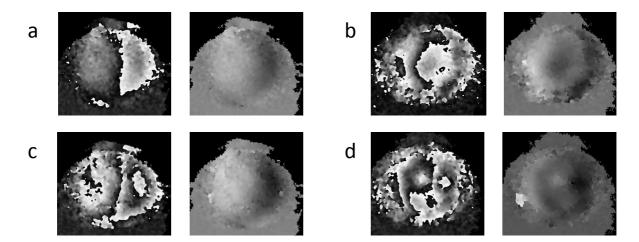
189 The testing procedure was repeated on a fresh porcine cornea. Initially the undamaged

sample was tested. It was then removed from the chamber and a superficial cut was made on

191 the right side surface of the cornea at approximately the centre line from the edge towards the

192 centre point and the tests were repeated. The resulting wrapped and unwrapped

193 interferograms are shown in **Figure 5**.





Despite the low increase in pressure (less than a 10th of that experienced by the cornea
resulting from cardiac cycle) differences in the response of the cornea to loading could be
observed after the introduction of a superficial cut to the surface. For the undamaged cornea
(Figure 5a, 5c) the fringes in the wrapped image are relatively symmetrical and straight,
however, for the damaged cornea (Figure 5b, 5d) the fringes are non-uniform and not

symmetrical indicating non uniform deformation, which has occurred as a result of damage tothe surface.

202

203 Conclusions

204 The technique discussed is capable of tracking the dynamic response of the cornea to 205 physiological loads with pixel resolution and gives full field data regarding strain and displacement that occurs on the corneal surface. The high sensitivity and full field nature of 206 207 the technique means it is capable of detecting changes in the biomechanical responses of the 208 cornea resulting from the structural damage associated with surgery. The xy location of such 209 changes are of great importance in determining points of weakness and their implications for 210 designing future surgery. In essence, it has the potential to increase understanding of the 211 mechanical behaviour of the normal cornea and how it changes with disease, and therefore may help improve diagnosis and treatment. Secondly these measurements will be 212 213 fundamental in the development of computer simulated models of the cornea. Thirdly, such 214 measurements in vivo would allow the diagnosis of patients with highly elastic corneas who 215 should perhaps not undergo laser surgery as such procedures may result in ectasia in such individuals. Finally, a detailed strain map of patients with pathological conditions, such as 216 217 Keratoconus would allow the development of topographic treatments using techniques such as riboflavin and UV based cross-linking. The clinical environment is extremely receptive 218 219 and waiting for a clinical version of the device used in this study.

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226	Declaration of Interest							
227	The authors report no conflict of interest. The authors alone are responsible for the content							
228	and writing of the manuscript.							
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230	References							
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Figure legends

Figure 1: Summary of the working principle of ESPSI; (a) Spatially and temporally coherent 302 light is used to illuminate the surface of the object, if the surface of the object is rough (height 303 304 variations > $\lambda/4$) the light scattered from the object has a random phase, constructive and 305 destructive interference of this light results in a speckle pattern which is captured on a charge-coupled device (CCD) chip; (b) The object beam is split into two parts via a beam 306 307 splitter- one of these beams is transformed laterally and the beams are combined on the 308 surface of the CCD chip. A unique speckle pattern is captured from the object in its reference state and stored, the object is then loaded and a second speckle pattern in captured, phase 309 310 stepping is used during data capture so quantitative data can be extracted; (c) The loaded 311 speckle phase data is subtracted from the reference speckle phase data in real time resulting 312 in subtraction fringes. A wrapped phase map is generated from the phase stepped data, this 313 wrapped data is then unwrapped to give the absolute phase change due to deformation ($\Delta \phi_{def}$) 314 for each pixel in the image plane.

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Figure 2: Dual beam interferometry system to separate components of IP and OOP strain; (a) A simplified version of test rig, data is collected individually from illumination with Beam 1 and then Beam 2 over two measurement cycles. The rotating stand enables rotation through 90° to obtain sensitivity in both the horizontal and vertical planes ensuring $\delta x = \delta y$. b) The direction of different planes with reference to the corneal surface. (c) An example of wrapped interference fringes for vertical and horizontal shear. (d) Equations demonstrating how phase data from different illumination angles is manipulated to give separate components of strain. Figure 3 – a) Out of plane strain $(\frac{\delta w}{\delta x})$ surface plot and line plot along the x-axis for central y axis position; b) Out of plane displacement (w) surface plot and line plot along the x-axis for central y axis position.

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Figure 4 - Comparison of undamaged and damaged samples; (a) wrapped and unwrapped phase maps of undamaged sample under hydrostatic pressure of 29.4 Pa; (b) wrapped and unwrapped phase maps of sample with superficial cut under hydrostatic pressure of 29.4 Pa, (c) Plot comparing horizontal in-plane strain $\frac{\partial u}{\partial x}$ for undamaged and damaged samples

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Figure 5 - a) Wrapped and unwrapped interferograms of an undamaged pigs cornea due to
9.8Pa hydrostatic pressure increase; b) Wrapped and unwrapped interferograms of a pigs
cornea with a superficial cut on the surface due to 9.8Pa hydrostatic pressure increase;
c)Wrapped and unwrapped interferograms of an undamaged pigs cornea due to 19.6Pa
hydrostatic pressure increase; d) Wrapped and unwrapped interferograms of a pigs cornea
with a superficial cut on the surface due to 19.6Pa hydrostatic pressure increase.

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