

Comparative Study on Carrier Phase Estimation Methods in Dispersion-Unmanaged Optical Transmission Systems

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Abstract—The comparative study on three carrier phase estimation (CPE) methods, involving a one-tap normalized least-mean-square algorithm, a block-wise average algorithm, and a Viterbi-Viterbi algorithm has been carried out in the long-haul high-speed dispersion-unmanaged coherent optical transmission systems. The close-form predictions for bit-error-rate behaviors in these CPE methods have been analyzed by considering both the laser phase noise and the equalization enhanced phase noise.

Keywords—coherent communication; optical fiber transmission; carrier phase estimation, laser phase noise, equalization enhanced phase noise

I. INTRODUCTION

The performance of long-haul high-speed optical fiber communication systems can be significantly degraded by the transmission system impairments, such as chromatic dispersion (CD), polarization mode dispersion (PMD), laser phase noise (PN) and fiber nonlinearities (FNLs) [1-10]. Coherent optical detection and digital signal processing (DSP) allows the powerful equalization and mitigation of system impairments in electrical domain, and have become one of the most promising techniques for the next-generation optical fiber communication networks to achieve a performance very close to the Shannon capacity limit, with an entire capture of the amplitude and phase of the optical signals [11-19]. To compensate the phase noise from the laser sources, some feed-forward and feed-back carrier phase estimation (CPE) algorithms have been proposed to estimate the phase of optical carriers [20-28]. Among these CPE approaches, the one-tap normalized least-mean-square (NLMS) algorithm, the block-wise average (BWA) algorithm, and the Viterbi-Viterbi (VV) algorithm have been validated for compensating the laser phase noise effectively, and are also regarded as promising DSP algorithms in the real-time high-speed coherent optical fiber transmission systems [26-28].

In the electronic dispersion compensation (EDC) based optical fiber communication systems, an effect of equalization enhanced phase noise (EEPN) is generated due to the interactions between the EDC module and the laser phase noise [29,30]. The performance of optical fiber communication

systems will be degraded seriously by EEPN, with the increase of fiber dispersion, laser linewidths, modulation formats, and symbol rates [31-34]. The effects of EEPN have been studied in the single-channel, the wavelength division multiplexing, the orthogonal frequency division multiplexing, the dispersion pre-distorted, and the multi-mode optical transmission systems [35-39]. Meanwhile, some investigations have also been carried out to study the performance of EEPN in the CPE of long-haul high-speed optical transmission systems [40-42]. Considering the impact of EEPN, the traditional analysis of the CPE algorithms is not suitable any longer for the design and the optimization of the long-haul high-speed optical fiber networks. Correspondingly, it will be interesting and useful to investigate the bit-error-rate (BER) performance in the one-tap NLMS, the BWA, and the VV carrier phase estimation algorithms, when the influence of EEPN is taken into account.

In this paper, the theoretical assessments on the CPE in long-haul coherent optical fiber communication systems using the one-tap NLMS, the BWA, and the VV algorithms are presented and discussed. The close-form expressions for the estimated carrier phase in the three algorithms are derived, and the BER performance such as the BER floors, has been predicted analytically. For different phase noise variance (or effective phase noise variance considering EEPN), the performance of the NLMS, the BWA, and the VV CPE methods have been compared.

II. LASER PHASE NOISE AND EQUALIZATION ENHANCED PHASE NOISE

A. Laser Phase Noise

In coherent optical communication systems, the variance of the phase noise from the transmitter (Tx) laser and the local oscillator (LO) laser can be described as follows [1,2],

$$\sigma_{Tx_LO}^2 = 2\pi(\Delta f_{Tx} + \Delta f_{LO}) \cdot T_S \quad (1)$$

where Δf_{Tx} and Δf_{LO} are the 3-dB linewidths of the Tx laser and the LO laser respectively, and T_S is the symbol period of

coherent system. It is found that the laser phase noise variance decreases with the increment of the signal symbol rate $R_S=1/T_S$.

B. Analysis of Equalization Enhanced Phase Noise

Considering the interplay between the EDC module and the LO laser phase noise, the noise variance of the EEPN in the long-haul optical communication systems can be expressed as the follow equation [29,34],

$$\sigma_{EEP_LO}^2 = \pi\lambda^2 D \cdot L \cdot \Delta f_{LO} / 2cT_S \quad (2)$$

where D is the CD coefficient of fiber, L is the fiber length, and $\lambda=c/f_{Tx}=c/f_{LO}$ is the central wavelength of optical carrier wave, f_{LO} is the central frequency of LO laser, which is equal to the central frequency of the Tx laser f_{Tx} in the homodyne communication systems.

When EEPN is considered in the CPE, the total effective noise variance in optical transmission systems can be described as the following expression [31,34],

$$\begin{aligned} \sigma_T^2 &\approx \sigma_{EEP}^2 + \sigma_{Tx_LO}^2 \\ &\approx \pi\lambda^2 D \cdot L \cdot \Delta f_{LO} / 2cT_S + 2\pi T_S (\Delta f_{Tx} + \Delta f_{LO}) \end{aligned} \quad (3)$$

III. ANALYSIS OF CARRIER PHASE ESTIMATION

A. One-tap NLMS Carrier Phase Estimation

The transfer function of the one-tap NLMS carrier phase estimation in the coherent optical communication systems can be expressed as follows [25,34],

$$y(k) = w_{NLMS}(k)x(k) \quad (4)$$

$$w_{NLMS}(k+1) = w_{NLMS}(k) + \mu e(k)x^*(k) / |x(k)|^2 \quad (5)$$

$$e(k) = d(k) - y(k) \quad (6)$$

where $x(k)$ is the input symbol, k is the symbol index, $y(k)$ is the output symbol, $w_{NLMS}(k)$ is the tap weight of the one-tap NLMS algorithm, $d(k)$ is the desired output symbol after the CPE, $e(k)$ is the estimation error between the output symbol and the desired output symbol, and μ is the step size of the one-tap NLMS algorithm.

It has been verified that the one-tap NLMS CPE behaves similar to the ideal differential CPE, and the BER floor in the one-tap NLMS CPE for the quadrature phase shift keying (QPSK) optical transmission systems can be approximately described as [25,34]:

$$BER_{floor}^{NLMS-QPSK} \approx \frac{1}{2} \operatorname{erfc} \left(\frac{\pi}{4\sqrt{2}\sigma_T} \right) \quad (7)$$

Therefore, the BER floor in the one-tap NLMS carrier phase estimation for the n -level phase shift keying (n -PSK)

coherent optical communication systems can be calculated accordingly [25]:

$$BER_{floor}^{NLMS} \approx \frac{1}{\log_2 n} \operatorname{erfc} \left(\frac{\pi}{n\sqrt{2}\sigma_T} \right) \quad (8)$$

where σ_T^2 is the total phase noise variance in the n -PSK optical transmission systems.

B. Block-wise Average Carrier Phase Estimation

As an n -th power CPE method, the block-wise average algorithm calculates the n -th power of the received symbols to remove the information of the modulated phase in the n -PSK coherent transmission systems, and the computed phase (n -th power) are summed and averaged over a certain block (the length of the block is called block size). The averaged phase value is then divided over n , and the final result is regarded as the estimated phase for the received symbols within the entire block. For n -PSK coherent optical systems, the estimated carrier phase for each process block using the BWA algorithm can be expressed as [25,27],

$$\phi_{BWA}(k) = \frac{1}{n} \arg \left\{ \sum_{p=1+(q-1)N_{BWA}}^{q \cdot N_{BWA}} x^n(p) \right\} \quad (9)$$

$$q = \lceil k / N_{BWA} \rceil \quad (10)$$

where k is the symbol index, N_{BWA} is the block size of BWA algorithm, and $\lceil x \rceil$ means the closest integer larger than x .

The BER floor in the BWA carrier phase estimation in the n -PSK coherent communication systems can be derived using the Taylor series expansion as [25]:

$$BER_{floor}^{BWA} \approx \frac{1}{N_{BWA} \log_2 n} \cdot \sum_{p=1}^{N_{BWA}} \operatorname{erfc} \left(\frac{\pi}{n\sqrt{2}\sigma_{BWA}(p)} \right) \quad (11)$$

$$\sigma_{BWA}^2(p) = \frac{\sigma_T^2}{6N_{BWA}^2} \left[2(p-1)^3 + 3(p-1)^2 + 2(N_{BWA} - p)^3 + 3(N_{BWA} - p)^2 + N_{BWA} - 1 \right] \quad (12)$$

where σ_T^2 is the total phase noise variance in the n -PSK optical transmission systems.

C. Viterbi-Viterbi Carrier Phase Estimation

As another n -th power CPE approach, the Viterbi-Viterbi algorithm also calculates the n -th power of the received symbols to remove the information of the modulated phase. The computed phase are also summed and averaged over the processing block (with a certain block length). Compared to the BWA algorithm, the VV algorithm only treats the extracted phase as the estimated phase for the central symbol in each processing block. The estimated carrier phase in the VV

algorithm in the n -PSK coherent transmission systems can be described using the following equation [25,28],

$$\phi_{VV}(k) = \frac{1}{n} \arg \left\{ \sum_{q=-(N_{VV}-1)/2}^{(N_{VV}-1)/2} x^n(k+q) \right\} \quad (13)$$

where N_{VV} is the block size in the VV algorithm, and is an odd value of e.g. 1,3,5,7...

Using the Taylor expansion, the BER floor in the VV carrier phase estimation for n -PSK coherent communication systems can be assessed and expressed approximately using the following equation [25],

$$BER_{floor}^{VV} \approx \frac{1}{\log_2 n} \operatorname{erfc} \left(\frac{\pi}{n \sigma_T} \sqrt{\frac{6N_{VV}}{N_{VV}^2 - 1}} \right) \quad (14)$$

where σ_T^2 is the variance of the total phase noise in n -PSK optical fiber transmission systems.

IV. RESULTS AND DISCUSSIONS

As shown in Fig. 1, Fig. 2 and Fig. 3, the BER floors versus different phase noise variances (or effective phase noise variance considering EEPN) in the above three carrier phase estimation (the one-tap NLMS, the BWA, and the VV) algorithms in the long-haul high-speed optical fiber communication systems have been comparatively investigated, where the modulation formats of the QPSK (Fig. 1), the 8-PSK (Fig. 2), and the 16-PSK (Fig. 3) have been applied respectively. In these analytical models, the attenuation, the PMD, the fiber nonlinearities are all neglected. A block size of 11 is used in both the block-wise average and the Viterbi-Viterbi carrier phase estimation methods, since the additive noise in the transmission channels such as the amplified spontaneous emission (ASE) noise should also be taken into consideration in practical optical communication systems. The BER floors in the three CPE approaches are evaluated and discussed comparatively in the range from 10^{-6} to 0.5.

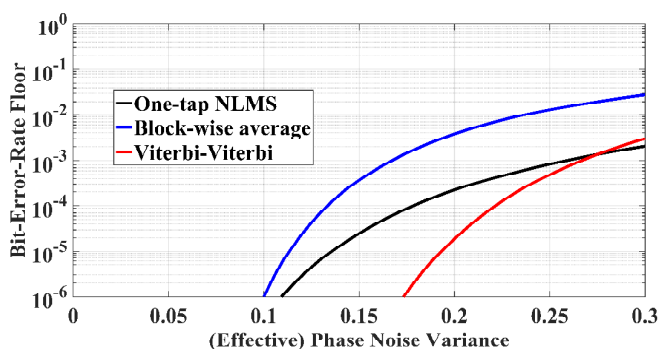


Fig. 1. BER floors versus different phase noise variances in the three carrier phase estimation algorithms in the QPSK optical fiber communication systems. Block sizes of the BWA and the VV algorithms are both 11.

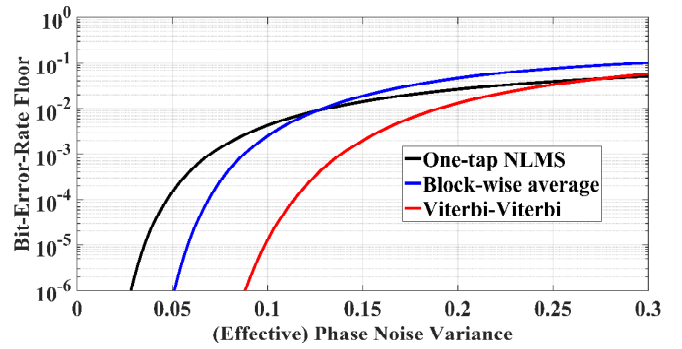


Fig. 2. BER floors versus different phase noise variances in the three carrier phase estimation algorithms in the 8-PSK optical fiber communication systems. Block sizes of the BWA and the VV algorithms are both 11.

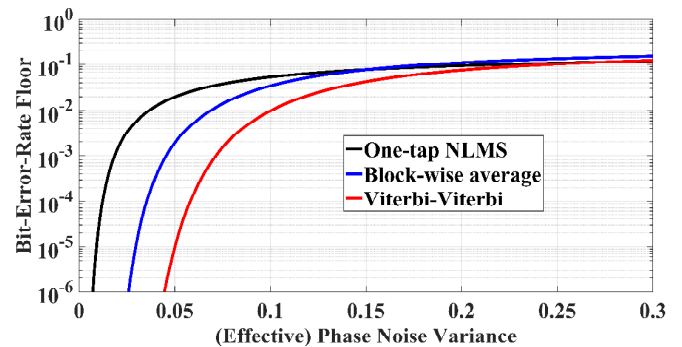


Fig. 3. BER floors versus different phase noise variances in the three carrier phase estimation algorithms in the 16-PSK optical fiber communication systems. Block sizes of the BWA and the VV algorithms are both 11.

It can be found in Fig. 1 that, in the QPSK transmission system, the Viterbi-Viterbi CPE algorithm outperforms the one-tap NLMS and the block-wise average algorithms for small phase noise variance (or effective phase noise variance), while the three CPE algorithms will converge to a similar behavior for the large phase noise variance (or effective phase noise variance). The same trends can be found in the 8-PSK coherent optical transmission system in Fig. 2 and in the 16-PSK coherent optical transmission system in Fig. 3. Meanwhile, it is also found that the difference between the three carrier phase estimation methods becomes smaller for higher-level modulation formats.

V. CONCLUSION

The analytical evaluation of the carrier phase estimation in the long-haul high-speed coherent optical fiber communication systems, using the one-tap normalized least-mean-square algorithm, the block-wise average algorithm, and the Viterbi-Viterbi algorithm, has been investigated, both considering the laser phase noise and the equalization enhanced phase noise. The close-form expressions for estimated carrier phase in the one-tap normalized least-mean-square, the block-wise average, and the Viterbi-Viterbi algorithms have been presented, and the BER performance such as the BER floors, in the three carrier phase estimation methods has been investigated comparatively.

The Viterbi-Viterbi CPE algorithm outperforms the one-tap NLMS and the block-wise average algorithms for small phase noise variance (or effective phase noise variance), while the three CPE algorithms will converge to a similar behavior for the large phase noise variance (or effective phase noise variance). Meanwhile, the difference between the three CPE methods becomes smaller for higher-level modulation formats.

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REFERENCES

- [1] I. Kaminow, T. Li, and A.E. Willner, *Optical Fiber Telecommunications VB: System and Networks*, Academic Press, Oxford, 2010.
- [2] G. P. Agrawal, *Fiber-Optic Communication Systems*, 4th ed., John Wiley & Sons, Inc., New York, 2010.
- [3] T. Xu, et al., "Field trial over 820 km installed SSMF and its potential Terabit/s superchannel application with up to 57.5-Gbaud DP-QPSK transmission," *Opt. Commun.*, vol. 353, pp. 133-138, 2015.
- [4] A. Berntson, et al., "Polarization dependence and gain tilt of Raman amplifiers for WDM systems," *Proc. IEEE Opt. Fiber Commun. Conf.*, pp. MI2, 2001.
- [5] H. Zhang, et al., "A quantitative robustness evaluation model for optical fiber sensor networks," *J. Lightwave Technol.*, vol. 31, pp. 1240-1246, 2013.
- [6] G. Jacobsen, K. Bertilsson, and Z. Xiaopin, "WDM transmission system performance: influence of non-Gaussian detected ASE noise and periodic DEMUX characteristic," *J. Lightwave Technol.*, vol. 16, pp. 1804-1812, 1998.
- [7] T. Xu, et al., "Normalized LMS digital filter for chromatic dispersion equalization in 112-Gbit/s PDM-QPSK coherent optical transmission system," *Opt. Commun.*, vol. 283, pp. 963-967, 2010.
- [8] G. Jacobsen, "Performance of DPSK and CPFSK systems with significant post-detection filtering," *J. Lightwave Technol.*, vol. 11, pp. 1622-1631, 1993.
- [9] Y. Li, et al., "Dynamic dispersion compensation in a 40 Gb/s single-channelled optical fiber communication system," *ACTA OPT. SIN.*, vol. 27, pp. 1161-1165, 2007.
- [10] I. Garrett and G. Jacobsen, "Theory for optical heterodyne narrow-deviation FSK receivers with delay demodulation," *J. Lightwave Technol.*, vol. 6, pp. 1415-1423, 1988.
- [11] E. Ip, et al., "Coherent detection in optical fiber systems," *Opt. Express*, vol. 16, pp. 753-791, 2008.
- [12] P. Bayvel, et al., "Maximising the optical network capacity," *Philos. Trans. R. Soc. A*, vol. 374, pp. 20140440, 2016.
- [13] T. Xu, et al., "Chromatic dispersion compensation in coherent transmission system using digital filters," *Opt. Express*, vol. 18, pp. 16243-16257, 2010.
- [14] T. Xu, et al., "Digital chromatic dispersion compensation in coherent transmission system using a time-domain filter," *Proc. IEEE Asia Commun. Photon. Conf.*, pp. 132-133, 2010.
- [15] E. Ip and J.M. Kahn, "Digital equalization of chromatic dispersion and polarization mode dispersion," *J. Lightwave Technol.*, vol. 25, pp. 2033-2043, 2007.
- [16] T. Xu, et al., "Frequency-domain chromatic dispersion equalization using overlap-add methods in coherent optical system," *J. Opt. Commun.*, vol. 32, pp. 131-135, 2011.
- [17] M.G. Taylor, "Phase estimation methods for optical coherent detection using digital signal processing," *J. Lightwave Technol.*, vol. 17, pp. 901-914, 2009.
- [18] G. Liga, et al., "On the performance of multichannel digital backpropagation in high-capacity long-haul optical transmission," *Opt. Express*, vol. 22, pp. 30053-30062, 2014.
- [19] R. Maher, et al., "Spectrally shaped DP-16QAM super-channel transmission with multi-channel digital back propagation," *Sci. Rep.*, vol. 5, pp. 08214, 2015.
- [20] E. Ip and J.M. Kahn, "Feedforward carrier recovery for coherent optical communications," *J. Lightwave Technol.*, vol. 25, pp. 2675-2692, 2007.
- [21] G. Jacobsen, et al., "Receiver implemented RF pilot tone phase noise mitigation in coherent optical nPSK and nQAM systems," *Opt. Express*, vol. 19, pp. 14487-14494, 2011.
- [22] G. Goldfarb and G. Li, "BER estimation of QPSK homodyne detection with carrier phase estimation using digital signal," *Opt. Express*, vol. 14, pp. 8043-8053, 2006.
- [23] I. Fatadin, D. Ives, and S. J. Savory, "Differential carrier phase recovery for QPSK optical coherent systems with integrated tunable lasers," *Opt. Express*, vol. 21, pp. 10166-10171, 2013.
- [24] G. Jacobsen, et al., "Study of EEPN mitigation using modified RF pilot and Viterbi-Viterbi based phase noise compensation," *Opt. Express*, vol. 21, pp. 12351-12362, 2013.
- [25] T. Xu, et al., "Carrier phase estimation methods in coherent transmission systems influenced by equalization enhanced phase noise," *Opt. Commun.*, vol. 293, pp. 54-60, 2013.
- [26] Y. Mori, et al., "Unrepeated 200-km transmission of 40-Gbit/s 16-QAM signals using digital coherent receiver," *Opt. Express*, vol. 17, pp. 1435-1441, 2009.
- [27] D.S. Ly-Gagnon, et al., "Coherent detection of optical quadrature phase-shift keying signals with carrier phase estimation," *J. Lightwave Technol.*, vol. 24, pp. 12-21, 2006.
- [28] A.J. Viterbi and A.M. Viterbi, "Nonlinear estimation of PSK-modulated carrier phase with application to burst digital transmission," *IEEE Trans. Inf. Theory*, vol. 29, pp. 543-551, 1983.
- [29] W. Shieh and K.P. Ho, "Equalization-enhanced phase noise for coherent detection systems using electronic digital signal processing," *Opt. Express*, vol. 16, pp. 15718-15727, 2008.
- [30] C. Xie, "Local oscillator phase noise induced penalties in optical coherent detection systems using electronic chromatic dispersion compensation," *Proc. IEEE Opt. Fiber Commun. Conf.*, pp. OMT4, 2009.
- [31] T. Xu, et al., "Analytical BER performance in differential n-PSK coherent transmission system influenced by equalization enhanced phase noise," *Opt. Commun.*, vol. 334, pp. 222-227, 2015.
- [32] A.P.T. Lau, et al., "Equalization-enhanced phase noise for 100Gb/s transmission and beyond with coherent detection," *Opt. Express*, vol. 18, pp. 17239-17251, 2010.
- [33] I. Fatadin and S. J. Savory, "Impact of phase to amplitude noise conversion in coherent optical systems with digital dispersion compensation," *Opt. Express*, vol. 18, pp. 16273-16278, 2010.
- [34] T. Xu, et al., "Analytical estimation of phase noise influence in coherent transmission system with digital dispersion equalization," *Opt. Express*, vol. 19, pp. 7756-7768, 2011.
- [35] G. Jacobsen, et al., "EEPN and CD study for coherent optical nPSK and nQAM systems with RF pilot based phase noise compensation," *Opt. Express*, vol. 20, pp. 8862-8870, 2012.
- [36] T. Xu, et al., "Equalization enhanced phase noise in Nyquist-spaced superchannel transmission systems using multi-channel digital back-propagation," *Sci. Rep.*, vol.5, pp. 13990, 2015.
- [37] Q. Zhuge, M.H. Morsy-Osman, and D.V. Plant, "Low overhead intra-symbol carrier phase recovery for reduced-guard-interval CO-OFDM," *J. Lightwave Technol.*, vol. 31, pp. 1158-1169, 2013.
- [38] G. Jacobsen, et al., "Influence of pre- and post-compensation of chromatic dispersion on equalization enhanced phase noise in coherent multilevel systems," *J. Opt. Commun.*, vol. 32, pp. 257-261, 2011.
- [39] K.P. Ho and W. Shieh, "Equalization-enhanced phase noise in mode-division multiplexed systems," *J. Lightwave Technol.*, vol. 31, pp. 2237-2243, 2013.

- [40] G. Colavolpe, et al., "Impact of phase noise and compensation techniques in coherent optical systems," *J. Lightwave Technol.*, vol. 29, pp. 2790-2800, 2011.
- [41] R. Farhoudi, A. Ghazisaeidi, and L.A. Rusch, "Performance of carrier phase recovery for electronically dispersion compensated coherent systems," *Opt. Express*, vol. 20, pp. 26568-26582, 2012.
- [42] T. Yoshida, T. Sugihara, and K. Uto, "DSP-based optical modulation technique for long-haul transmission," *Proc. SPIE Next-Generation Opt. Commun.: Compon., Sub-Syst., Syst. IV*, vol. 9389, pp. 93890K, 2015.