# Wireless Powered Cooperative Jamming for Secrecy Multi-AF Relaying Networks

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Abstract—This paper studies secrecy transmission with the aid of a group of wireless energy harvesting-enabled amplifyand-forward (AF) relays performing cooperative jamming (CJ) and relaying. The source node in the network does simultaneous wireless information and power transfer with each relay employing a power splitting receiver in the first phase; each relay further divides its harvested power for forwarding the received signal and generating artificial noise for jamming the eavesdroppers in the second transmission phase. In the centralized case with global channel state information (CSI), we provide the closedform expressions for the optimal and/or suboptimal AF-relay beamforming vectors to maximize the achievable secrecy rate subject to individual power constraints of the relays, using the technique of semidefinite relaxation (SDR), which is proved to be tight. A fully distributed algorithm utilizing only local CSI at each relay is also proposed as a performance benchmark. Simulation results validate the effectiveness of the proposed multi-AF relaying with CJ over other suboptimal designs.

*Index Terms*—Artificial noise, cooperative jamming, amplify-and-forward relaying, secrecy communication, semidefinite relaxation, wireless energy harvesting, power splitting.

## I. INTRODUCTION

W IRELESS powered communication network has arisen as a new system with stable and self-sustainable power supplies in shaping future-generation wireless communications [1], [2]. The enabling technology, known as simultaneous wireless information and power transfer (SWIPT), has particularly drawn an upsurge of interests owing to the far-field electromagnetic power carried by

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radio-frequency (RF) signals that affluently exist in wireless communications. With the transmit power, waveforms, and dimensions of resources, etc., being all fully controllable, SWIPT promises to prolong the lifetime of wireless devices while delivering essential communication functionality, as will be important for low-power applications such as wireless sensor networks (WSNs) (see [3], [4] and the references therein).

On the other hand, privacy and authentication have increasingly become major concerns for wireless communications and physical (PHY)-layer security has emerged as a new layer of defence to realize perfect secrecy transmission in addition to the costly upper-layer techniques. In this regard, relay-assisted secure transmission was proposed [5], [6] and PHY-layer security enhancements by means of cooperative communications have since attracted much attention [7]–[14], [14]–[17].

In particular, cooperative schemes can be mainly classified into three categories: decode-and-forward (DF), amplify-andforward (AF), and cooperative jamming (CJ) [7] with CJ being the most relevant to PHY-layer security. Specifically, coordinated CJ refers to the scheme of generating a common jamming signal across all relay helpers against eavesdropping [7], [9]–[11], while uncoordinated CJ considers that each relay helper emits independent artificial noise (AN) to confound the eavesdroppers [13], [14]. In addition, when the direct link is broken between the transmitter (Tx) and the legitimate receiver (Rx), some of the relays have to be chosen to forward the information while others will perform CJ [16]. A recent paradigm that generalizes all the aforementioned cooperation strategies is *cooperative beamforming* (CB) mixed with CJ [17], where the available power at each relay is split into two parts: one for forwarding the confidential message and the other for CJ.

However, mixed CB-CJ approaches may be prohibitive in applications with low power devices because idle relays with limited battery supplies would likely prefer saving power for their own traffic to assisting others' communication. In light of this, SWIPT provides the incentive for potential helpers to perform dedicated CB mixed with CJ at no expense of its own power. Motivated by this, our work considers secrecy transmission from a Tx to a legitimate Rx with the aid of a set of single-antenna wireless energy harvesting (WEH)-enabled AF-operated relays in the presence of multiple single-antenna eavesdroppers. As a matter of fact, cooperative schemes that

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involve WEH-enabled relays operating with *dynamic power* splitting (DPS) [18] were early investigated in [19] and [20] without (w/o) security consideration. References [23], [24], and [25] advocated the dual use of AN signal for concurrently confusing the eavesdropper(s) and satisfying the energy harvesting (EH) requirements of Rx(s) in the SWIPT multipleinput single-output (MISO) and fading wiretap channels, respectively, while our work differs from them in the sense that our WEH-enabled Rxs will continue performing CB mixed with CJ for (secrecy) transmission in the second transmitslot after harvesting power as well as receiving information in the first transmit-slot of AF relaying. Reference [26], in spite of considering secure cooperative beamforming in a SWIPT-enabled AF relay network, employed conventional self-powered relay in the first transmit-slot and separate energy and information Rxs in the second transmit-slot, which also differs from ours.

In particular, motivated by the strong interest in SWIPT and the vast degree-of-freedom (DoF) achievable by cooperative relays, this paper aims to maximize the secrecy rate with the aid of WEH-enabled AF-operated relays, subject to the EH power constraints of individual relays. The scenario is applicable to WSNs, e.g., a remote health system where a moving patient reports its physical data to a health centre with the aid of intermediary sensor nodes installed on other patients in the vicinity. In this paper, we assume that there is no direct link between the source and the destination, and perfect global channel state information (CSI) is available for the case of centralized optimization.

It is worth pointing out that our work also differs from [22] where an efficient algorithm was proposed to maximize the secrecy rate by optimizing the PS ratios and AF relay beamforming. The difference is two-fold. First, AN was not considered in the second transmission phase in [22]. Second, they proposed an algorithm that is shown to converge to only a local optimum, as opposed to our work that gives the global optimal solutions for "CB mixed with CJ" with relays operating with *static power splitting (SPS)*, and "purely CB" with relays operating with DPS, respectively.

The rest of the paper is organized as follows. Section II describes two types of WEH-enabled Rx architecture for the AF relays and defines the secrecy rate of the relay wiretap channel. Section III then formulates the secrecy rate maximization problems that jointly optimize the AN (or CJ) and the AF-relay CB for the WEH-enabled relays operating with the two types of Rx. The problems are respectively solved by centralized schemes in Section IV and distributed approaches in Section V. Section VI provides simulation results to evaluate the performance of the proposed schemes. Finally, Section VII concludes the paper.

*Notations:* We use the uppercase boldface letters for matrices and lowercase boldface letters for vectors. The superscripts  $(\cdot)^T$ ,  $(\cdot)^{\dagger}$ ,  $(\cdot)^H$  and  $(\cdot)^*$  represent, respectively, the transpose, conjugate, conjugate transpose operations on vectors or matrices, and the optimum. In addition, trace $(\cdot)$  stands for the trace of a square matrix. Moreover,  $[\cdot]_{i,j}$  denotes the (i, j)th entry of a matrix, while  $\|\cdot\|$  and  $\|\cdot\|^2$  represent the Euclidean norm and the entry-wise absolute value square of a vector,

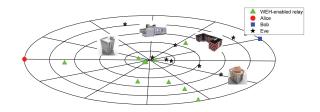


Fig. 1. The system model for an AF relay-assisted SWIPT WSN.

respectively. Also, diag(·) denotes a diagonal matrix with its diagonal specified by the given vector and  $[\cdot]_{i=1}^{N}$  represents an  $N \times 1$  vector with each element indexed by *i*. Furthermore,  $\cdot$  and  $\circ$  stand for product and Hadamard product, respectively.  $\mathbb{C}(\mathbb{R})^{x \times y}$  denotes the field of complex (real) matrices with dimension  $x \times y$  and  $\mathbb{E}[\cdot]$  indicates the expectation operation. Finally,  $(x)^+$  is short for max(0, x).

# II. SYSTEM MODEL

In this paper, we consider secrecy transmission in a SWIPT-enabled WSN as shown in Fig. 1, where a Tx (Alice) wants to establish confidential communication with the legitimate Rx (Bob) with the aid of N WEH-enabled sensors operating as AF relays,<sup>1</sup> denoted by  $\mathcal{K} = \{1, 2, ..., N\}$ , in the presence of multiple eavesdroppers (Eves), denoted by  $\mathcal{K} = \{1, 2, ..., K\}$ , all equipped with single antenna. Note that we only consider the case of no direct Tx-Eves links herein for the simplicity of exposition, since eavesdroppers are assumed to be distributed outside from a "security zone" [34] centered at the Tx, within which, eavesdroppers are otherwise detectable by the Tx [35].<sup>2</sup> We also assume that there is no direct link from the source to the destination due to, for instance, severe path loss.

We consider a two-hop relaying protocol based on two equal time slots and the duration of one transmit-slot is normalized to be one unit so that the terms "energy" and "power" are interchangeable with respect to (w.r.t.) one transmit-slot.

At the receiver of each AF relay, we introduce two types of WEH-enabled receiver architecture, namely, static power splitting (SPS) (Fig. 2(a)) and DPS (Fig. 2(b)), both of which allow the relay to harvest energy and receive information from the same received signal. Specifically, the receiver first splits a portion of  $\alpha_i$ , of the received power for EH and the rest  $1 - \alpha_i$  for information receiving (IR),  $\forall i \in \mathcal{N}$ . The  $\alpha_i$  portion of harvested power is further divided into two streams with a fraction  $\rho_i$  of the power used for generating the AN versus the rest  $1 - \rho_i$  used for amplifying the received signal, where  $y_{r_i}$  is the *i*th element of the received signal  $y_r \in \mathbb{C}^{N \times 1}$ , and  $0 \le \eta < 1$  denotes the EH efficiency. Note that DPS with adjustable  $\alpha_i$ 's is presently the most general receiver operation because practical circuits cannot directly process the information from the stream used for EH [18]. Furthermore, SPS is just a special case of DPS with  $\alpha_i = \bar{\alpha}_i$  fixed for the

<sup>1</sup> "N" only refers to the number of active sensors that are within direct connection to the Tx.

<sup>&</sup>lt;sup>2</sup>Note that even if there exist direct links, our problem formulation and solutions are still applicable w/o much difficulties in modification by incorporating destination-aided AN in the first transmit-slot (see [22]).

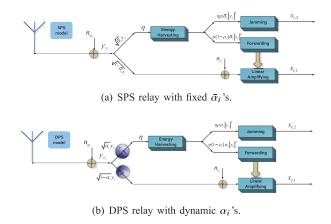


Fig. 2. Architectures of the receiver for WEH-enabled relay.

whole transmission duration. However, SPS, advocated for its ease of implementation, is introduced separately in the sequel for its simplified relay beamforming design.

In the first transmit-slot, the received signal at each individual relay can be expressed as

$$y_{r_i} = h_{sr_i} \sqrt{P_s s + n_{a,i}}, \quad \forall i, \tag{1}$$

where the transmit signal *s* is a circularly symmetric complex Gaussian (CSCG) random variable with zero mean and unit variance, denoted by  $s \sim CN(0, 1)$ ,  $h_{sr_i}$  denotes the complex channel from the Tx to the *i*th relay,  $P_s$  is the transmit power at the Tx, and  $n_{a,i}$  is the additive white Gaussian noise (AWGN) introduced by the receiving antenna of the *i*th relay, denoted by  $n_{a,i} \sim CN(0, \sigma_{n_a}^2)$ . As such, the linearly amplified baseband equivalent signal at the output of the *i*th relay is given by

$$x_{r_i 1} = \beta_i (\sqrt{1 - \alpha_i} y_{r_i} + n_{c,i}), \quad \forall i,$$
 (2)

where  $\beta_i$  denotes the complex AF coefficient, and  $n_{c,i}$  denotes the noise due to signal conversion from the RF band to baseband, denoted by  $n_{c,i} \sim CN(0, \sigma_{n_c}^2)$ . Since  $x_{r_i1}$  is constrained by the portion of the harvested power for forwarding, i.e.,  $\eta(1 - \rho_i)\alpha_i |y_{r_i}|^2$ ,  $\beta_i$  is accordingly given by

$$\beta_{i} = \sqrt{\frac{\eta(1-\rho_{i})\alpha_{i}|h_{sr_{i}}|^{2}P_{s}}{(1-\alpha_{i})|h_{sr_{i}}|^{2}P_{s} + (1-\alpha_{i})\sigma_{n_{a}}^{2} + \sigma_{n_{c}}^{2}}}e^{j\,\angle\beta_{i}},\quad(3)$$

where  $\measuredangle \beta_i$  denotes the phase of the AF coefficient for the *i*th relay.

Next, we introduce the CJ scheme. Denote the CJ signal generated from N relays by  $\mathbf{x}_{r2} = [x_{r12}, \ldots, x_{rN2}]^T$  and define its covariance matrix as  $\mathbf{S} = \mathbf{E}[\mathbf{x}_{r2}\mathbf{x}_{r2}^H]$ . Then the coordinated CJ transmission can be uniquely determined by the truncated eigenvalue decomposition (EVD) of  $\mathbf{S}$  given by  $\mathbf{S} = \tilde{V}\tilde{\boldsymbol{\Sigma}}\tilde{\boldsymbol{V}}^H$ , where  $\tilde{\boldsymbol{\Sigma}} = \text{diag}([\sigma_1, \ldots, \sigma_d])$  is a diagonal matrix with  $\sigma_j$ ,  $j = 1, \ldots, d$ , denoting all the positive eigenvalues of  $\mathbf{S}$  and  $\tilde{\boldsymbol{V}} \in \mathbb{C}^{N \times d}$  is the precoding matrix satisfying  $\tilde{\boldsymbol{V}}^H \tilde{\boldsymbol{V}} = \boldsymbol{I}$ . Note that  $d \leq N$  denotes the rank

of S which will be designed later. As a result, the CJ signal can be expressed as

$$\boldsymbol{x}_{r2} = \sum_{j=1}^{d} \sqrt{\sigma_j} \boldsymbol{v}_j \boldsymbol{s}'_j, \qquad (4)$$

where  $v_j$ 's are drawn from the columns of V, and  $s'_j$ 's are independent and identically distributed (i.i.d.) complex Gaussian variables denoted by  $s'_j \sim C\mathcal{N}(0, 1)$ . On the other hand,  $|x_{r_i2}|^2 \leq \eta \rho_i \alpha_i |y_{r_i}|^2$ ,  $\forall i$ , denotes the power constraint for jamming at the *i*th relay, which implies that

$$\operatorname{trace}(\boldsymbol{S}\boldsymbol{E}_{i}) \leq \eta \rho_{i} \alpha_{i} P_{s} |h_{sr_{i}}|^{2}, \quad \forall i,$$
(5)

where  $E_i$  is a diagonal matrix with its diagonal  $e_i$  (a unit vector with the *i*th entry equal to 1 and the rest equal to 0).

Note that the CJ scheme proposed above is of the most general form. For the special case when d = 1, i.e.,  $\mathbf{x}_{r2} = \sqrt{\sigma_1} \mathbf{v}_1 s'_1$ , each relay transmits a common jamming signal  $s'_1$  with their respective weight drawn from  $\mathbf{v}_1$  [7], [11]. This case is desirable in practice since it has the lowest complexity for implementation. In summary, the transmitted signal at the *i*th relay is given by

$$x_{r_i} = x_{r_i 1} + x_{r_i 2}, \quad \forall i.$$
 (6)

According to (6) together with (1), (2), and (4), the transmit signal from all relays can be expressed in a vector form as

$$\boldsymbol{x}_{r} = \boldsymbol{D}_{\beta\alpha}\boldsymbol{h}_{sr}\sqrt{P_{s}s} + \boldsymbol{D}_{\beta\alpha}\boldsymbol{n}_{a} + \boldsymbol{D}_{\beta}\boldsymbol{n}_{c} + \sum_{j=1}^{d}\sqrt{\sigma_{j}}\boldsymbol{v}_{j}s_{j}^{\prime}, \quad (7)$$

where  $D_{\beta\alpha}$  and  $D_{\beta}$  are, respectively, diagonal matrices with their diagonals composed of  $(\beta_1 \sqrt{1 - \alpha_1}, \dots, \beta_N \sqrt{1 - \alpha_N})^T$ and  $(\beta_1, \dots, \beta_N)^T$ . In addition,  $h_{sr} = [h_{sr_i}]_{i=1}^N$ ,  $n_a = [n_{a,i}]_{i=1}^N$ , and  $n_c = [n_{c,i}]_{i=1}^N$ .

In the second transmit-slot, the received signal at the desired receiver, i.e., Bob, is given by

$$y_d = \boldsymbol{h}_{rd}^T \boldsymbol{x}_r + n_d, \qquad (8)$$

where  $\mathbf{h}_{rd} = [h_{rid}]_{i=1}^{N}$  comprises complex channels from the *i*th relay to the Rx and  $n_d \sim CN(0, \sigma_{n_d}^2)$  is the corresponding receiving AWGN. By substituting (7) into (8),  $y_d$  can be expressed as

$$y_{d} = \boldsymbol{h}_{rd}^{T} \boldsymbol{D}_{\beta \alpha} \boldsymbol{h}_{sr} \sqrt{P_{s}} s + \boldsymbol{h}_{rd}^{T} \boldsymbol{D}_{\beta \alpha} \boldsymbol{n}_{a} + \boldsymbol{h}_{rd}^{T} \boldsymbol{D}_{\beta} \boldsymbol{n}_{c} + \boldsymbol{h}_{rd}^{T} \sum_{j=1}^{d} \sqrt{\sigma_{j}} \boldsymbol{v}_{j} s_{j}' + n_{d}.$$
(9)

The received signal at the *k*th Eve,  $\forall k \in \mathcal{K}$ , is given by

$$y_{e,k} = \boldsymbol{h}_{re,k}^{T} \boldsymbol{D}_{\beta \alpha} \boldsymbol{h}_{sr} \sqrt{P_s} s + \boldsymbol{h}_{re,k}^{T} \boldsymbol{D}_{\beta \alpha} \boldsymbol{n}_a + \boldsymbol{h}_{re,k}^{T} \boldsymbol{D}_{\beta} \boldsymbol{n}_c + \boldsymbol{h}_{re,k}^{T} \sum_{j=1}^{d} \sqrt{\sigma_j} \boldsymbol{v}_j s'_j + n_{e,k}, \quad (10)$$

where  $\mathbf{h}_{re,k} = [h_{rie,k}]_{i=1}^{N}$  denotes the complex channels from the relays to the *k*th Eve and  $n_{e,k} \sim C\mathcal{N}(0, \sigma_{n_{e,k}}^2)$  is the AWGN at the *k*th eavesdropper.

The mutual information for the Rx (Bob) is given by  $r_{S,D} = \frac{1}{2} \log_2(1 + SINR_{S,D})$ , and that for the *k*th Eve is

 $<sup>^{3}</sup>$ Note that the harvested power from the receiving antenna noise is considerably little compared with that transferred by the information signal, and therefore is safely removed in the sequel [4], [18].

 $r_{S,E,k} = \frac{1}{2} \log_2(1 + SINR_{S,E,k}), \forall k$ , where  $SINR_{S,D}$  (c.f. (12)) and  $SINR_{S,E,k}$  (c.f. (13)) denote their respective signal-to-interference-plus-noise ratios (SINRs).

Next, we define the secrecy rate as follows [7], [27].

$$r_{\rm sec} = \left( r_{\rm S,D} - \max_{k \in \mathcal{K}} r_{\rm S,E,k} \right)^+. \tag{11}$$

# III. PROBLEM FORMULATION

# A. AN-Aided Secrecy Relay Beamforming for SPS

In this section, we consider the secrecy rate maximization problem by jointly optimizing the AN beams, relay beam and their power allocations for WEH-enabled AF relays operating with SPS, i.e.,  $\alpha_i = \bar{\alpha}_i$ ,  $\forall i$ , is fixed. For the purpose of simplifying SINR expressions in (12) and (13), as shown at the bottom of this page, and facilitating the analysis in the sequel, we embark on a series of basic variable transformation to yield

$$r_{\rm S,D} = \frac{1}{2} \log_2 \left( 1 + \frac{P_s |\tilde{\boldsymbol{h}}_{sd}^T \boldsymbol{w}_1|^2}{\operatorname{trace}(\boldsymbol{S}\boldsymbol{h}_{rd}^\dagger \boldsymbol{h}_{rd}^T) + \boldsymbol{w}_1^H \boldsymbol{D}_{sd} \boldsymbol{w}_1 + \sigma_{n_d}^2} \right), \qquad (14)$$

where  $w_{1,i} = \sqrt{1 - \rho_i} e^{j \measuredangle \beta_i}$ ,

$$[\tilde{\boldsymbol{h}}_{sd}]_i \triangleq h_{sr_i} h_{r_i d} \sqrt{\frac{\eta \bar{\alpha}_i (1-\bar{\alpha}_i) |h_{sr_i}|^2 P_s}{(1-\bar{\alpha}_i) (|h_{sr_i}|^2 P_s + \sigma_{n_a}^2) + \sigma_{n_c}^2}},$$
(15)

and

$$[\boldsymbol{D}_{\hat{sd}}]_{i,i} = \frac{\eta \bar{a}_i P_s |h_{sr_i}|^2 |h_{r_id}|^2 ((1 - \bar{a}_i)\sigma_{n_a}^2 + \sigma_{n_c}^2)}{(1 - \bar{a}_i)(|h_{sr_i}|^2 P_s + \sigma_{n_a}^2) + \sigma_{n_c}^2},$$
(16)

 $\forall i \in \mathcal{N}$ . Similarly by letting

$$[\tilde{\boldsymbol{h}}_{se,k}]_{i} \triangleq h_{sr_{i}}h_{r_{i}e,k}\sqrt{\frac{\eta\bar{\alpha}_{i}(1-\bar{\alpha}_{i})|h_{sr_{i}}|^{2}P_{s}}{(1-\bar{\alpha}_{i})(|h_{sr_{i}}|^{2}P_{s}+\sigma_{n_{a}}^{2})+\sigma_{n_{c}}^{2}}}$$
(17)

and

$$[\mathbf{D}_{\hat{s}e,k}]_{i,i} \triangleq \frac{\eta \bar{\alpha}_i P_s |h_{sr_i}|^2 |h_{r_ie,k}|^2 ((1 - \bar{\alpha}_i) \sigma_{n_a}^2 + \sigma_{n_c}^2)}{(1 - \bar{\alpha}_i)(|h_{sr_i}|^2 P_s + \sigma_{n_a}^2) + \sigma_{n_c}^2}, \quad (18)$$

we have

$$r_{\rm S,E,k} = \frac{1}{2} \log_2 \left( 1 + \frac{P_s |\tilde{h}_{se,k}^T w_1|^2}{\operatorname{trace}(Sh_{re,k}^\dagger h_{re,k}^T) + w_1^H D_{\hat{se},k} w_1 + \sigma_{ne,k}^2} \right). \quad (19)$$

(5) can thus be reformulated as a per-relay jamming power constraint given by

$$\operatorname{trace}(\boldsymbol{SE}_{i}) \leq \eta \bar{\alpha}_{i} P_{s} |h_{sr_{i}}|^{2} (1 - |w_{1,i}|^{2}), \quad \forall i.$$
 (20)

Now, the secrecy rate maximization problem w.r.t.  $\rho_i$ 's,  $\measuredangle \beta_i$ 's and *S* for the SPS-based relays can be formulated as

(P1): 
$$\max_{\boldsymbol{w}_1,\boldsymbol{S}} \left( r_{\mathrm{S},\mathrm{D}} - \max_{k \in \mathcal{K}} r_{\mathrm{S},\mathrm{E},\mathrm{k}} \right)^+ \text{ s.t. (20), } \boldsymbol{S} \succeq \boldsymbol{0}.$$

#### B. AN-Aided Secrecy Relay Beamforming for DPS

Here, we consider the secrecy rate maximization problem for WEH-enabled AF relays with adjustable PS ratios  $\{\alpha_i\}$  by jointly optimizing the AN beams, relay beam, WEH PS ratios  $\{\alpha_i\}$ , and AN PS ratios  $\{\rho_i\}$ . In order to expose (12) and (13) in tractable forms for the joint optimization, consider the following variable transformation:

$$\begin{cases} u_{1,i} = \sqrt{\frac{a_i(1-a_i)(1-\rho_i)}{(1-a_i)(|h_{sr_i}|^2 P_s + \sigma_{n_a}^2) + \sigma_{n_c}^2}} e^{j \measuredangle \beta_i} \\ u_{2,i} = \sqrt{\frac{a_i(1-\rho_i)}{(1-a_i)(|h_{sr_i}|^2 P_s + \sigma_{n_a}^2) + \sigma_{n_c}^2}} , \quad \forall i.$$
(23)

Using this, SINR<sub>S,D</sub> and SINR<sub>S,E,k</sub>,  $\forall k$ , can be alternatively expressed as (21) and (22), as shown at the bottom of the next page, where  $s_{sd} = [h_{sr_i}h_{r_id}\sqrt{\eta|h_{sr_i}|^2P_s}]_{i=1}^N$ ,  $s_{se,k} = [h_{sr_i}h_{r_ie,k}\sqrt{\eta|h_{sr_i}|^2P_s}]_{i=1}^N$ ,  $\forall k$ , and  $c_{0,i} = \eta P_s|h_{sr_i}|^2$ ,  $\forall i$ .

Then, we recast the constraints w.r.t. S,  $\alpha_i$ 's, and  $\rho_i$ 's to those w.r.t. the transformed variables  $u_{1,i}$ 's and  $u_{2,i}$ 's as follows.

$$\begin{cases} \alpha_{i} = 1 - \frac{|u_{1,i}|^{2}}{|u_{2,i}|^{2}} \\ \rho_{i} = 1 - \frac{|u_{2,i}|^{2}(c_{1,i}|u_{1,i}|^{2} + \sigma_{n_{c}}^{2}|u_{2,i}|^{2})}{|u_{2,i}|^{2} - |u_{1,i}|^{2}} \end{cases}, \quad \forall i,$$
(24)

where  $c_{1,i} = P_s |h_{sr_i}|^2 + \sigma_{n_a}^2$ . Replacing  $\alpha_i$ 's and  $\rho_i$ 's with (24), (5) is reformulated as

$$\operatorname{trace}(\mathbf{SE}_{i}) \leq c_{0,i} \left( 1 - \frac{|u_{2,i}|^{2} (c_{1,i} |u_{1,i}|^{2} + \sigma_{n_{c}}^{2} |u_{2,i}|^{2})}{|u_{2,i}|^{2} - |u_{1,i}|^{2}} \right) \times \left( 1 - \frac{|u_{1,i}|^{2}}{|u_{2,i}|^{2}} \right), \quad \forall i.$$
(25)

On the other hand, since  $\alpha_i \ge 0$  and  $\rho_i \ge 0$ ,  $\forall i$ , it follows from (24) that

$$|u_{1,i}|^2 - |u_{2,i}|^2 \le 0, \ \forall i,$$
(26)

$$|u_{2,i}|^2 (c_{1,i}|u_{1,i}|^2 + \sigma_{n_c}^2 |u_{2,i}|^2) \le |u_{2,i}|^2 - |u_{1,i}|^2, \quad \forall i.$$
(27)

As such, the secrecy rate maximization problem for the DPS-based relays becomes

(P2): 
$$\max_{u_1, u_2, S} \left( \frac{1}{2} \log_2(1 + (21)) - \frac{1}{2} \log_2(1 + \max_{k \in \mathcal{K}} (22)) \right)^+$$
  
s.t. (25), (26), (27), and  $S \succeq 0$ .

$$\operatorname{SINR}_{S,D} = \frac{P_s |\boldsymbol{h}_{rd}^T \boldsymbol{D}_{\beta\alpha} \boldsymbol{h}_{sr}|^2}{\operatorname{trace}(\boldsymbol{S}\boldsymbol{h}_{rd}^\dagger \boldsymbol{h}_{rd}^T) + \sigma_{n_a}^2 \|\boldsymbol{h}_{rd}^T \boldsymbol{D}_{\beta\alpha}\|^2 + \sigma_{n_c}^2 \|\boldsymbol{h}_{rd}^T \boldsymbol{D}_{\beta}\|^2 + \sigma_{n_d}^2}$$
(12)

$$\operatorname{SINR}_{S,E,k} = \frac{P_{s} |\boldsymbol{n}_{re,k} \boldsymbol{D}_{\beta \alpha} \boldsymbol{n}_{sr}|^{2}}{\operatorname{trace}(\boldsymbol{S} \boldsymbol{h}_{re,k}^{\dagger} \boldsymbol{h}_{re,k}^{T}) + \sigma_{n_{a}}^{2} \|\boldsymbol{h}_{re,k}^{T} \boldsymbol{D}_{\beta \alpha}\|^{2} + \sigma_{n_{c}}^{2} \|\boldsymbol{h}_{re,k}^{T} \boldsymbol{D}_{\beta}\|^{2} + \sigma_{n_{e},k}^{2}}$$
(13)

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#### IV. CENTRALIZED SECURE AF RELAYING

In this section, we resort to centralized approaches to solve problem (P1) and (P2), respectively, assuming that there is a central optimizer that is able to collect global CSI, perform the optimization and necessary secrecy code designs, and broadcast to relays their individual optimized parameters.

## A. Optimal Solutions for SPS

To start with, we recast (P1) into a two-stage problem by introducing a slack variable  $\tau$ . First of all, we solve the epigraph reformulation of (P1) with a fixed  $\tau \in (0, 1]$  as

(P1.1): 
$$\max_{\boldsymbol{w}_{1},\boldsymbol{S} \succeq \boldsymbol{0}} \frac{P_{s} |\tilde{\boldsymbol{h}}_{sd}^{T} \boldsymbol{w}_{1}|^{2}}{\operatorname{trace}(\boldsymbol{S}\boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T}) + \boldsymbol{w}_{1}^{H} \boldsymbol{D}_{sd} \boldsymbol{w}_{1} + \sigma_{n_{d}}^{2}}$$
  
s.t. (20) and  $\forall k$ ,  
$$1 + \frac{P_{s} |\tilde{\boldsymbol{h}}_{se,k}^{T} \boldsymbol{w}_{1}|^{2}}{\operatorname{trace}(\boldsymbol{S}\boldsymbol{h}_{re,k}^{\dagger} \boldsymbol{h}_{re,k}^{T}) + \boldsymbol{w}_{1}^{H} \boldsymbol{D}_{se,k} \boldsymbol{w}_{1} + \sigma_{n_{e},k}^{2}} \leq 1/\tau.$$

Defining  $f_1(\tau)$  as the optimum value of (P1.1) and denoting  $H_1(\tau) = \tau f_1(\tau)$ , the objective function of (P1) is given by

$$\frac{1}{2}\log_2(1+f_1(\tau)) - \frac{1}{2}\log_2(1/\tau) = \frac{1}{2}\log_2(\tau+H_1(\tau)),$$
(28)

where  $(\cdot)^+$  in the objective function has been omitted and we claim a zero secrecy rate if (28) admits a negative value. As a result, (P1) can be equivalently given by

(P1.2): 
$$\max_{\tau_{\min,1} \le \tau \le 1} \log_2(\tau + H_1(\tau)).$$

Note that this single-variable optimization problem allows for simple one-dimension search over  $\tau \in [\tau_{\min,1}, 1]$ , assuming that  $H_1(\tau)$  is attainable. As the physical meaning of  $1/\tau - 1$  in (P1.1) can be interpreted as the maximum permitted SINR for the best eavesdropper's channel, feasibility for a non-zero secrecy rate implies that

$$\tau \stackrel{(a)}{\geq} \frac{1}{1 + P_s \|\tilde{\boldsymbol{h}}_{sd}\|^2 \|\boldsymbol{w}_1\|^2 / \sigma_{n_d}^2} \\ \stackrel{(b)}{\geq} \frac{1}{1 + NP_s \|\tilde{\boldsymbol{h}}_{sd}\|^2 / \sigma_{n_d}^2} = \tau_{\min,1},$$
(29)

where Cauchy-Schwarz inequality has been applied in (a), and (b) follows from  $|w_{1,i}|^2 \leq 1$ ,  $\forall i \in \mathcal{N}$ .

The above epigraph reformulation of non-convex problems like (P1) has been widely employed in the literature [17], [32], and (P1.2) admits the same optimal value as (P1) while (P1.1) with the optimal  $\tau$  provides the corresponding optimal solution to (P1). We summarize the steps for solving (P1)

here: given any  $\tau \in [\tau_{\min,1}, 1]$ , solve (P1.1) to obtain  $H_1(\tau)$ ; solve (P1.2) via a one-dimensional search over  $\tau$ . Before developing solutions to (P1.1), we have the lemma below.

<u>Lemma</u> 4.1:  $H_1(\tau)$  is a concave function of  $\tau$ .

*Proof:* We only outline the sketch of the proof herein due to the space limitation. The interested reader can refer to a longer version of this paper [28, Appendix]. First, we formulate the dual problem of (P1.1-SDP), and then we investigate the property of  $H_1(\tau)$  by looking into the objective function of the dual problem through strong duality.

<u>Remark</u> 4.1: Using Lemma 4.1, it is easy to verify that  $\frac{1}{2}\log_2(\tau + H_1(\tau))$  is also a concave function of  $\tau$  according to the composition rule [29, p. 84], which allows for a more effective search for the optimum  $\tau$ , e.g., bi-section method, than the exhaustive search used in [23]. Moreover, although  $H_1(\tau)$  is not differentiable w.r.t.  $\tau$ , the bi-section method can still be implemented, and the involved algorithm will be given later in Section IV-B.

In the sequel, we focus on solving (P1.1). By introducing  $X_1 = \boldsymbol{w}_1 \boldsymbol{w}_1^H$  and ignoring the rank-one constraint on  $X_1$ , (P1.1) can be alternatively solved by

(P1.1-SDR) :

$$\begin{cases} \max_{X_1, S \succeq \mathbf{0}} \frac{\tau P_s \operatorname{trace}(X_1 \tilde{\mathbf{h}}_{sd}^{\dagger} \tilde{\mathbf{h}}_{sd}^T)}{\operatorname{trace}(S h_{rd}^{\dagger} h_{rd}^T) + \operatorname{trace}(X_1 D_{sd}) + \sigma_{rd}^2} \\ \text{s.t.} \frac{P_s \operatorname{trace}(X_1 \tilde{\mathbf{h}}_{se,k}^{\dagger} \tilde{\mathbf{h}}_{se,k}^T)}{\operatorname{trace}(S h_{re,k}^{\dagger} h_{re,k}^T) + \operatorname{trace}(X_1 D_{se,k}) + \sigma_{re,k}^2} \leq \frac{1}{\tau} - 1, \quad \forall k, \\ \operatorname{trace}((S + \eta \tilde{\alpha}_i P_S | h_{sr_i} |^2 X_1) E_i) \leq \eta \tilde{\alpha}_i P_S | h_{sr_i} |^2, \quad \forall i. \end{cases}$$

Note that the objective function has been multiplied by  $\tau$  compared with that of (P1.1) for ready computation of  $H_1(\tau)$ .

Although (P1.1-SDR) is made easier to solve than (P1.1) by rank relaxation, it is still a quasi-convex problem considering the linear fractional form of the objective function and constraints [36], to which Charnes-Cooper transformation [30] will be applied for equivalent convex reformulation. Specifically, by substituting  $X_1 = \hat{X}_1/\xi$  and  $S = \hat{S}/\xi$  into (P1.1-SDR), it follows that

$$(P1.1-SDP): \\ \begin{cases} \max_{\hat{X}_{1},\hat{S} \succeq \mathbf{0}, \xi \ge 0} P_{s} \operatorname{trace}(\hat{X}_{1} \tilde{\boldsymbol{h}}_{sd}^{\dagger} \tilde{\boldsymbol{h}}_{sd}^{T}) \\ \text{s.t. } \operatorname{trace}(\hat{S} \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T}) + \operatorname{trace}(\hat{X}_{1} \boldsymbol{D}_{sd}) + \xi \sigma_{n_{d}}^{2} = \tau, \\ (\frac{1}{\tau} - 1) \left( \operatorname{trace}(\hat{S} \boldsymbol{h}_{re,k}^{\dagger} \boldsymbol{h}_{re,k}^{T}) + \operatorname{trace}(\hat{X}_{1} \boldsymbol{D}_{se,k}) + \xi \sigma_{n_{e},k}^{2} \right) \\ \ge P_{s} \operatorname{trace}(\hat{X}_{1} \tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^{T}), \quad \forall k, \\ \operatorname{trace}((\hat{S} + \eta \bar{\alpha}_{i} P_{s} | \boldsymbol{h}_{sr_{i}} |^{2} \hat{X}_{1}) \boldsymbol{E}_{i}) \le \xi \eta \bar{\alpha}_{i} P_{s} | \boldsymbol{h}_{sr_{i}} |^{2}, \quad \forall i. \end{cases}$$

Problem (P1.1-SDP) can now be optimally and efficiently solved using interior-point based methods by some off-the-shelf convex optimization toolboxes, e.g., CVX [31].

$$SINR_{S,D} = \frac{P_{s}|s_{sd}^{T}\boldsymbol{u}_{1}|^{2}}{\operatorname{trace}(\boldsymbol{S}\boldsymbol{h}_{rd}^{\dagger}\boldsymbol{h}_{rd}^{T}) + \sigma_{n_{a}}^{2}\boldsymbol{u}_{1}^{H}\operatorname{diag}(\boldsymbol{c}_{0} \circ \|\boldsymbol{h}_{rd}\|.^{2})\boldsymbol{u}_{1} + \sigma_{n_{c}}^{2}\boldsymbol{u}_{2}^{H}\operatorname{diag}(\boldsymbol{c}_{0} \circ \|\boldsymbol{h}_{rd}\|.^{2})\boldsymbol{u}_{2} + \sigma_{n_{d}}^{2}}{P_{s}|s_{se,k}^{T}\boldsymbol{u}_{1}|^{2}}$$

$$SINR_{S,E,k} = \frac{P_{s}|s_{se,k}^{T}\boldsymbol{u}_{1}|^{2}}{\operatorname{trace}(\boldsymbol{S}\boldsymbol{h}_{re,k}^{\dagger}\boldsymbol{h}_{re,k}^{T}) + \sigma_{n_{a}}^{2}\boldsymbol{u}_{1}^{H}\operatorname{diag}(\boldsymbol{c}_{0} \circ \|\boldsymbol{h}_{re,k}\|.^{2})\boldsymbol{u}_{1} + \sigma_{n_{c}}^{2}\boldsymbol{u}_{2}^{H}\operatorname{diag}(\boldsymbol{c}_{0} \circ \|\boldsymbol{h}_{re,k}\|.^{2})\boldsymbol{u}_{2} + \sigma_{n_{e},k}^{2}}$$

$$(22)$$

*Proposition 4.1:* We have the following results:

- 1) The optimal solution to (P1.1-SDP) satisfies  $\operatorname{rank}(\hat{X}_{1}^{*}) = 1;$
- 2)  $\hat{X}_1^* = \hat{w}_1^* \hat{w}_1^{*H}$ , where  $\hat{w}_1^*$  is given by

$$\hat{\boldsymbol{w}}_{1}^{*} = \sqrt{\frac{\tau - \zeta^{*} \sigma_{n_{d}}^{2} - \operatorname{trace}(\hat{\boldsymbol{S}}^{*} \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T})}{\operatorname{trace}(\hat{\boldsymbol{w}}_{1} \hat{\boldsymbol{w}}_{1}^{H} \boldsymbol{D}_{\hat{sd}})}} \hat{\boldsymbol{w}}_{1}, \quad (30)$$

in which  $\hat{\boldsymbol{w}}_1$  is given in Appendix;

3)  $\operatorname{rank}(\hat{\boldsymbol{S}}^*) \leq \min(K, N).$ 

*Proof:* Please refer to Appendix.

Proposition 4.1 implies that the rank-one relaxation of (P1.1-SDR) from (P1.1) is tight for any given  $\tau$ . The  $\rho^*$ 's and  $\measuredangle \beta_i^*$ 's can thus be retrieved from the magnitude and angle of  $\boldsymbol{w}_1^*$ , respectively, by applying EVD to  $\boldsymbol{X}_1^*$ .

# B. Proposed Solutions for DPS

Similar to Section IV-A, in this section, we aim at solving the two-stage reformulation of (P2) by introducing a slack variable  $\tau \in [\tau_{\min,2}, 1]$ . First, for a given  $\tau$ , we solve

(P2.1): 
$$\max_{u_1, u_2, S} (21)$$
 s.t.  $(22) \le \frac{1}{\tau}, \ \forall k, \ (25) - (27).$ 

Next, denoting  $\tau f_2(\tau)$  by  $H_2(\tau)$  (c.f. (31)), where  $f_2(\tau)$  is the optimum value for problem (P2.1), we solve the following problem that attains the same optimum value as (P2):

(P2.2): 
$$\max_{\tau} \log_2(\tau + H_2(\tau))$$
 s.t.  $\tau_{\min,2} \le \tau \le 1$ ,

where  $\tau_{\min,2}$  is similarly derived as  $\tau_{\min,1}$  so that we directly arrive at

$$\tau \geq \frac{1}{1 + P_s \|\mathbf{s}_{sd}\|^2 \sum_{i=1}^{N} \frac{1}{\sigma_{n_d}^2 (|h_{sr_i}|^2 P_s + \sigma_{n_d}^2 + \sigma_{n_c}^2)}},$$
(33)

which is denoted by  $\tau_{\min,2}$ . We claim that (P2.2) can be solved by bi-section for  $\tau$  over the interval [ $\tau_{\min,2}$ , 1] assuming that  $H_2(\tau)$  is valid for any given  $\tau$  (Otherwise a zero secrecy rate, i.e.,  $H_2(\tau) = 0$ , is returned.), since  $H_2(\tau)$  has the following property.

<u>Lemma</u> 4.2:  $H_2(\tau)$  is a concave function of  $\tau$ .

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*Proof:* The proof is similar to that for Lemma 4.1, and thus is omitted.

It is also seen that how to attain  $H_2(\tau)$  forms the main thrust for solving (P2). However, the constraints in (25), (26) and (27) are not convex w.r.t.  $u_{1,i}$  and/or  $u_{2,i}$ ,  $\forall i$ , due to their high orders and multiplicative structure. (P2.1) thus turns out to be very hard to solve in general. To cope

with these non-convex constraints, we introduce the following lemma.

<u>Lemma</u> 4.3 ([21]): The restricted hyperbolic constraints which have the form  $\mathbf{x}^H \mathbf{x} \leq yz$ , where  $\mathbf{x} \in \mathbb{C}^{N \times 1}$ ,  $y, z \geq 0$ , are equivalent to rotated second-order cone (SOC) constraints as follows.

$$\left\| \begin{pmatrix} 2x\\ y-z \end{pmatrix} \right\| \le y+z. \tag{34}$$

For convenience, denoting  $|u_{1,i}|^2$ ,  $|u_{2,i}|^2$ , trace(*SE<sub>i</sub>*) by  $x_i$ ,  $y_i$ , and  $z_i$ , respectively,  $\forall i$ , (25) can be rewritten as

$$z_{i} \leq c_{0,i} \left( 1 - \frac{y_{i}(c_{1,i}x_{i} + \sigma_{n_{c}}^{2}y_{i})}{y_{i} - x_{i}} \right) \left( 1 - \frac{x_{i}}{y_{i}} \right)$$
  

$$\Leftrightarrow \frac{z_{i}}{c_{0,i}} \leq 1 - \frac{x_{i}}{y_{i}} - (c_{1,i}x_{i} + \sigma_{n_{c}}^{2}y_{i})$$
  

$$\Leftrightarrow (\sigma_{n_{c}}y_{i})^{2} + \left( \sqrt{\left( 1 - \frac{z_{i}}{c_{0,i}} \right) \frac{1}{c_{1,i}}} \right)^{2}$$
  

$$\leq \left( 1 - \frac{z_{i}}{c_{0,i}} - c_{1,sr,i}x_{i} \right) \left( y_{i} + \frac{1}{c_{1,i}} \right).$$
(35)

According to (5) and (23), it is easily verified that  $1 - \frac{z_i}{c_{0,sr,i}} - c_{1,sr,i}x_i > 1 - \rho_i \alpha_i - (1 - \rho_i)\alpha_i \ge 0$ . Hence, (35) is eligible for Lemma 4.3, which is reformulated into the SOC constraint:

$$\left\| \begin{array}{c} 2\sigma_{n_{c}} y_{i} \\ 2\sqrt{\left(1 - \frac{z_{i}}{c_{0,i}}\right) \frac{1}{c_{1,i}}} \\ \left(1 - \frac{z_{i}}{c_{0,i}} - c_{1,i}x_{i}\right) - \left(y_{i} + \frac{1}{c_{1,i}}\right) \\ \leq \left(1 - \frac{z_{i}}{c_{0,i}} - c_{1,i}x_{i}\right) + \left(y_{i} + \frac{1}{c_{1,i}}\right).$$
(36)

Similarly, (27) can be simplified as  $y_i(c_{1,i}x_i + \sigma_{n_c}^2 y_i) \le y_i - x_i$ , and after some manipulation, it is recast into a constraint of the restricted hyperbolic form as

$$\left(\sigma_{n_c} y_i\right)^2 + \left(\sqrt{\frac{1}{c_{1,i}}}\right)^2 \le \left(1 - c_{1,i} x_i\right) \left(y_i + \frac{1}{c_{1,i}}\right).$$
 (37)

(37) is thus, in line with Lemma 4.3, equivalent to an SOC constraint given by

$$\left\| \begin{array}{c} 2\sigma_{n_{c}}y_{i} \\ 2\sqrt{\frac{1}{c_{1,i}}} \\ \left(1-c_{1,i}x_{i}\right) - \left(y_{i} + \frac{1}{c_{1,i}}\right) \end{array} \right\| \leq \left(1-c_{1,i}x_{i}\right) + \left(y_{i} + \frac{1}{c_{1,i}}\right).$$

$$(38)$$

At last, (26) is a linear constraint w.r.t.  $x_i$  and  $y_i$  given by

$$x_i - y_i \le 0, \ \forall i. \tag{39}$$

$$\frac{\tau P_s \operatorname{trace}(\boldsymbol{U}_1 \boldsymbol{s}_{sd}^{\dagger} \boldsymbol{s}_{sd}^{T})}{\operatorname{trace}(\overline{\boldsymbol{S}} \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T}) + \operatorname{trace}((\sigma_{n_a}^2 \boldsymbol{U}_1 + \sigma_{n_c}^2 \boldsymbol{U}_2) \operatorname{diag}(\boldsymbol{c}_0 \circ \|\boldsymbol{h}_{rd}\|^2)) + \sigma_{n_d}^2}$$
(31)

$$\frac{P_{s}\operatorname{trace}(\boldsymbol{U}_{1}\boldsymbol{s}_{se,k}^{*}\boldsymbol{s}_{se,k}^{T})}{\operatorname{trace}(\overline{\boldsymbol{S}}\boldsymbol{h}_{re,k}^{\dagger}\boldsymbol{h}_{re,k}^{T}) + \operatorname{trace}((\sigma_{n_{a}}^{2}\boldsymbol{U}_{1} + \sigma_{n_{c}}^{2}\boldsymbol{U}_{2})\operatorname{diag}(\boldsymbol{c}_{0} \circ \|\boldsymbol{h}_{re,k}\|^{2})) + \sigma_{n_{e},k}^{2}} \leq \frac{1}{\tau}$$
(32)

Note that (25)–(27) have so far been equivalently transformed into the SOC constraints (36), the linear constraints (39), as well as (38), the latter two of which are jointly convex w.r.t.  $x_i$  and  $y_i$ ,  $\forall i$ . However, (36) is still not convex w.r.t.  $z_i$ ,  $\forall i$ , yet. To circumvent this, in the sequel we propose to solve problem (P2) by alternating optimization. The upshot of the algorithm is that first we fix S by  $\overline{S}$  and thus  $z_i$  by  $\overline{z}_i = \text{trace}(\overline{S}E_i)$ ,  $\forall i$ , and solve problem (P2')<sup>4</sup> to find the optimal { $\alpha^*$ }, { $\rho^*$ } and { $\angle \beta_i$ } via (P2'.1) and (P2'.2); then with  $\overline{a}_i = \alpha_i^*$ ,  $\forall i$ , we devise the optimal solution derived in Section IV-A to obtain the optimal CJ covariance, viz,  $S^*$ , and thus  $z_i^* = \text{trace}(S^*E_i)$ ,  $\forall i$ ; finally, by updating  $\overline{S} = S^*$  and  $\overline{z}_i = z_i^*$ ,  $\forall i$ , problems (P2') and (P1) are iteratively solved until they converge.

The remaining challenges lie in solving problem (P2'.1) now that (36), (38) and (39) are all made convex w.r.t. their variables  $x_i$ ,  $y_i$ ,  $\forall i$ . Similar to that for (P1.1), we introduce  $U_1 = u_1 u_1^H$  and  $U_2 = u_2 u_2^H$  and exempt problem (P2'.1) from rank( $U_1$ ) = 1 and rank( $U_2$ ) = 1 as follows:

$$(P2'.1-SDR): \begin{cases} \max_{U_1, U_2 \geq 0, \{x_i\}, \{y_i\}} H_2(\tau) \\ \text{s.t. (32), } \forall k, (36), (38), (39), \\ \operatorname{trace}(U_1 E_i) = x_i, \operatorname{trace}(U_2 E_i) = y_i, \forall i. \end{cases}$$

Recalling the procedure to deal with (P1.1-SDR), we now apply Charnes-Cooper transformation to convert (P2'.1-SDR) into a convex problem, denoted by (P2'.1-SDP), by replacing  $U_1$  and  $U_2$  with  $\hat{U}_1/\xi$  and  $\hat{U}_2/\xi$ , respectively. The solution for (P2'.1-SDP) is tight and characterized by the following proposition.

Proposition 4.2: We have the following results:

- 1) The optimal solution to (P2'.1-SDP) satisfies rank $(\hat{U}_1^*) = 1$  such that  $\hat{U}_1^* = \hat{u}_1^* \hat{u}_1^{*H}$ ;
- 2)  $\hat{u}_1^*$  is given by

$$\hat{\boldsymbol{u}}_{1}^{*} = \sqrt{\frac{\tau - \boldsymbol{\zeta}^{*} \sigma_{n_{d}}^{2} - \sigma_{n_{c}}^{2} \operatorname{trace}(\hat{\boldsymbol{U}}_{2}^{*} \boldsymbol{C}_{rd}) - \boldsymbol{\zeta}^{*} \operatorname{trace}(\overline{\boldsymbol{S}} \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T})}{\sigma_{n_{d}}^{2} \operatorname{trace}(\hat{\boldsymbol{u}}_{1} \hat{\boldsymbol{u}}_{1}^{H} \boldsymbol{C}_{rd})} \hat{\boldsymbol{u}}_{1}, (40)$$

where  $\hat{\boldsymbol{u}}_{1} = (\boldsymbol{\Xi}' + \sum_{k=1}^{K} \theta_{k}^{*} P_{s} \boldsymbol{s}_{se,k}^{\dagger} \boldsymbol{s}_{se,k}^{T})^{-1} \boldsymbol{s}_{sd}^{\dagger},$  $\boldsymbol{C}_{rd} = \text{diag}(\boldsymbol{c}_{0} \circ \|\boldsymbol{h}_{rd}\|^{2});$ 

3)  $\hat{U}_{2}^{*}$ , of which the diagonal entries compose a vector denoted by  $\hat{u}_{2}^{*}$ , can be reconstructed by  $\hat{u}_{2}^{*}.^{\frac{1}{2}}\hat{u}_{2}^{*H}.^{\frac{1}{2}}$ , where  $(\cdot).^{\frac{1}{2}}$  denotes the element-wise square root.

**Proof:** We only outline the sketch of the proof herein due to the space limitation. The interested reader can refer to a longer version of this paper [28, Appendix C]. First, we show that problem (P2'.1-SDR) is equivalent to another problem w/o equality constraints; next, we devise the Charnes-Cooper transformation to the equivalent problem and derive its partial Lagrangian in terms of the optimization variables requiring proof of rank one; then, in accordance with the resultant KKT conditions, the rank property of  $\hat{U}_1^*$  is investigated by discussing the positive definiteness of a constructive matrix as similar to Appendix.

TABLE I Algorithm for Solving (P2)

**Require:**  $S^*$ ;  $r^*_{\text{SPS}}$  that denotes the optimum value for (P1) given  $\bar{\alpha}_i = .5$ , 1:  $ii \leftarrow 0, r_{\text{sec}}^{(ii)} \leftarrow r_{\text{SPS}}^*$ 2: repeat . *ii ← ii* + 1 3. 
$$\begin{split} \mathbf{\bar{S}} &\leftarrow \mathbf{S}^*, \ \bar{z}_i \leftarrow \operatorname{trace}(\mathbf{S}^* \mathbf{E}_i), \ \forall i, \text{ and solve (P2'):} \\ kk \leftarrow 0, \ r_{\mathrm{DPS}}^{(0)} \leftarrow 10^{-6}, \ r_{\mathrm{DPS}}^{(1)} \leftarrow 10, \ l \leftarrow \tau_{\min,2}, \ u \leftarrow 1 \\ \\ \text{while } |r_{\mathrm{DPS}}^{(kk+1)} - r_{\mathrm{DPS}}^{(kk)}| / r_{\mathrm{DPS}}^{(kk)} > \epsilon_b \ \mathbf{do} \\ kk \leftarrow kk + 1, \ \tau \leftarrow \frac{l+u}{2} \end{split}$$
4: 5: 6: 7: 8: solve (P2'.1) and 9: return  $H_2(\tau)$  $\begin{array}{l} r_{\text{DPS}}^{(k\,k+1)} \leftarrow \frac{1}{2} \log_2(\tau + H_2(\tau)) \\ r_{\text{temp}} \leftarrow \frac{1}{2} \log_2(\tilde{\tau} + H_2(\tilde{\tau})), \text{ where } \tilde{\tau} \leftarrow \max(\tau - \Delta\tau, \tau_{\min,1}) \text{ and } \end{array}$ 10: 11.  $\Delta \tau > 0$  denotes an arbitrary small value. if  $r_{\text{DPS}}^{(k\,k+1)} \leq r_{\text{temp}}$  then  $u \leftarrow \tau$ 12: 13: 14: else 15:  $l \leftarrow \tau$ end if 16:  $17 \cdot$ end while **return**  $U_1^*, U_2^*$ , and obtain  $\{\alpha_i^*\}$  according to (24)  $\bar{\alpha}_i \leftarrow \alpha_i^*, \forall i$ , and solve (P1) via (P1.1) and (P1.2) 18: 19: **return**  $X_1^*$ ,  $S^*$ , and obtain  $\{\rho_i^*\}$  and  $\{\measuredangle \beta_i^*\}$  according to  $w_{1,i}^* =$ 20:  $\sqrt{1-\rho_i^*}e^{j\measuredangle\beta_i^*},\,\forall i$ 21: Update  $r_{sec}^{(ii)}$  according to (11) 22: until  $r_{sec}^{(ii)} - r_{sec}^{(ii-1)} \le \epsilon_0$ Ensure:  $\{\alpha_i^*\}, \{\rho_i^*\}, \{\Delta\beta_i^*\}$ , and  $S^*$ 

<u>Remark</u> 4.2: The proof for both Propositions 4.1 and 4.2 relies on an important argument that the dual variables associated with  $\hat{X}_1$  and  $\hat{U}_1$  are both shown to take on a special structure, that is, a full-rank matrix minus a rank-one matrix. Note that this observation plays a key role in proving the rank-one property of  $\hat{X}_1^*$  and  $\hat{U}_1^*$ , which is also identified in [17, Appendix C].

The  $\alpha_i^*$ 's and  $\rho_i$ 's are thus attained according to (24) via EVD of  $U_1^*$  and  $U_2^*$ . The proposed algorithm for solving (P2) is presented in Table I.

## V. DISTRIBUTED ALGORITHMS

In this section, we investigate heuristic algorithms to solve problems (P1) and (P2) in a completely distributed fashion. Note that different from the paradigm of *distributed optimiza*tion that allows for certain amount of information exchange based on which iterative algorithms are developed to gradually improve the system performance, we herein assume that each individual relay can only make decision based on its local CSIs, namely,  $h_{sr_i}$ ,  $h_{r_id}$ ,  $h_{r_ie}$ ,  $\forall i$ , and there is no extra means of information acquisition for ease of implementation. The purpose for such an algorithm is twofold: on one hand, we aim to answer the question that in the least favorable situation, namely, no coordination over the relays, how to improve the achievable secrecy rate of the system? On the other hand, it provides a lower-bound for the centralized schemes proposed in Section IV, which sheds light upon the trade-off achievable between secrecy performance and complexity.

Furthermore, we emphasize the jamming scheme that is different from the CJ in the centralized schemes. Unlike the CJ signal coordinately transmitted by all relays, in the distributed implementation, each relay is only able to generate

<sup>&</sup>lt;sup>4</sup>Note that we denote problem (P2) ((P2.1), (P2.2)) with fixed S as (P2') ((P2'.1), (P2'.2)) in the sequel.

its AN locally, i.e.,  $\mathbf{x}'_{r2} = [\sqrt{\sigma_1 s'_1}, \dots, \sqrt{\sigma_N s'_N}]^T$ , in which  $s'_i$ 's are i.i.d. AN beams, denoted by  $s'_i \sim C\mathcal{N}(0, 1)$ . This type of CJ is known to be uncoordinated with the covariance matrix given by  $\mathbf{S} = \text{diag}([\sigma_1, \dots, \sigma_N])$ . In this section, we assume that each relay consumes all of its remaining power from AF for AN, i.e.,  $\sigma_i = \eta \rho_i \alpha_i P_s |h_{sr_i}|^2$ ,  $\forall i \in \mathcal{N}$  (c.f. (5)). Hence, the AN design solely depends on  $\alpha_i$ 's and/or  $\rho_i$ 's.

### A. Distributed Algorithm for SPS

First, we propose a heuristic scheme for the *i*th AF relay to decide on  $\rho_i$ ,  $\forall i$ , which is given by

$$\rho_i = \delta \left( 1 - \frac{|h_{r_i d}|^2}{\max_{k \in \mathcal{K}} |h_{r_i e, k}|^2} \right)^+,\tag{41}$$

where  $\delta \in (0, 1)$  is a constant controlling the relay's level of jamming. For example, a larger  $\delta$  indicates that each relay prefers to splitting a larger portion of power for jamming and vice versa. The intuition behind (41) is that if the *i*th relay observes that  $|h_{r_id}|^2 \ge \max_{k\mathcal{K}} |h_{r_ie,k}|^2$ , which means that a nonnegative secrecy rate is achievable even if there is only itself in the system, it will shut down the AN; otherwise, it will split up to  $\delta$  portion of  $\rho_i$  for jamming. In an extreme case of  $|h_{r_id}|^2 \ll \max_{k\mathcal{K}} |h_{r_ie,k}|^2$ , probably when an Eve is located within the very proximity of this relay, it allocates the maximum permissible portion of power, i.e.,  $\delta$ , for AN.

Next, since an individual relay cannot evaluate the secrecy performance of the whole system,  $\measuredangle \beta_i$ 's are simply chosen to be the optimum for the multi-AF relaying w/o security considerations, i.e.,  $\measuredangle \beta_i = -\measuredangle h_{r_id} - \measuredangle h_{sr_i}, \forall i$ .

# B. Distributed Algorithm for DPS

Following the same designs for  $\rho_i$ 's and  $\measuredangle \beta_i$ 's in Section V-A, the remaining task for WEH-enabled relays operating with DPS is to set proper values for  $\alpha_i$ 's. We choose  $\alpha_i$ 's that maximize the "hypothetical SINR". This "hypothetical" SINR may not be the actual SINR for the destination, but just a criterion calculated based on the "hypothetical" received signal seen by the *i*th relay, given by

$$\tilde{y}_{d_i} = h_{r_i d} \beta_i \sqrt{1 - \alpha_i} \sqrt{P_s} h_{sr_i} s + h_{r_i d} \beta_i \sqrt{1 - \alpha_i} n_{a,i} + h_{r_i d} \beta_i n_{c,i} + h_{r_i d} \sqrt{\sigma_i} s'_i + n_d, \ \forall i.$$
(42)

The corresponding SINR is thus expressed as

$$\text{SINR}_{\tilde{y}_{d_i}} = \frac{\eta(1-\rho_i)P_s|h_{sr_i}|^2}{\eta\sigma_{n_a}^2 + \frac{\eta\sigma_{n_c}^2}{1-\alpha_i} + f(\gamma_i) + \eta\rho_i P_s|h_{sr_i}|^2},$$
 (43)

where

$$f(\gamma_i) = \frac{\gamma_i(P_s|h_{sr_i}|^2 + \sigma_{n_a}^2)}{\alpha_i} + \frac{\gamma_i\sigma_{n_c}^2}{\alpha_i(1 - \alpha_i)}$$
(44)

with  $\gamma_i = \frac{\sigma_{n_d}^2}{P_s |h_{sr_i}|^2 |h_{r_id}|^2}$ . Consequently, the maximization of (43) w.r.t.  $\alpha_i$ ,  $\forall i$ , is formulated as

(P2-distr.):  

$$\begin{cases}
\min_{\alpha_i} \frac{\eta \sigma_{n_c}^2}{1-\alpha_i} + \frac{\gamma_i(P_s|h_{sr_i}|^2 + \sigma_{n_a}^2)}{\alpha_i} + \frac{\gamma_i \sigma_{n_c}^2}{\alpha_i(1-\alpha_i)} \\
\text{s.t. } 0 \le \alpha_i \le 1.
\end{cases}$$

*Proposition 5.1:* The optimal  $\alpha_i$ ,  $\forall i$ , to (P2-distr.) is

$$\alpha_i^* = \frac{1}{1 + \sqrt{\frac{(\eta + \gamma_i)\sigma_{n_c}^2}{\gamma_i(P_s|h_{sr_i}|^2 + \sigma_{n_a}^2 + \sigma_{n_c}^2)}}}.$$
(45)

*Proof:* It is easy to verify that problem (P2-distr.) is convex and the minimum solution of its objective function derived from the first-order derivative happens to fall within the feasible region of  $\alpha_i$ , which is seen in (45).

With  $\rho_i$ 's,  $\measuredangle \beta_i$ 's and  $\alpha_i$ 's set, each AF relay is then able to decide its relay weight and AN transmission.

#### VI. NUMERICAL RESULTS

In this section we compare our proposed schemes operating with SPS or DPS with some benchmarks. In the centralized case, the optimal solution for SPS in Section IV-A is denoted by CJ-SPS, while Algorithm I in Section IV-B is denoted by CJ-DPS. The distributed schemes in Section V-A and Section V-B are referred to as Distributed-SPS and Distributed-DPS, respectively. To demonstrate the effectiveness of our AN-aided secure multi-AF relay beamforming algorithms, we also provide three benchmark schemes: NoCJ-SPS, NoCJ-DPS and Random PS.<sup>5</sup> For NoCJ-SPS, we solve problem (P1) by replacing S with 0. Similarly, for *NoCJ-DPS*, we initialize  $\overline{S} = 0$  and quit the loop in Algorithm I after the very first time of solving problem (P2'). *Random PS*, on the other hand, picks up i.i.d.  $\alpha_i$  and  $\rho_i$ uniformly generated over [0, 1], respectively, and co-phases  $\measuredangle \beta_i = -\measuredangle h_{sr_i} - \measuredangle h_{r_id}, \forall i.$ 

Consider that N WEH-enabled AF relays and K eavesdroppers (only existing outside from the "security zone") are uniformly located within a circular area of radius R. We also assume that the channel models consist of both large-scale path loss and small-scale multi-path fading. The unified path loss model is given by

$$L = A_0 \left(\frac{d}{d_0}\right)^{-\kappa},\tag{46}$$

where  $A_0 = 10^{-3}$ , *d* denotes the relevant distance,  $d_0 = 1$ m is a reference distance, and  $\kappa$  is the path loss exponent set to be 2.5.  $h_{sr_i}$ ,  $h_{r_id}$ , and  $h_{r_ie,k}$ ,  $\forall i \in \mathcal{N}$ ,  $\forall k \in \mathcal{K}$ , are generated from independent Rayleigh fading with zero mean and variance specified by (46).

The simulation parameters are set as follows unless otherwise specified: the radius defining the range is R = 5m; the transmit power at the source is  $P_s = 40$ dBm; the noise variances are set as  $\sigma_{n_a}^2 = -80$ dBm,  $\sigma_{n_c}^2 = -50$ dBm,  $\sigma_{n_d}^2 = \sigma_{n_a}^2 + \sigma_{n_c}^2$ , and  $\sigma_{n_e,k}^2 = \sigma_{n_d}^2$ ,  $\forall k$ ; the EH efficiency is set to be  $\eta = 50\%$ . Also, numerical results are averaged over 500 independent channel realizations.

# A. Secrecy Performance by Centralized Approach

Here, we evaluate the performance of the proposed centralized designs in Section IV. The efficiency of the alternating optimization that iteratively attains numerical solution to (P2)

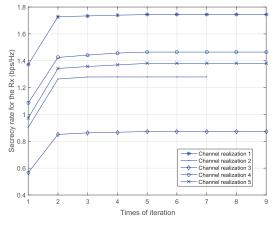
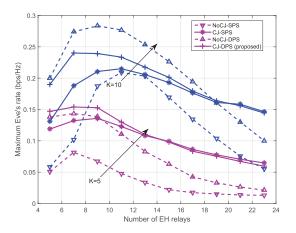


Fig. 3. The secrecy rate by *CJ-DPS* versus the number of iterations for the alternating optimization in Table I with  $P_s = 40$ dBm, N = 10, and K = 5.

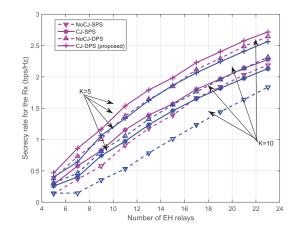
is studied in Fig. 3, which shows the increment of the achievable secrecy rate after each round of the iteration. The most rapid increase is observed after the first iteration, which illustrates that the optimization of the PS ratios,  $\alpha_i$ 's, accounts for the main factor for the secrecy rate performance gains over a SPS scheme that sets { $\alpha_i = 0.5$ }. It is seen that the alternating algorithm converges within the relative tolerance set to be  $10^{-3}$ , after an average of 5–6 iterations for several channel realizations, which appears reasonable in terms of complexity.

Fig. 4 shows the achievable secrecy rate for the legitimate Rx with the increase in the number of AF relays by different schemes. As we can see, the secure multi-AF relaying schemes assisted by the transmission of AN outperforms those w/o AN for both SPS and DPS. In addition, with the increase in N, the role of CJ gradually reduces for both schemes of SPS and DPS. This is because as N gets larger, the optimal designs tend to suppress the interception at the most capable eavesdropper more effectively with N DoF, enforcing the numerator of max SINR<sub>S.E.k</sub> to a relatively low level, which  $k \in \mathcal{K}$ can also be observed from max  $r_{S,E,k}$  in Fig.4(a), and therefore  $k \in \mathcal{K}$ the optimal amount of power allocated to AN beams inclines to be little; otherwise the jamming yielded will be detrimental to the reception at the legitimate Rx.

Fig. 5 shows the achievable secrecy rate for the legitimate Rx versus the number of eavesdroppers by different schemes. First, similar to the results shown in Fig. 4, the proposed AN-aided multi-AF relaying designs operating with DPS-enabled relays perform best among all the schemes. Secondly, as K goes up, the AN-aided schemes allow the secrecy rate to drop slowly, in other words, more robust against multiple eavesdroppers, while the secrecy rate of their NoCJ counterparts almost goes down linearly with K. Furthermore, with K increasing, for example, more than 10, the increase in the number of relays, from N = 10 to 20, cannot replace the role of CJ as shown in Fig. 4 and 5, since in the presence of many eavesdroppers, more relays may also result in improved eavesdroppers' decoding ability w/o the assistance of CJ. It is also noteworthy that with K = 1, there is little use of CJ by the centralized schemes, which was also observed in [32].



(a) max  $r_{S,E,k}$  versus the number of AF relays.



(b) The achievable secrecy rate versus the number of AF relays.

Fig. 4. Comparison of different schemes with  $P_s = 10$ dB for K = 5.

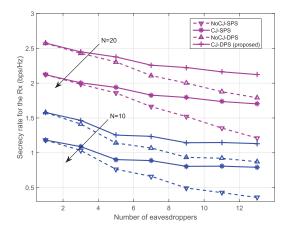


Fig. 5. The secrecy rate versus the number of eavesdroppers with  $P_s = 10$ dB for N = 10 and N = 20, respectively.

Fig. 6 provides simulation results of different schemes by varying the source transmit power. It is seen that with more power available at the source, the advantage of CJ is more pronounced, since given other variables fixed, larger  $P_s$  indicates larger feasible regions for (P1) and (P2). Furthermore, as similarly seen in Fig. 4, with a mild number of eavesdroppers (K = 5), subject to the same  $P_s$ , a large number of cooperative

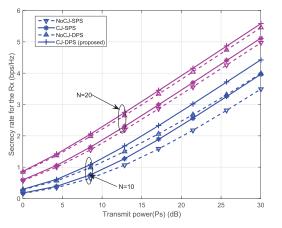


Fig. 6. The secrecy rate versus the transmit power with K = 5 for N = 10 and N = 20, respectively.

relays enables more DoF in designing the optimal  $\alpha_i$ 's and  $\measuredangle \beta_i$ 's, which alleviates the dependence on AN beams to combat Eves.

It is worthy of noting that there are two other well-known suboptimal centralized schemes in the literature, namely, "nulling out the AN at the desired destination [10]", and "nulling out the confidential message at the Eves [8]", denoted by ZF-D-SPS/DPS and ZF-Eves-SPS/DPS, respectively, in the sequel. These two schemes are in general acknowledged to have reasonable performance with less computational complexity. However, since in this paper we mainly focus on the effectiveness of joint wireless powered CJ and AF relaying on wiretap channels, we preclude them from the numerical results to present, but include herein a brief summary of our comparison studies between the optimal/proposed schemes and the suboptimal ones abovementioned. We conclude from simulation results that ZF-D-SPS/DPS schemes achieve the optimal/proposed solutions with negligible gap, while ZF-Eves-SPS/DPS schemes are overwhelmingly outperformed by all the other schemes, especially when there are a mild to large number of eavesdroppers in the presence. This is expectable, as the more the eavesdroppers are, the harder the equivalent channels between the Tx and the eavesdroppers lie in the orthogonal space of the beamforming direction. Moreover, ZF-D-SPS/DPS schemes only reduce the dimension of the optimization variables (S) by 1, while ZF-Eves-SPS/DPS schemes drastically reduce the complexity, because both S = 0and  $\tau = 1$  do not need to be optimized.

## B. Secrecy Performance by Distributed Algorithms

Here, we study the performance of the distributed schemes, namely, *Distributed-SPS* and *Distributed-DPS* in Section V. As mentioned earlier, these heuristics are provided as benchmarks to demonstrate what can be done under the extreme "no-coordination" circumstance, in comparison with *Random PS*. Note that any other distributed schemes with certain level of cooperation among relays are supposed to increase the secrecy performance up to the proposed centralized algorithms, namely, *CJ-DPS* and *CJ-SPS*, at the expense of extra computational complexity and system overhead.  $\delta$  is set to be 0.5.

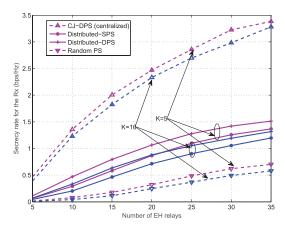


Fig. 7. The secrecy rate versus the number of AF relays by distributed algorithms with  $P_s = 10$ dB.

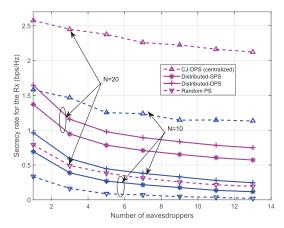


Fig. 8. The secrecy rate versus the number of eavesdroppers by distributed algorithms with  $P_s = 10$ dB.

Fig. 7 provides the results for the achievable secrecy rate of various schemes versus the number of relays. *Distributed-SPS* and *Distributed-DPS*, are observed to be outperformed by their centralized counterparts though, they are considerably superior to *Random PS*. It is also seen that the performance gap between the centralized and distributed approaches is enlarged as N increases, which is expected, since larger N yields more DoF for cooperation that is exclusively beneficial for the centralized schemes. Furthermore, compared with the centralized schemes, the distributed ones are more vulnerable to the increase in the eavesdroppers' number.

In Fig. 8, we investigate the relationship between the secrecy rate performance and the number of eavesdroppers by different methods. As can be observed, compared with the centralized schemes, the secrecy rates achieved by *Distributed-SPS* and *Distributed-DPS* both reduce more drastically with the increase in *K* due to the lack of effective cooperation. Also, the advantage of DPS over SPS for the distributed schemes is compromised since  $\alpha_i$ 's are not jointly designed with other parameters. At last, a similar observation has been made as that for Fig. 7, that is, larger *N* yields more visible performance gap between the centralized and distributed approaches.

In Fig. 9, we examine the effect of increasing the transmit power at the source on the secrecy performance of different schemes under the same settings as those in Fig. 6. Among all the presented designs, *CJ-DPS* still achieves the best secrecy

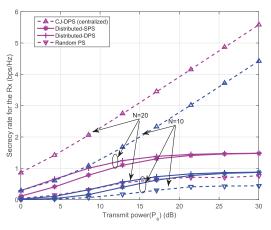


Fig. 9. The secrecy rate versus transmit power by distributed algorithms with K = 5.

rate as observed in other examples. Also, the fact that larger N benefits more from cooperative designs is corroborated again due to the same reason as that for Fig. 7 and 8. Furthermore, the secrecy rate of *Distributed-SPS* or *Distributed-DPS* is quickly saturated when  $P_s > 20$ dB while that for their centralized counterparts still rises at fast speed.

## VII. CONCLUSION

This paper studied secure communications using multiple single-antenna WEH-enabled AF relays assisted by AN via CJ for a SWIPT network with multiple single-antenna eavesdroppers. Using PS at the relays, the achievable secrecy rates for the relay wiretap channel were maximized by jointly optimizing the CB and the CJ covariance matrix along with the PS ratios for relays operating with, respectively, SPS and DPS. For DPS, Reformulating the constraints into restricted hyperbolic forms enabled us to develop convex optimization-based solutions. Further, we proposed an information-exchange-free distributed algorithm that outperforms the random decision.

# APPENDIX PROOF OF PROPOSITION 3

The Lagrangian of problem (P1.1-SDP) is given by (47), as shown at the bottom of the next page, where  $\chi$  denotes a tuple consisting of all the primal and dual variables. Specifically,  $Y_1$ ,  $Y_2$  and  $\lambda$  are Lagrangian multipliers associated with  $\hat{X}_1$ ,  $\hat{S}$  and the first constraint of (P1.1-SDP), respectively;  $\{\theta_k\}$  are the dual variables associated with the SINR constraint for the *k*th Eve, respectively;  $U = \text{diag}([u_i]_{i=1}^N)$  with each diagonal entry  $u_i$  denoting the dual variable associated with the per-relay power constraint;  $\zeta$  is the Lagrangian multiplier associated with  $\xi \ge 0$ . In addition,  $W_0 = \text{diag}([\eta \bar{\alpha}_i P_s |h_{sr_i}|^2]_{i=1}^N)$ . The Karush-Kuhn-Tucker (KKT) conditions for (47) are listed as follows:

$$\boldsymbol{Y}_{1} = -P_{s}\tilde{\boldsymbol{h}}_{sd}^{\dagger}\tilde{\boldsymbol{h}}_{sd}^{T} + \lambda \boldsymbol{D}_{sd} - \sum_{k=1}^{K} \theta_{k} \left(\frac{1}{\tau} - 1\right) \boldsymbol{D}_{se,k} + \sum_{k=1}^{K} \theta_{k} P_{s}\tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^{T} + \boldsymbol{W}_{0}^{\frac{1}{2}} \boldsymbol{U} \boldsymbol{W}_{0}^{\frac{1}{2}}, \qquad (48a)$$

$$Y_{2} = \lambda \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T} - \sum_{k=1}^{K} \theta_{k} \left(\frac{1}{\tau} - 1\right) \boldsymbol{h}_{re,k}^{\dagger} \boldsymbol{h}_{re,k}^{T} + \boldsymbol{U}, \quad (48b)$$
  
$$\zeta = \lambda \sigma_{n_{d}}^{2} - \sum_{k=1}^{K} \theta_{k} \left(\frac{1}{\tau} - 1\right) \sigma_{n_{e},k}^{2} - \operatorname{trace}(\boldsymbol{W}_{0}^{\frac{1}{2}} \boldsymbol{U} \boldsymbol{W}_{0}^{\frac{1}{2}}), \quad (48c)$$

$$\boldsymbol{Y}_1 \hat{\boldsymbol{X}}_1^* = \boldsymbol{0}, \tag{48d}$$

$$\boldsymbol{Y}_2 \hat{\boldsymbol{S}}^* = \boldsymbol{0}. \tag{48e}$$

Pre- and post-multiplying  $W_0^{\frac{1}{2}}$  with the left hand side (LHS) and right hand side (RHS) of (48b), respectively, and substituting  $W_0^{\frac{1}{2}}U^*W_0^{\frac{1}{2}}$  into (48a),  $Y_1^*$  can be rewritten as

$$Y_{1} = -P_{s}\tilde{\boldsymbol{h}}_{sd}^{\dagger}\tilde{\boldsymbol{h}}_{sd}^{T} + \lambda \boldsymbol{D}_{sd} - \sum_{k=1}^{K} \theta_{k} \left(\frac{1}{\tau} - 1\right) \boldsymbol{D}_{se,k}$$
$$-\lambda \boldsymbol{W}_{0}^{\frac{1}{2}}\boldsymbol{h}_{rd}^{\dagger}\boldsymbol{h}_{rd}^{T}\boldsymbol{W}_{0}^{\frac{1}{2}} + \sum_{k=1}^{K} \theta_{k} P_{s}\tilde{\boldsymbol{h}}_{se,k}^{\dagger}\tilde{\boldsymbol{h}}_{se,k}^{T}$$
$$+ \boldsymbol{W}_{0}^{\frac{1}{2}}Y_{2}\boldsymbol{W}_{0}^{\frac{1}{2}} + \sum_{k=1}^{K} \theta_{k} \left(\frac{1}{\tau} - 1\right) \boldsymbol{W}_{0}^{\frac{1}{2}}\boldsymbol{h}_{re,k}^{\dagger}\boldsymbol{h}_{re,k}^{T}\boldsymbol{W}_{0}^{\frac{1}{2}}.$$
(49)

Introducing the notation of  $[\cdot]_{offd}$  to represent a square matrix with its diagonal entries removed, it follows from (48b) that

$$\begin{bmatrix} W_0^{\frac{1}{2}} Y_2 W_0^{\frac{1}{2}} - \lambda W_0^{\frac{1}{2}} \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^T W_0^{\frac{1}{2}} \\ + \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) W_0^{\frac{1}{2}} \boldsymbol{h}_{re,k}^{\dagger} \boldsymbol{h}_{re,k}^T W_0^{\frac{1}{2}} \end{bmatrix}_{\text{offd}} = \boldsymbol{0}. \quad (50)$$

By subtracting (50) from (49),  $Y_1$  can be rewritten as

$$Y_{1} = -P_{s}\tilde{\boldsymbol{h}}_{sd}^{\dagger}\tilde{\boldsymbol{h}}_{sd}^{T} + \lambda \boldsymbol{D}_{\hat{sd}} - \sum_{k=1}^{K} \theta_{k} \left(\frac{1}{\tau} - 1\right) \boldsymbol{D}_{\hat{se},k}$$
$$- \left[\lambda \boldsymbol{W}_{0}^{\frac{1}{2}}\boldsymbol{h}_{rd}^{\dagger}\boldsymbol{h}_{rd}^{T}\boldsymbol{W}_{0}^{\frac{1}{2}}\right]_{d} + \sum_{k=1}^{K} \theta_{k} P_{s}\tilde{\boldsymbol{h}}_{se,k}^{\dagger}\tilde{\boldsymbol{h}}_{se,k}^{T}$$
$$+ \left[\boldsymbol{W}_{0}^{\frac{1}{2}}\boldsymbol{Y}_{2}\boldsymbol{W}_{0}^{\frac{1}{2}}\right]_{d} + \left[\sum_{k=1}^{K} \theta_{k} \left(\frac{1}{\tau} - 1\right) \boldsymbol{W}_{0}^{\frac{1}{2}}\boldsymbol{h}_{re,k}^{\dagger}\boldsymbol{h}_{re,k}^{T}\boldsymbol{W}_{0}^{\frac{1}{2}}\right]_{d},$$
(51)

where  $[\cdot]_d$  denotes a square matrix with only the diagonal remained. Observing that

$$(\boldsymbol{D}_{\hat{sd}})^{-1}\boldsymbol{D}_{\hat{se},k} = \left[\boldsymbol{W}_{0}^{\frac{1}{2}}\boldsymbol{h}_{rd}^{\dagger}\boldsymbol{h}_{rd}^{T}\boldsymbol{W}_{0}^{\frac{1}{2}}\right]_{d}^{-1} \left[\boldsymbol{W}_{0}^{\frac{1}{2}}\boldsymbol{h}_{re,k}^{\dagger}\boldsymbol{h}_{re,k}^{T}\boldsymbol{W}_{0}^{\frac{1}{2}}\right]_{d}$$
$$= \operatorname{diag}\left([|\boldsymbol{h}_{rie,k}|^{2} / |\boldsymbol{h}_{rid}|^{2}]_{i=1}^{N}\right) \equiv \boldsymbol{R}_{ed,k}.$$
(52)

As a result,  $Y_1^*$  can be finally recast as

$$\boldsymbol{Y}_{1}^{*} = -P_{s}\tilde{\boldsymbol{h}}_{sd}^{\dagger}\tilde{\boldsymbol{h}}_{sd}^{T} + \boldsymbol{\Xi} + \sum_{k=1}^{K}\theta_{k}P_{s}\tilde{\boldsymbol{h}}_{se,k}^{\dagger}\tilde{\boldsymbol{h}}_{se,k}^{T}, \qquad (53)$$

where

$$\Xi = \left[ \boldsymbol{W}_{0}^{\frac{1}{2}} \boldsymbol{Y}_{2} \boldsymbol{W}_{0}^{\frac{1}{2}} \right]_{d} - \left( \left[ \boldsymbol{W}_{0}^{\frac{1}{2}} \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T} \boldsymbol{W}_{0}^{\frac{1}{2}} \right]_{d} - \boldsymbol{D}_{\hat{sd}} \right) \\ \times \left( \lambda \boldsymbol{I} - \sum_{k=1}^{K} \theta_{k} \left( \frac{1}{\tau} - 1 \right) \boldsymbol{R}_{ed,k} \right).$$
(54)

In the following, we show that  $\Xi + \sum_{k=1}^{K} \theta_k P_s \tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^{T}$  is a positive definite matrix. Note that since  $\Xi$  is a diagonal matrix, its definiteness is only determined by the signs of its diagonal entries, for which we commence with the discussion in three difference cases below.

- 1) Case I:  $\exists i$  such that  $\lambda \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} 1\right) [\boldsymbol{R}_{ed,k}]_{i,i} < 0.$ Since  $\left[ \left[ \boldsymbol{W}_0^{\frac{1}{2}} \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T} \boldsymbol{W}_0^{\frac{1}{2}} \right]_d - \boldsymbol{D}_{\hat{sd}} \right]_{i,i}$   $= \eta \bar{\alpha}_i P_s |h_{sr_i}|^2 |h_{r_id}|^2 \left( 1 - \frac{(1 - \bar{\alpha}_i)\sigma_{n_a}^2 + \sigma_{n_c}^2}{(1 - \bar{\alpha}_i)(|h_{sr_i}|^2 P_s + \sigma_{n_a}^2) + \sigma_{n_c}^2} \right) > 0,$  it follows from (54) that  $[\boldsymbol{\Xi}]_{i,i} > 0$  in this case. 2) Case II:  $\exists i$  such that  $\lambda - \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) [\boldsymbol{R}_{ed,k}]_{i,i} > 0.$ In accordance with (48b), we have  $\left[ \left[ \boldsymbol{W}_0^{\frac{1}{2}} \boldsymbol{Y}_2 \boldsymbol{W}_0^{\frac{1}{2}} \right]_{d} \right]_{i,i} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{i,k} - \frac{1}{2} \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) \left[ \boldsymbol{R}_{ed,k} \right]_{$
- 2) **Case II:**  $\exists i$  such that  $\lambda \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} 1\right) [\mathbf{R}_{ed,k}]_{i,i} > 0.$ In accordance with (48b), we have  $\left[ \left[ \mathbf{W}_0^{\frac{1}{2}} \mathbf{Y}_2 \mathbf{W}_0^{\frac{1}{2}} \right]_{\mathbf{d}} \right]_{i,i} - [\mathbf{W}_0]_{i,i} |h_{r_id}|^2 (\lambda^* - \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) [\mathbf{R}_{ed,k}]_{i,i}) \ge 0,$ which implies that  $[\mathbf{\Xi}]_{i,i} = \left[ \left[ \mathbf{W}_0^{\frac{1}{2}} \mathbf{Y}_2 \mathbf{W}_0^{\frac{1}{2}} \right]_{\mathbf{d}} \right]_{i,i} - [\mathbf{W}_0]_{i,i} |h_{r_id}|^2 (\lambda - \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) [\mathbf{R}_{ed,k}]_{i,i}) + [\mathbf{D}_{\hat{s}\hat{d}}]_{i,i} (\lambda - \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) [\mathbf{R}_{ed,k}]_{i,i}) + [\mathbf{R}_{ed,k}]_{i,i}) > 0$  (c.f. (54)).
- 3) Case III:  $\exists i$  such that  $\lambda \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} 1\right)$   $[\mathbf{R}_{ed,k}]_{i,i} = 0$ . In this case, it follows that  $[\mathbf{\Xi}]_{i,i} = \begin{bmatrix} \mathbf{W}_0^{\frac{1}{2}} \mathbf{Y}_2 \mathbf{W}_0^{\frac{1}{2}} \end{bmatrix}_{i,i} \geq 0$ . It is noteworthy that the number of *i*'s such that  $\lambda - \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) [\mathbf{R}_{ed,k}]_{i,i} = 0$  cannot exceed one. This can be proved by contradiction as follows. If  $\exists i_1, i_2, i_1 \neq i_2$ , such that  $\lambda - \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) [\mathbf{R}_{ed,k}]_{i,i} = 0$  and  $\lambda - \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) [\mathbf{R}_{ed,k}]_{i_1,i_1} = 0$  and  $\lambda - \sum_{k=1}^{K} \theta_k \left(\frac{1}{\tau} - 1\right) [\mathbf{R}_{ed,k}]_{i_2,i_2} = 0$ , it implies that  $\sum_{k=1}^{K} \theta_k$  $[\mathbf{R}_{ed,k}]_{i_1,i_1} = \sum_{k=1}^{K} \theta_k [\mathbf{R}_{ed,k}]_{i_2,i_2}$ , which contradicts

 $[\mathbf{K}_{ed,k}]_{i_1,i_1} = \sum_{k=1}^{k} 0_k [\mathbf{K}_{ed,k}]_{i_2,i_2}$ , which contradicts to the fact that for any two independent continuously distributed random variables, the chance that they are equal is zero.

In summary,  $[\Xi]_{i,i} \ge 0$ ,  $\forall i$ . If  $[\Xi]_{i,i} > 0$ , then it is obvious that  $\Xi + \sum_{k=1}^{K} \theta_k P_s \tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^T > \boldsymbol{0}$ . Next, we show that it still holds true in the case that  $\exists i'$ , such that  $[\Xi]_{i',i'} = 0$ ,  $i' \in \mathcal{N}$ , by definition. Define the null-space of  $\Xi$  by  $\psi = \{\eta | \eta = \alpha e_{i'}, \alpha \in \mathbb{C}\} \text{ and multiply } \eta^{H} \text{ and } \eta, \forall \eta \neq \mathbf{0}, \text{ on the LHS and RHS of } \Xi + \sum_{k=1}^{K} \theta_{k} P_{s} \tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^{T}, \text{ respectively. If } \eta \notin \psi, \text{ it is straightforward to obtain } \eta^{H} (\Xi + \sum_{k=1}^{K} \theta_{k} P_{s} \tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^{T}) \eta > 0; \text{ otherwise, it follows that } \eta^{H} (\Xi + \sum_{k=1}^{K} \theta_{k} P_{s} \tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^{T}) \eta = \sum_{k=1}^{K} \theta_{k} P_{s} \alpha^{2} |[\tilde{\boldsymbol{h}}_{se,k}]_{i'}|^{2} > 0, \text{ as } [\tilde{\boldsymbol{h}}_{se,k}]_{i'} \neq 0 \text{ in probability. This completes the proof.}$ 

Finally, multiplying both sides of (53) by  $\hat{X}_{1}^{*}$ , as per (48d), we obtain the following equation:

$$\hat{\boldsymbol{X}}_{1}^{*} = P_{s} \left( \boldsymbol{\Xi} + \sum_{k=1}^{K} \theta_{k} P_{s} \tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^{T} \right)^{-1} \tilde{\boldsymbol{h}}_{sd}^{\dagger} \tilde{\boldsymbol{h}}_{sd}^{T} \hat{\boldsymbol{X}}_{1}^{*}, \quad (55)$$

which further implies that  $\operatorname{rank}(\hat{X}_1^*) \leq \operatorname{rank}(\tilde{h}_{sd}^* \tilde{h}_{sd}^T) = 1$ . In addition, since the optimality of (P1.1-SDP) suggests that  $\hat{X}_1^* \neq \mathbf{0}$ ,  $\operatorname{rank}(\hat{X}_1^*) = 1$  is thus proved.

As  $\hat{X}_1^*$  can be decomposed as  $\hat{w}_1^* \hat{w}_1^{*H}$  by EVD, (48d) results in  $Y_1 \hat{w}_1^* = 0$ , which further implies that

$$\hat{\boldsymbol{w}}_{1}^{*} = P_{s} \left( \boldsymbol{\Xi} + \sum_{k=1}^{K} \theta_{k} P_{s} \tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^{T} \right)^{-1} \tilde{\boldsymbol{h}}_{sd}^{\dagger} \tilde{\boldsymbol{h}}_{sd}^{T} \hat{\boldsymbol{w}}_{1}^{*}.$$
(56)

Therefore, (56) admits a unique solution  $\hat{w}_1$  up to a scaling factor, which is given by

$$\hat{\boldsymbol{w}}_{1} = \left(\boldsymbol{\Xi} + \sum_{k=1}^{K} \theta_{k} P_{s} \tilde{\boldsymbol{h}}_{se,k}^{\dagger} \tilde{\boldsymbol{h}}_{se,k}^{T} \right)^{-1} \tilde{\boldsymbol{h}}_{sd}^{\dagger}.$$
 (57)

Consequently, we have  $\hat{\boldsymbol{w}}_{1}^{*} = \beta \hat{\boldsymbol{w}}_{1}$ , where  $\beta \in \mathbb{R}_{+}$ . On the other hand, by plugging  $\hat{\boldsymbol{w}}_{1}^{*} = \beta \hat{\boldsymbol{w}}_{1}$  into the equality constraint of (P1.1-SDP), we have  $\beta = \sqrt{\frac{\tau - \zeta^{*} \sigma_{n_{d}}^{2} - \operatorname{trace}(\hat{\boldsymbol{S}}^{*} \boldsymbol{h}_{rd}^{+} \boldsymbol{h}_{rd}^{T})}{\operatorname{trace}(\hat{\boldsymbol{w}}_{1} \hat{\boldsymbol{w}}_{1}^{H} \boldsymbol{D}_{s\hat{d}})}$ , which yields

$$\hat{\boldsymbol{w}}_{1}^{*} = \sqrt{\frac{\tau - \xi^{*} \sigma_{n_{d}}^{2} - \operatorname{trace}(\hat{\boldsymbol{S}}^{*} \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T})}{\operatorname{trace}(\hat{\boldsymbol{w}}_{1} \hat{\boldsymbol{w}}_{1}^{H} \boldsymbol{D}_{\hat{sd}})}} \hat{\boldsymbol{w}}_{1}.$$
(58)

At last, we show 3) of Proposition 4.1. For the case of  $K \ge N$ , it is obvious that  $\operatorname{rank}(\hat{S})^* \le N$ . For the case of K < N, only a sketch of the proof is provided here due to the length constraint. According to (48b), first it is provable that  $\lambda \boldsymbol{h}_{rd}^{\dagger} \boldsymbol{h}_{rd}^{T} + \boldsymbol{U}$  is a full-rank matrix when (P1.1-SDP) obtains its optimum value; next, observing that  $\operatorname{rank}(Y_2) \ge N - \operatorname{rank}(\sum_{k=1}^{K} \theta_k \boldsymbol{h}_{re,k}^{\dagger} \boldsymbol{h}_{re,k})$ , it follows that  $\operatorname{rank}(Y_2) \ge N - K$  as a result of  $\operatorname{rank}(\sum_{k=1}^{K} \theta_k \boldsymbol{h}_{re,k}^{\dagger}) \le K$ ; then according to (48e),  $\operatorname{rank}(\hat{S}^*) \le K$  is thus obtained.

$$\mathcal{L}(\chi) = \operatorname{trace}\left(\left(P_{s}\tilde{\boldsymbol{h}}_{sd}^{\dagger}\tilde{\boldsymbol{h}}_{sd}^{T} - \lambda \boldsymbol{D}_{sd} + \sum_{k=1}^{K}\theta_{k}\left(\frac{1}{\tau} - 1\right)\boldsymbol{D}_{se,k} - \sum_{k=1}^{K}\theta_{k}P_{s}\tilde{\boldsymbol{h}}_{se,k}^{\dagger}\tilde{\boldsymbol{h}}_{se,k}^{T} - \boldsymbol{W}_{0}^{\frac{1}{2}}\boldsymbol{U}\boldsymbol{W}_{0}^{\frac{1}{2}} + \boldsymbol{Y}_{1}\right)\hat{\boldsymbol{X}}_{1}\right) + \lambda\tau + \operatorname{trace}\left(\left(-\lambda\boldsymbol{h}_{rd}^{\dagger}\boldsymbol{h}_{rd}^{T} + \sum_{k=1}^{K}\theta_{k}\left(\frac{1}{\tau} - 1\right)\boldsymbol{h}_{re,k}^{\dagger}\boldsymbol{h}_{re,k}^{T} - \boldsymbol{U} + \boldsymbol{Y}_{2}\right)\hat{\boldsymbol{S}}\right) + \left(-\lambda\sigma_{n_{d}}^{2} + \sum_{k=1}^{K}\theta_{k}\left(\frac{1}{\tau} - 1\right)\sigma_{n_{e},k}^{2} + \operatorname{trace}\left(\boldsymbol{W}_{0}^{\frac{1}{2}}\boldsymbol{U}\boldsymbol{W}_{0}^{\frac{1}{2}}\right) + \zeta\right)\boldsymbol{\zeta}$$

$$(47)$$

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