# The concerted impact of galaxies and QSOs on the ionization and thermal state of the intergalactic medium

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# ABSTRACT

We present a detailed analysis of the ionization and thermal structure of the intergalactic medium (IGM) around a high-redshift (z = 10) QSO, using a large suite of cosmological, multifrequency radiative transfer simulations, exploring the contribution from galaxies as well as the QSO, and the effect of X-rays and secondary ionization. We show that in high-z QSO environments both the central QSO and the surrounding galaxies concertedly control the reionization morphology of hydrogen and helium and have a non-linear impact on the thermal structure of the IGM. A QSO imprints a distinctive morphology on HII regions if its total ionizing photon budget exceeds that of the surrounding galaxies since the onset of hydrogen reionization; otherwise, the morphology shows little difference from that of H II regions produced only by galaxies. In addition, the spectral shape of the collective radiation field from galaxies and QSOs controls the thickness of the I-fronts. While a UV-obscured QSO can broaden the I-front, the contribution from other UV sources, either galaxies or unobscured OSOs, is sufficient to maintain a sharp I-front. X-ray photons from the OSO are responsible for a prominent extended tail of partial ionization ahead of the I-front. QSOs leave a unique imprint on the morphology of He II/He III regions. We suggest that, while the physical state of the IGM is modified by QSOs, the most direct test to understand the role of galaxies and QSOs during reionization is to perform galaxy surveys in a region of sky imaged by 21 cm tomography.

**Key words:** radiative transfer – methods: numerical – intergalactic medium – dark ages, reionization, first stars.

### **1 INTRODUCTION**

In the current paradigm of extragalactic astronomy, the Universe has undergone two major reionization epochs. H I and He I reionization are thought to occur at  $z \sim 6-20$ , driven by early star-forming galaxies and/or quasars (QSOs; e.g. Madau & Haardt 2015; Robertson et al. 2015). This first reionization epoch contains information about the formation of the first luminous objects in the Universe, a period called cosmic dawn. The second reionization epoch, from He II to He III, occurs later time, at  $z \sim 2-4$ , and it is likely driven by the high QSO activity near the peak of cosmic star formation history. Understanding the full reionization process of intergalactic hydrogen and helium will provide a milestone in investigating the

nature of high-redshift galaxies and QSOs and of their interaction with the intergalactic medium (IGM).

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Current observations of the H I Ly  $\alpha$  Gunn–Peterson trough suggest that hydrogen reionization is largely completed by  $z \sim 6$  (e.g. Fan et al. 2006). However, the nature of the sources that drive hydrogen reionization is still unknown. A concordance picture is one in which (undetected) faint star-forming galaxies with an escape fraction of ionizing photons as large as ~20 per cent are the main reionizing agents (e.g. Robertson et al. 2015). At lower redshift, observations of the He II Ly  $\alpha$  Gunn–Peterson trough suggest that He II reionization is mostly completed by  $z \sim 2.5$  (Syphers et al. 2011; Worseck et al. 2011). Unlike H I reionization, He II reionization is likely driven by the already detected population of QSOs (Gialongo et al. 2015). In fact, simulations calibrated with the observed QSO luminosity function can grossly reproduce the observed properties of the He II Ly  $\alpha$  forest (McQuinn et al. 2009; Compostella, Cantalupo & Porciani 2013, 2014).

As hydrogen and helium reionization have a strong impact on the thermal state of the IGM (Lai et al. 2006; McQuinn et al. 2011; Greig, Bolton & Wyithe 2015), constraints on the reionization process can be obtained by measurements of the IGM temperature. Such measurements from the Ly  $\alpha$  forest (McQuinn et al. 2011; Lidz & Malloy 2014) suggest that the end of H I reionization should be at a redshift lower than  $z \simeq 9$  (Theuns et al. 2002; Bolton et al. 2010; Raskutti et al. 2012), while He II reionization should be extended over  $2 \le z \le 4.8$  (Becker et al. 2011). Furthermore, the IGM temperature in QSO near zones at  $z \sim 6$  suggests that the onset of He II reionization may be as early as the formation of the first QSOs at z > 6 (Bolton et al. 2012).

Although many authors have studied the impact of QSOs on the ionization and thermal state of the IGM, the role of QSOs during H I reionization at z > 6 still remains unclear. While it has been argued that QSOs alone cannot be responsible for hydrogen reionization based on constraints from the unresolved X-ray background (Dijkstra, Haiman & Loeb 2004; Salvaterra, Haardt & Ferrara 2005; Salvaterra, Haardt & Volonteri 2007; Haardt & Salvaterra 2015) and the decreasing number density of high-*z* QSOs (Meiksin 2005), recent re-investigations suggest a possible important contribution (e.g. Glikman et al. 2011; Fontanot, Cristiani & Vanzella 2012; Giallongo et al. 2015; Madau & Haardt 2015).

Furthermore, theoretical predictions about how the QSOs impact on the ionization and thermal state of the local environment do not always agree. For example, there seems to be no consensus about whether a QSO imprints a distinctive ionization and thermal structure on the IGM by producing a very large ionized region (e.g. Zaroubi et al. 2007; Thomas & Zaroubi 2008; Feng et al. 2013), if it can be distinguished from one produced only by galaxies (Alvarez & Abel 2007; Lidz et al. 2007; Datta, Friedrich & Mellema 2012), if the spectra of galaxies and QSOs induce a different shape of the ionization front (I-front; Zaroubi & Silk 2005; Kramer & Haiman 2008), or whether the sphericity of an ionized region may serve as discriminator of the type of source that created it (Datta et al. 2012). These theoretical discrepancies must be resolved to interpret QSO absorption spectra and upcoming 21 cm observations. In other words, a correct theoretical understanding is vital to place constraints on the role of galaxies and QSOs in driving reionization.

Understanding the impact of ionization from galaxies and/or QSOs on the physical state of the IGM relies on an accurate modelling of the effects of (i) the spectral shape of QSOs and galaxies [i.e. multifrequency radiative transfer (RT)], (ii) galaxies surrounding a QSO (i.e. cosmological *N*-body/hydrodynamical simulations), (iii) an anisotropic propagation of the I-front (i.e. 3D simulation), and (iv) a coherent treatment of both UV and X-ray photons as well as secondary ionization (i.e. UV/X-ray physics). Previous works addressed the above aspects separately. For example, the 1D RT simulations by Thomas & Zaroubi (2008) and Kramer & Haiman (2008) focused on (i) and (iv), whereas the 3D RT simulation by Datta et al. (2012) including both galaxies and QSOs, but no thermal structure, focused on addressing (i), (ii) and (iii).<sup>1</sup> At the time of writing, no RT calculation addressing all four points in a single simulation is reported.

In this work, we therefore investigate the ionization state of both hydrogen and helium, and the thermal state of the IGM in the environment of a high-*z* QSO by performing a suite of multidimensional, multifrequency RT simulations post-processing a cosmological hydrodynamical simulation. This is to our knowledge the most detailed calculation of this kind to date. This work distinguishes itself from previous investigations, as we present the case-by-case analysis of hydrogen and helium reionization, as well as the thermal state of the environment of a QSO at z = 10, including the effect of surrounding galaxies, X-ray and secondary ionization. This large suite of RT simulations aims at providing insights into the underlying physical mechanisms responsible for controlling the physical state of the IGM around QSOs, and on how all processes collectively shape it. Our work is an important first step towards full cosmological reionization simulations including both galaxies and multiple QSOs.

The paper is organized as follows. First, we describe the simulation set-up in Section 2. In Section 3, we present the results of hydrogen and helium reionization. In Section 4, we discuss the thermal state in the QSO environment. We compare our results with previous works in Section 5. Observational implications are briefly discussed in Section 6. Conclusions are then presented in Section 7.

### **2 SIMULATIONS**

In the following, we will describe the simulations employed in this paper. Hereafter, we assume cosmological parameters:  $\Omega_{\Lambda} = 0.74$ ,  $\Omega_{\rm m} = 0.26$ ,  $\Omega_{\rm b} = 0.0463$ , h = 0.72,  $n_{\rm s} = 0.95$  and  $\sigma_8 = 0.85$ , which is consistent with the *Wilkinson Microwave Anisotropy Probe* 9 result (Hinshaw et al. 2013).

#### 2.1 Hydrodynamical simulations

We have used hydrodynamical simulations of the IGM with the smoothed particle hydrodynamics code GADGET-3, which is an updated version of the publicly available code GADGET-2 (Springel 2005). The size of the simulation box is  $(50 h^{-1} \text{ cMpc})^3$ , with  $2 \times 512^3$  dark matter and gas particles, corresponding to a mass of  $5.53 \times 10^7$  and  $1.20 \times 10^7 h^{-1} M_{\odot}$ , respectively. The simulation is by design centred on the most massive halo (with mass  $1.34 \times 10^{10} h^{-1} M_{\odot}$ ) at z = 10. Haloes are identified using the friends-of-friends algorithm with a linking length of 0.2 times the mean inter-particle separation. All haloes are considered to harbour one galaxy with the empirically motivated prescription described in Section 2.3, which results in 7534 galaxies at z = 10. The lowest halo mass at this redshift is  $3.9 \times 10^8 h^{-1} M_{\odot}$ .

As a UV background is turned in the hydrodynamical simulation only at z = 9, the snapshots used in our analysis do not include this heating component. We re-compute the temperature using the RT code. As a reference, the mean (median) gas temperature at z = 10 before RT calculations is 100 K (25 K). Star formation is included using a simplified prescription that converts all gas particles with overdensity  $\rho/\langle \rho \rangle > 10^3$  and temperature  $T < 10^5$  K into collisionless 'star' particles. Note that because of this simple treatment our simulation does not self-consistently model star formation and feedback. Instead, we scale the halo masses in the hydrodynamical simulation to populate the ionizing sources in the RT simulations.

The gas density and temperature are mapped on to Cartesian grids with 256<sup>3</sup> cells; in total, 11 snapshots are present in the redshift range z = 15-10, with a  $\Delta z = 0.5$  interval. These are used as input for the RT code CRASH (see Section 2.2).

<sup>&</sup>lt;sup>1</sup> Feng et al. (2013) and Keating et al. (2015) have also conducted RT simulation post-processing cosmological hydrodynamical simulation, but without simultaneously accounting for both galaxies and QSOs.

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**Table 1.** Parameters used for the simulations described in the text. From left to right, the columns refer to the simulation ID; the normalization of the total ionizing photon emissivity of galaxies,  $f_{UV}$ ; the galaxy/QSO spectrum slope  $\alpha_G/\alpha_Q$ ; the inclusion/exclusion of the reionization history from galaxies in the range z = 15-10 ('history' column); the presence of a QSO; the inclusion of X-ray photons and of secondary ionization. The one highlighted in boldface (GAL\_R+QSO\_UVXsec) is our reference run.

Run ID	$f_{\rm UV}$	$\alpha_{\rm G}, \alpha_{\rm Q}$	History	QSO	X-ray	Secondary
Galaxies only						
GAL	0.1	3, n/a	off	off	off	off
GAL_0.5R	0.05	3, n/a	on	off	off	off
GAL_R	0.1	3, n/a	on	off	off	off
GAL_2R	0.2	3, n/a	on	off	off	off
QSO only						
QSO_UV	n/a	n/a, 1.5	off	on	off	off
QSO_UVX	n/a	n/a, 1.5	off	on	on	off
QSO_UVXsec	n/a	n/a, 1.5	off	on	on	on
QSO_obsc_UVXsec	n/a	n/a, 1.5 (obscured)	off	on	on	on
Galaxies+QSO						
GAL_R+QSO_UV	0.1	3, 1.5	on	on	off	off
GAL_R+QSO_UVX	0.1	3, 1.5	on	on	on	off
GAL_0.5R+QSO_UVXsec	0.05	3, 1.5	on	on	on	on
GAL_R+QSO_UVXsec	0.1	3, 1.5	on	on	on	on
GAL_2R+QSO_UVXsec	0.2	3, 1.5	on	on	on	on
GAL_R+QSO_obsc_UVXsec	0.1	3, 1.5 (obscured)	on	on	on	on

### 2.2 Multifrequency RT simulations

The outputs of the hydro simulations described above are postprocessed with the Monte Carlo RT code CRASH (Ciardi et al. 2001; Maselli, Ferrara & Ciardi 2003; Maselli, Ciardi & Kanekar 2009; Graziani, Maselli & Ciardi 2013; Graziani et al., in preparation), which, in its latest version, solves the cosmological RT of UV and soft X-ray photons<sup>2</sup> in a gas made of hydrogen and helium. We refer the reader to the original papers for more details on the code. Here, we assume an H and He number fraction of X = 0.92 and Y = 0.08, respectively.

The code self-consistently evolves the ionization state of hydrogen and helium and recalculates the gas temperature by solving for non-equilibrium chemistry and radiative heating and cooling processes. The photoionization heating of H<sub>I</sub>, He<sub>I</sub> and He<sub>II</sub>, recombination cooling and adiabatic cooling by cosmological expansion are self-consistently included within the RT calculation (see Maselli et al. 2003; Graziani et al. 2013; Graziani et al., in preparation for a more comprehensive list of heating and cooling mechanisms implemented in the code).

For our multifrequency RT calculations, the source spectrum from 13.6 eV to 2 keV is sampled by 42 frequency bins using 29 bins for the UV range, with finer sampling near the ionization threshold of H<sub>1</sub>(13.6 eV), He<sub>1</sub>(24.6 eV) and He<sub>II</sub>(54.4 eV), and 13 bins to cover the soft X-ray range. We have tested the sensitivity of the results to the upper frequency adopted, using 1, 2 and 4 keV. We find that the ionization and thermal structure within  $\sim 20 h^{-1}$  cMpc is insensitive to the upper cut, and we have thus chosen 2 keV. The Monte Carlo simulations cast 10<sup>6</sup> photon packets per galaxy and 2 × 10<sup>8</sup> per QSO. We have verified the convergence of the results in Appendix A. The RT of X-ray photons and the effect of fast photoelectrons produced by high-energy photons are described in detail in Graziani et al. (in preparation). Secondary ionization effects have been modelled by many authors (e.g. Shull & van Steenberg 1985; Dalgarno, Yan & Liu 1999; Valdés & Ferrara 2008; Furlanetto & Stoever 2010). Although the results are qualitatively similar among different approaches, there are some quantitative differences in the IGM thermal and ionization states. Here, we adopt the model by Valdés & Ferrara (2008). We refer the reader to Graziani et al. (in preparation) for a more comprehensive comparative analysis.

We create a suite of 14 RT simulations to study the reionization models by galaxies and QSOs (see Table 1). The procedure adopted is the following.

Our multifrequency RT simulations consist of two steps. First, we perform three runs from z = 15 until z = 10 with only galaxy-type sources. The runs differ only in the total ionizing photon emissivities of galaxies (parametrized by  $f_{UV}$ , see Section 2.3). Our fiducial run is indicated by 'R' (standing for Reference), while the other two ('0.5R' and '2R') have an emissivity that is  $0.5 \times R$  and  $2 \times R$ . The source models of galaxies are described in Section 2.3.

Secondly, we further evolve the final snapshot (at z = 10) for a time corresponding to the lifetime of the QSO,  $t_Q$ , including only galaxies ('Galaxies only' runs) or both galaxies and a QSO ('Galaxies+QSO' runs). The QSO is positioned within the most massive halo ( $1.34 \times 10^{10} h^{-1} M_{\odot}$ ) at the centre of the simulation box (see Section 2.4 for the detail of our QSO model). As a reference, the QSO alone is also switched on in a fully neutral medium ('QSO only' runs).

We then perform simulations with various combinations of RT processes (with/out photoionization by X-rays and contribution of secondary ionization) to study the impact of the QSO in exquisite details. Our reference run (GAL\_R+QSO\_UVXsec) follows UV and X-ray photons (with secondary ionization) emitted by galaxies

 $<sup>^{2}</sup>$  We refer to photons in the energy range 13.6–200 eV (200 eV–2 keV) as UV (soft X-ray) photons.





**Figure 1.** Total ionizing comoving emissivity from galaxies as a function of redshift, for  $f_{UV} = 0.05, 0.1, 0.2$  (dotted, solid and dashed lines). The data points are from Becker et al. (2015) based on observations of Lymanbreak galaxies by Oesch et al. (2013) and Bouwens et al. (2015). The arrow indicates the redshift (z = 10) at which a QSO is turned on.

as well as by the QSO in a medium ionized by the pre-existing galaxy population. The suite of RT simulations is summarized in Table 1.

#### 2.3 Source model: galaxies

To assign an ionizing photon production rate to a galaxy, we follow the method described in Ciardi et al. (2012), and we refer the reader to this paper for more details. Briefly, the comoving ionizing photon emissivity of the entire galaxy population at z > 6 is modelled based on a pre-assumed global star formation rate density, observations of the ionizing background from the Ly  $\alpha$  forest (Bolton & Haehnelt 2007) and of high-redshift galaxies (Oesch et al. 2013; Bouwens et al. 2015). The total ionizing photons are then distributed among all galaxies in the simulation box.

The comoving ionizing photon emissivity is given by (in units of photons  $s^{-1} cMpc^{-3}$ )

$$\dot{n}_{\rm ion}(z) = 10^{50.89} \chi(z) \frac{\alpha_{\rm b} + 3}{2\alpha} f_{\rm UV},\tag{1}$$

where  $\alpha$  and  $\alpha_b$  are the extreme-ultraviolet power-law spectral index of the sources and of the ionizing background, respectively, which are assumed to be equal to 3. The redshift dependence of the star formation rate density is parametrized as  $\chi(z) = \frac{\xi e^{\zeta(z-9)}}{\xi - \zeta + \zeta e^{\xi(z-9)}}$ , with  $\xi = 14/15$  and  $\zeta = 2/3$  (Bolton & Haehnelt 2007; Ciardi et al. 2012). The emissivity is normalized using the free parameter  $f_{\rm UV}$ , which is 0.1 in our fiducial model. Fig. 1 shows a comparison between our ionizing photon emissivity and the values inferred from observations of Lyman-break galaxies assuming an escape fraction of 30 per cent (Becker, Bolton & Lidz 2015 based on Oesch et al. 2013 and Bouwens et al. 2015). To take into account the large uncertainties in the value of the emissivity, we have also considered  $f_{\rm UV} = 0.05$  and 0.2.

To distribute the total ionizing photons among galaxies, we assume that each halo hosts one galaxy *i*, whose ionizing photon pro-



**Figure 2.** Model spectra of a QSO (red thick solid line), obscured QSO (red thick dashed) and galaxy (blue thin solid). For a comparison, the black dash-dotted line shows a spectrum at 10 Myr after a burst of star formation with metallicity Z = 0.001 from starburst99. The vertical lines indicate the ionization thresholds of H I, He I and He II, from left to right.

duction rate,  $\dot{N}_{ion}^{GAL}(M_{h,i})$  (in units of photons s<sup>-1</sup>), scales linearly with the host halo mass, i.e.

$$\dot{N}_{\rm ion}^{\rm GAL}(M_{{\rm h},i}) = \dot{n}_{\rm ion}(z) V_{\rm box} \frac{M_{{\rm h},i}}{\sum_{j=1}^{N_{\rm s}} M_{{\rm h},j}},$$
(2)

where  $V_{\text{box}}$  is the comoving volume of the simulation box and  $N_s$  is the total number of galaxies (or haloes) in the simulation.  $\dot{n}_{\text{ion}}(z)V_{\text{box}}$ is the total number of ionizing photons present at redshift z.

The spectrum of a galaxy is modelled with a power-law spectral energy distribution (SED),  $L_{\nu}^{\text{GAL}}(\nu) \propto \nu^{-\alpha_{\text{G}}}$ , with spectral index  $\alpha_{\rm G} = 3$ , and it is related to the ionizing photon production rate as  $\dot{N}_{\text{ion}}^{\text{GAL}} = \int_{\nu_{\text{I}}}^{\infty} (L_{\nu}^{\text{GAL}}(\nu)/h\nu) \, d\nu$ , where  $\nu_{\text{L}} = 3.29 \times 10^{15}$  Hz is the frequency at the Lyman limit. The spectrum is plotted in Fig. 2 (solid thick blue line), together with a spectrum at 10 Myr after a starburst with metallicity Z = 0.001 from starburst99 (black dotted line; Leitherer et al. 1999). While the SED between  $hv_{H_{I}}$  and  $hv_{H_{I}}$  is well approximated by the power law, it drops abruptly at  $> h v_{\text{HeI}}$  due to the absorption by the stellar atmosphere in the spectral synthesis model. We have nevertheless adopted a simple power law for a more straightforward comparison with a QSO model (Section 2.4), and show the He III results for galaxies for completeness. In this paper, we have drawn conclusions that are not affected by this assumption, and we intend to employ a more accurate population synthesized galaxy spectra in future work.

### 2.4 Source model: QSO

We model the ionizing photon production rate,  $\dot{N}_{\rm ion}^{\rm QSO}$ , of our z = 10 QSO by re-scaling the properties of the ULAS J1120+0641 QSO at z = 7.085, which is estimated to have a central supermassive black hole (SMBH) of mass  $M_{\rm BH} = 2 \times 10^9 \, \rm M_{\odot}$  and  $\dot{N}_{\rm ion}^{\rm QSO} = 1.36 \times 10^{57}$  photons s<sup>-1</sup> (Bolton et al. 2011; Mortlock et al. 2011). Assuming a smaller SMBH mass of  $M_{\rm BH} = 2 \times 10^8 \, \rm M_{\odot}$  to reflect a higher redshift environment and adopting an Eddington limit accretion rate, i.e. the bolometric QSO luminosity scaling linearly with the SMBH mass, this translates into  $\dot{N}_{\rm ion}^{\rm QSO} \propto M_{\rm BH}$ , giving

$$\dot{N}_{\rm ion}^{\rm QSO} = 1.36 \times 10^{56} \text{ photons s}^{-1}.$$
 (3)



**Figure 3.** 3D visualization of the H II (left), He II (middle) and He III (right) fractions in the QSO environment, as produced by both the central QSO and the surrounding galaxies with full UV and X-ray physics at (GAL\_R+QSO\_UVXsec). The images refer to a time  $t_Q = 10^7$  yr after the QSO has been turned on at z = 10. Unless otherwise stated, all the following figures refer to the same time. Top panels: the whole simulation box of 50  $h^{-1}$  cMpc. Bottom panels: dissection through the central QSO. Some ionized regions near the edge appear to reside outside the box because of the visualization reason. The colours correspond to an ionized fraction of  $x_i \sim 1$  (red),  $x_i \sim 0.1$ –0.001 (green to blue) and  $x_i \sim 0$  (grey), where i = H II, He II. A more quantitative analysis is shown in Sections 3.1–3.4.

The QSO spectrum is assumed to be a power law  $L_{\nu}^{\text{QSO}}(\nu) \propto \nu_{\text{L}}^{-\alpha_{\text{Q}}}$  with index  $\alpha_{\text{Q}} = 1.5$  (the same as the one of ULAS J1120+0641; Bolton et al. 2011; Mortlock et al. 2011), and it is lated to the ionizing photon production rate as  $\dot{N}_{\text{ion}}^{\text{QSO}} = \int_{\nu_{\text{L}}}^{\infty} (L_{\nu}^{\text{QSO}}(\nu)/h\nu) d\nu$ . In addition, we also consider a model (red dashed line in Fig. 2)

In addition, we also consider a model (red dashed line in Fig. 2) in which the QSO spectrum is obscured by a spherical shell of neutral gas with an H<sub>I</sub> column density<sup>3</sup> of  $N_{\rm H_I} = 10^{20}$  cm<sup>-2</sup>, i.e.  $L_{\nu}^{\rm QSO,obsc}(\nu) = L_{\nu}^{\rm QSO}(\nu)e^{-\sigma_{\rm H_I}(\nu)N_{\rm H_I}}$ , where  $\sigma_{\rm H_I}(\nu)$  is the H<sub>I</sub> photoionization cross-section (Draine 2011). Note that in an obscured QSO model the ionizing photon production rate is reduced to  $\dot{N}_{\rm ion}^{\rm QSO,obsc} = 4.33 \times 10^{54}$  photons s<sup>-1</sup> because a large fraction of ionizing photons with  $\nu < \nu_{\rm He_{II}}$  are absorbed before escaping into the IGM. This effectively hardens the spectrum of the QSO, by removing most of its UV photons.

The lifetime of the QSO is assumed to be  $t_Q = 10^7$  yr unless otherwise stated. This is chosen from the range of values  $10^6$  yr  $< t_Q < 10^8$  yr that are observationally allowed at lower redshift (Martini 2004). We note that, because the recombination time-scale is much shorter than the QSO lifetime, increasing lifetime and/or luminosity trivially increases the size of ionized regions as  $R_I \propto (\dot{N}_{\rm ion}^{\rm QSO} t_Q)^{1/3}$ . The temperature is expected to be insensitive to luminosity and lifetime, although the radius to which the gas is photoheated increases with luminosity and lifetime. We discuss the impact of the QSO duty cycle in Appendix B for interested readers.

 $^3$  This H<sub>1</sub> column density is chosen based on lower redshift observations of AGNs (Ueda et al. 2003; La Franca et al. 2005) and on the value assumed in a similar theoretical work (Kramer & Haiman 2008).

In our model, both unobscured and obscured QSOs are assumed to emit ionizing photons isotropically. The opening angle of QSOs at z > 6 is not well constrained, but anisotropic emission will generally produce an anisotropic (possibly bipolar) region of ionization in the IGM around the QSOs.

# **3 IONIZATION STATE OF THE IGM**

In this section, we present the results from our suite of RT simulations with galaxies alone (galaxies only models), a QSO alone (QSO only models), and galaxies and a QSO combined (galaxies+QSO models), and we discuss their impact on hydrogen and helium reionization.

The 3D visualization in Fig. 3 describes the results for our full reference simulation (GAL\_R+QSO\_UVXsec) at the end of the QSO lifetime.<sup>4</sup> The figure shows clearly the very rich morphology of H II and He II/He III regions in the high-*z* QSO environment. The QSOs, together with the surrounding galaxies, form a central large H II region on scales of tens of comoving megaparsecs and many smaller H II regions. The X-ray radiation from the QSO also partially ionizes the IGM beyond the sharp H II I-front. The He II regions show a morphology similar to that of the H II regions, although the He II I-front is slightly broader than the H II I-front because of the larger mean free path of photons near the He II regions produced

<sup>&</sup>lt;sup>4</sup> Unless otherwise stated, all our results are shown at a time corresponding to  $t_Q = 10^7$  yr after the QSO has been turned on at z = 10.



**Figure 4.** Maps of H II (top panels), He II (middle) and He III (bottom) fractions for model GAL (left column) and QSO\_UVXsec (right). In both models, the sources are turned on in a fully neutral medium at z = 10 and shine for  $10^7$  yr. The maps have a side length of  $50 h^{-1}$  cMpc and the width of the slice is  $195 h^{-1}$  ckpc.

by galaxies are extremely small<sup>5</sup> because of the paucity of He IIionizing photons emitted by them. On the other hand, the QSO produces a large almost spherical He III region because of the high He II-ionizing radiation. The He III I-front is even broader due to the larger mean free path of photons near the He II ionization threshold.

In the following, we explore in detail the impact of varying both the source models (of the galaxies and the QSO) and the physical processes of RT on the intergalactic hydrogen and helium.

# 3.1 H II, He II and He III regions from galaxies and a QSO in a neutral IGM

We first examine the simplest case in which either galaxies or a QSO create ionized regions in a fully neutral gas.

Fig. 4 (top panels) shows slices of H II fraction,  $x_{\text{HII}}$ , in models GAL and QSO\_UVXsec, where only galaxies or a QSO are switched on at z = 10 and for a duration of  $10^7$  yr in a fully neutral IGM. While a single large fully ionized region appears around the QSO, the numerous fainter galaxies produce many smaller H II regions. This morphological difference is caused by the fact that in the QSO model all the photon budget is concentrated in one single



Figure 5. Distribution of the H II (top panel) and He III (bottom panel) Ifront radii for models GAL (dashed) and QSO\_UVXsec (solid). The PDF of the He II I-fronts is nearly identical to that of the H II I-fronts, and thus it is not shown here.

source rather than being distributed among many fainter galaxies. In addition, the QSO emits about 15 times more ionizing photons than the galaxies. Another prominent difference in the ionization structure is the partially ionized shell produced by the X-ray photons emitted by the QSO (see Section 3.2 for more details).

The middle and bottom panels of Fig. 4 show maps of He II and He III fractions. As for the H II fraction, the GAL and QSO\_UVXsec models present a clearly different morphology. When reionization is driven by galaxies, the morphology of the He II and H II regions is qualitatively very similar. The reason for this is that, although our galaxy-type spectrum emits a factor of  $L_{\nu}^{GAL}(\nu_{HeI})/L_{\nu}^{GAL}(\nu_{HI}) \simeq 0.17$  less He I- than H I-ionizing photons, the abundance of helium is  $Y/X \simeq 0.09$  smaller than the one of hydrogen. As a result, when driven by galaxies, the reionization history and morphology of He I and H I are similar. On the other hand, as galaxies emit a factor of  $L_{\nu}^{GAL}(\nu_{HeII})/L_{\nu}^{GAL}(\nu_{HI}) \simeq 0.016$  less He II- than H I-ionizing photons due to the higher ionization threshold of He II, the He III regions are much more compact.

A QSO, on the other hand, produces a very distinctive He II region, as well as a highly regular, large He III region. Because a QSO emits  $\simeq 0.4$  He I- and  $\simeq 0.13$  He II-ionizing photons per H I-ionizing photon, unlike galaxies, a QSO drives He I and He II reionization simultaneously to H I reionization, and the He III I-front follows immediately after the He II I-front. This creates a 'shell'-like structure in He II, containing a large He III region. Note that this structure is a distinctive feature in a high-redshift QSO environment; in contrast, at lower redshift (z < 6) a QSO creates a 'hole' in He II, because He I reionization by that time has already been completed by galaxies.

For a more quantitative comparison, in the top panels of Fig. 5, we plot the distribution of the I-front radii,<sup>6</sup>  $R_{\rm I}^{\rm H\,I}$ , produced by the QSO (solid line) and the galaxies (dashed line) along 100 random

<sup>&</sup>lt;sup>5</sup> Note that a non-negligible contribution of galaxies to the He III regions is a result of our power-law spectrum assumption. For population synthesized galaxy spectra, we expect galaxies to produce negligibly small He III region.

<sup>&</sup>lt;sup>6</sup> The I-front radius is defined as the distance from the central source at which  $x_{H_{II}}$  drops below 50 per cent for the first time.

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lines of sight (LOSs) from the central source. While a central QSO alone can create an H II region as large as  $R_{\rm I}^{\rm H\,II} \sim 13 \, h^{-1} \, {\rm cMpc}$ , galaxies produce a smaller I-front with radius  $R_{\rm I}^{\rm H\,II} < 3 \, h^{-1} \, {\rm cMpc}$ . Furthermore, a QSO-type source shows a dispersion of the H II I-front radii of  $\sim 5 \, h^{-1} \, {\rm cMpc}$ . This is caused by density fluctuations of the IGM: while dense gas clumps cast shadows behind them, the I-fronts propagate unimpeded along underdense directions (Iliev et al. 2006; Keating et al. 2015 and also see Graziani et al., in preparation). Because the I-fronts propagate more quickly than the gas can respond, shadowing will persist until gas clumps are photoevaporated. Depending on their column density, then, the clumps could also remain self-shielded. This has been shown, e.g., in the coupled radiation hydrodynamic simulation of Meiksin & Tittley (2012).

The distribution of the He III I-front radii is shown in the bottom panel of Fig. 5. QSO's He III I-fronts (solid line) have an extension of  $R_{\rm I}^{\rm He III} \sim 12 \, h^{-1} \, \rm cMpc$ , slightly smaller than the corresponding H II I-fronts. Galaxies (dashed line) produce negligibly small radii. The dispersions of the QSO's H II and He III I-fronts are very similar, as both of them are caused by shadowing by dense clumps.

#### 3.2 Effect of X-rays and secondary ionization

Here we study the effect of X-rays and secondary ionization on the region ionized by the central QSO. This clarifies the physical origin of the extended tail of partial ionization in the QSO model seen in Figs 3 and 4.

Fig. 6 shows the spherically averaged profiles of ionization fractions,  $\langle x_i(r) \rangle_S$ , together with the corresponding  $1\sigma$  scatter,  $\sigma_i^2(r) = \langle x_i^2(r) \rangle_S - \langle x_i(r) \rangle_S^2$ , where  $i = H \Pi$ , He II, He III. The figure compares the three QSO only models with different RT processes, i.e. spectra restricted only to UV photons (QSO\_UV), including UV+X-ray photons but neglecting the effect of secondary ionization (QSO\_UVX), and including UV+X-ray photons and secondary ionization (QSO\_UVX), and including UV+X-ray photons and secondary ionization (QSO\_UVX). The main impact of X-rays and secondary ionization on both hydrogen and helium is to produce an extended tail of low ionization beyond the I-fronts.

In the case of hydrogen, while the impact of X-rays is to increase the ionized fraction to  $\langle x_{\rm Hmathscii}(r) \rangle_S \sim 10^{-3}$  (QSO\_UVX), secondary ionization further enhances it to  $\langle x_{\rm H\, II}(r) \rangle_S \sim 10^{-2}$  (QSO\_UVXsec; see also Wise & Abel 2011). The ionized fraction has LOS fluctuations of about a factor of ~3 as a result of density fluctuations.<sup>7</sup>

Similarly, the partially ionized tails of He II and He III have ionized fractions of  $\langle x_{\text{He II}}(r) \rangle_S \sim 10^{-2}$  and  $\langle x_{\text{He III}}(r) \rangle_S \sim 10^{-4} - 10^{-3}$ . However, the impact of secondary ionization is less significant than on hydrogen, with an enhancement of only a factor of ~2. This is because, due to its lower abundance, the probability that helium is collisionally ionized by fast electrons is, to a first-order approximation, a factor of  $Y/X \simeq 0.09$  lower than the one for hydrogen.





**Figure 6.** Spherically averaged profiles of H II (top panel), He II (middle) and He III (bottom) fractions around a QSO turned on at z = 10 in a neutral medium including only UV photons (QSO\_UV, blue dotted lines), UV and X-ray photons (QSO\_UVX, red dashed), UV, X-ray photon and secondary ionization (QSO\_UVXsec, black solid). The shaded regions show the  $1\sigma$  scatter of LOS fluctuations. The profiles are shown at the end of the QSO lifetime  $t_{\rm Q} = 10^7$  yr.

Fig. 7 shows the distribution of the H II and He III I-front radii and their I-front thickness<sup>8</sup> based on 100 random LOSs for the three QSO models discussed above. When neglecting secondary ionization, both distributions are weakly affected by X-rays (red dashed versus blue dotted lines). This is a direct consequence of the fact that most of the H I- and He II-ionizing power is dominated by photons emitted near the ionization thresholds, i.e. the UV photons. The photoionization by X-ray photons alone does not sensitively modify the ionization state of the IGM near the I-fronts, while the extended tail of partially ionized regions is indeed a strong feature of X-rays.

With secondary ionization, the I-front positions are pushed slightly outwards, by  $\sim 1 h^{-1}$  cMpc, and their thickness is broadened by  $\sim 50$  per cent. While this could be a result of secondary ionization preferentially enhancing the ionization level in initially more neutral regions, we caution that the extent of such effect is also

<sup>8</sup> The thickness is defined as the distance between the location where the ionized fraction is 90 per cent and that at which it becomes 10 per cent. As a first approximation, the thickness is about a mean free path,  $\lambda_{mfp}(\nu) = [n_H(z)\sigma_{H1}(\nu)]^{-1}$ , of typical photons reaching the I-front (e.g. Spitzer 1998; Zaroubi & Silk 2005; Kramer & Haiman 2008). Although the thickness of the I-front is unresolved, i.e.  $\lambda_{mfp} < \Delta x_{cell}$ , where  $\Delta x_{cell} = 195 h^{-1}$  kpc is the cell size of our simulations, we use the above definition to support the claim that the presence of X-ray photons alone does not modify the thickness of the I-fronts.



**Figure 7.** Distribution of the H II/He III I-front positions (left-hand panels) and thickness (right-hand panels) for the three QSO models including only UV photons (QSO\_UV, blue dotted), UV and X-ray photons (QSO\_UVX, red dashed), UV, X-ray photon and secondary ionization (QSO\_UVXsec, black solid).

related to the gas distribution and the model used for the physics of secondary ionization (Graziani et al., in preparation), as well as the I-front definition.

# 3.3 H II, He II and He III regions from galaxies and a QSO in a pre-ionized IGM

We now analyse the more realistic case in which a QSO is turned on at z = 10 in a medium that has already been ionized by pre-existing galaxies. We consider three different reionization histories, which differ only for the total ionizing photon emissivity, namely models 2R, R and 0.5R. As a reference, the H II (He II) volume-averaged fraction at z = 10is  $\langle x_{\text{H II}} \rangle_V \approx 28$  per cent, 13 per cent, 6 per cent ( $\langle x_{\text{He II}} \rangle_V \approx$ 26 per cent, 12 per cent, 5 per cent) for 2R, R, 0.5R, respectively. On the other hand, the contribution of the pre-existing galaxies to He II reionization is negligibly small. In the following, we analyse in great detail how the combined effect of a QSO and galaxies shapes the ionization state of the IGM.

The top panels of Fig. 8 show maps of H II fraction for both galaxies only and galaxies+QSO models. Differently from the scenario in Section 3.1, the combined effect of galaxies and a QSO produces a morphology (size and shape) of the fully ionized H II regions (with  $x_{\rm Hu} \gtrsim 0.9$  similar to the one when no QSO is present (see Fig. 9 for a quantitative description). Galaxies alone, in fact, can also produce a large quasi-spherical HII region due to a combination of their clustering in the high-density regions where QSOs preferentially reside and the long time-scale that they have been shining for, allowing for the growth and overlap of many small H II regions. The OSO contributes to produce a slightly larger HII region (see the discussion below) and a prominent tail of partial ionization, which remains a distinctive feature produced by the X-ray photons (see Section 3.2). Furthermore, the QSO contributes to hydrogen ionization within the HII region. As a reference, in the galaxies+QSO model (GAL R+QSO+UVXsec), the median value of the residual neutral hydrogen fraction is only  $x_{\rm H_{I}} \approx 9 \times 10^{-6}$ , while the galaxies only model (GAL\_R) still contains  $x_{\rm H_{I}} \approx 8 \times 10^{-4}$  neutral hydrogen in the central HII region (cf. the mean value inside the H II region for the galaxies only model is  $\langle x_{\rm HI} \rangle_V \approx 2 \times 10^{-3}$ ).

The middle and bottom panels of Fig. 8 show the corresponding maps of He  $\scriptstyle\rm II$  and He  $\scriptstyle\rm III$  fractions. Unlike for the H  $\scriptstyle\rm II$ 



**Figure 8.** Maps of H II (top panels), He II (middle) and He III (bottom) fraction for galaxies only models GAL\_0.5R, GAL\_R, GAL\_2R, and galaxies+QSO models GAL\_0.5R+QSO\_UVXsec, GAL\_R+QSO\_UVXsec, GAL\_2R+QSO\_UVXsec. In both sets of models, galaxies start to reionize the IGM at z = 15, while the QSO is turned on at z = 10 for a duration of  $10^7$  yr in the medium already reionized by the pre-existing galaxies. The maps have a side length of  $50 h^{-1}$  cMpc and the width of a slice is  $195 h^{-1}$  ckpc.



Figure 9. Distribution of the H  $\pi$  (left-hand panels) and He  $\pi$  (right-hand panels) I-front positions for galaxies only (top) and galaxies+QSO (bottom) models. The line style indicates the different source models of galaxies (i.e. different total ionizing photon emissivity): GAL\_0.5R (blue dotted), GAL\_R (black solid) and GAL\_2R (red dashed).

regions, the galaxies only and galaxies+QSO models exhibit very distinctive features not only in the partially ionized tails but also in the fully ionized He II/He III regions. In the galaxies only models, He I and HI reionizations progress simultaneously and have a similar morphology. The QSO just increases the extent of the pre-existing He II regions. At the same time, its hard spectrum doubly ionizes helium behind the He II I-fronts induced by galaxies, producing an extended He III region and leaving only a shell of He II. The width of the shell increases with the ionizing photon emissivity of galaxies because the extent of the pre-existing He II region is larger. As the QSO dominates the ionization of He II to He III, the He III region is very regular, almost spherical.

The left-hand panels of Fig. 9 show the distribution of the HII I-front radii for galaxies only and galaxies+QSO models. As expected, the radius increases with the total ionizing photon emissivity. With our I-front definition, the dispersion is  $>5 h^{-1}$  cMpc, larger than the one in the QSO-only models (see Fig. 5), because it is induced not only by the density fluctuations as discussed in Section 3.1 but also by the irregularities that follow the overlap of multiple smaller HII regions. The QSO pushes the HeIII I-front to  $\sim 13 h^{-1}$  cMpc (right-hand panels). As the QSO dominates the production of the HeIII region, the I-front radius is insensitive to the change in total ionizing emissivity of galaxies. In addition, the dispersion of the He III I-front is limited to only  $\sim 5 h^{-1}$  cMpc, smaller than that of the H II I-front, because the fluctuations in this case are caused only by the density fluctuations of the IGM (as discussed in Section 3.1), while the irregularities due to the overlap of negligibly small He III regions produced by galaxies are irrelevant.

#### 3.3.1 Relative importance of galaxies and QSO

We highlight that the ratio of total cumulative ionizing photons emitted by galaxies and QSOs since the onset of reionization is the most important quantity for determining the ionization structure of the IGM during reionization. We elaborate on the role of galaxies around a QSO by the following simple illustrative argument.

The total number of ionizing photons emitted by galaxies within a comoving radius *r* around a QSO since the onset of reionization,

$$N_{\rm ion}^{\rm GAL}(< r) = \int_{z}^{z_0} dz' \left| \frac{dt}{dz'} \right| \dot{n}_{\rm ion}(z') \int_{0}^{r} dr' 4\pi r'^{2} [1 + \xi_{\rm qg}(r')],$$
$$= \frac{4\pi}{3} n_{\rm ion}^{\rm GAL}(z) r^{3} \left[ 1 + \frac{4\pi}{3 - \gamma} \left( \frac{r}{r_0} \right)^{-\gamma} \right], \tag{4}$$

where  $n_{\rm ion}^{\rm GAL}(z) = \int_{z}^{z_0} dz' |dt/dz'| \dot{n}_{\rm ion}(z')$ , with |dt/dz| = 1/[H(z)(1 + z)], is the total comoving ionizing photon density from galaxies between the onset of reionization  $z_0$  and redshift z.  $\xi_{\rm qg}(r) = (r/r_0)^{-\gamma}$  is the QSO–galaxy correlation function, where  $r_0$  is the correlation length and  $\gamma$  is the power-law index. The I-front radius of the H II region produced by such population of galaxies,  $R_{\rm I,gal}^{\rm H\,II}$ , can be estimated by equating the number of ionizing photons and hydrogen atoms inside the radius, i.e.  $(4\pi/3)\bar{n}_{\rm H}(0)(R_{\rm I,gal}^{\rm H\,II})^3 = N_{\rm ion}^{\rm GAL}(< R_{\rm I,gal}^{\rm H\,II})$ , obtaining

$$R_{\rm I,gal}^{\rm H\,II} = r_0 \left[ \frac{3 - \gamma}{4\pi} \left( \frac{\bar{n}_{\rm H}(0)}{n_{\rm ion}^{\rm GAL}(z)} - 1 \right) \right]^{-1/\gamma},\tag{5}$$

where  $\bar{n}_{\rm H}(0)$  is the mean comoving hydrogen number density. Using the best-fitting power-law QSO–galaxy correlation function to our simulation, i.e.  $r_0 = 18.6 h^{-1}$  cMpc and  $\gamma = 1.6$ , we find  $R_{\rm L,gal}^{\rm H\,I} \approx 12 h^{-1}$  cMpc for our reference galaxies model (GAL\_R), which is in reasonable agreement with the simulation (see Fig. 9).

Once a QSO is switched on in the H II region produced by preexisting galaxies, it dominates the growth of the I-front radius,  $R_I^{H II}$ , which can be estimated from Donahue & Shull (1987), Shapiro & Giroux (1987) and Madau et al. (1999):

$$\frac{4\pi}{3} (R_{\rm I}^{\rm H\,{\scriptscriptstyle II}})^3 - \frac{4\pi}{3} (R_{\rm I,gal}^{\rm H\,{\scriptscriptstyle II}})^3 = \frac{\dot{N}_{\rm ion}^{\rm QSO} \tilde{t}_{\rm rec,\,\rm H\,{\scriptscriptstyle II}}}{\bar{n}_{\rm H}(0)} \left(1 - e^{-t_{\rm Q}/\tilde{t}_{\rm rec,\,\rm H\,{\scriptscriptstyle II}}}\right), \qquad (6)$$

where  $\bar{t}_{rec,Hu}$  is the recombination time-scale of hydrogen. Assuming that the QSO lifetime is much shorter than the recombination time-scale, the final I-front radius is given by

$$R_{\rm I}^{\rm H\,{}_{\rm I}} = R_{\rm I,gal}^{\rm H\,{}_{\rm I}} \left[ 1 + \left( \frac{R_{\rm I,QSO}^{\rm H\,{}_{\rm I}}}{R_{\rm I,gal}^{\rm H\,{}_{\rm I}}} \right)^3 \right]^{1/3},\tag{7}$$

where  $R_{1,QSO}^{H_{II}} = [\frac{3\dot{N}_{QSO}^{O_{IQ}}}{4\pi \bar{n}_{H(0)}}]^{1/3}$  is the comoving I-front radius produced by a QSO when it is turned on in isolation. For our reference values, we find  $R_{1,QSO}^{H_{II}} \approx 11.8 h^{-1}$  cMpc, consistent with the results of the simulations shown in Fig. 5 (QSO\_UVXsec). Finally, the total I-front radius including both galaxies and a central QSO is  $R_{I}^{H_{II}} \approx 15 h^{-1}$  cMpc, again in reasonable agreement with the simulations (see Fig. 9, GAL\_R+QSO\_UVXsec). Note that in our three galaxies+QSO models the ratio of ionizing photons emitted by galaxies compared with QSOs within  $10 h^{-1}$  cMpc is  $N_{ion}^{GAL}(<10 h^{-1} \text{ cMpc})/(\dot{N}_{ion}^{QSO}t_Q) = 0.65$  (GAL\_0.5R+QSO\_UVXsec), 1.30 (GAL\_R+QSO\_UVXsec) and 2.60 (GAL\_2R+QSO\_UVXsec), encompassing the cases for QSO-dominated, comparable contribution from galaxies and a QSO, and galaxies-dominated scenarios.

The fact that the simulated size of the H II region can be broadly obtained using simple analytic estimates indicates that the ionization structure of the IGM largely depends on (i) the total cumulative ionizing photon emissivity from galaxies,  $n_{\rm ion}^{\rm GAL}(z)$ , (ii) the QSO–galaxy correlation function,  $\xi_{\rm qg}(r)$ , and (iii) the ionizing photons emitted by a QSO,  $\dot{N}_{\rm ion}^{\rm QSO} t_{\rm Q}$ . More specifically, the final size of the H II region strongly depends on the ratio between the product of the ionizing photon production rate and the lifetime of the central QSO,  $\dot{N}_{\rm ion}^{\rm QSO} t_{\rm Q}$ , and the integrated total ionizing photons of galaxies



Figure 10. Spherically averaged profiles of H II (solid), He II (dotted) and He III (dashed) fractions for QSO (QSO\_UVXsec, red lines) and obscured QSO (QSO\_obsc\_UVXsec, blue lines) models.

around a QSO,  $N_{\text{ion}}^{\text{GAL}}(< r)$ , since the onset of reionization. If the cumulative number of photons emitted from galaxies since the onset of reionization exceeds or is comparable to that from a QSO during its activity, the resulting H II region is very similar. On the other hand, if a QSO dominates the total ionizing photons in the environment, the QSO imprints a distinctive H II region.

### 3.4 Effect of an obscured QSO

In the following, we analyse the RT simulation suite to understand the impact of the QSO's spectral properties on the ionization state of the IGM.

Here, we consider a variant of the QSO model (and galaxies+QSO model) in which all the ionizing UV photons are absorbed by neutral hydrogen inside the host galaxy (see Fig. 2)

and the radiation impacting the surrounding IGM is composed only by the soft X-ray part of the original spectrum.

Fig. 10 shows the spherically averaged profiles of the unobscured (QSO\_UVXsec) and obscured (QSO\_obsc\_UVXsec) QSO models. In the obscured QSO model, reionization is driven only by soft X-ray photons, and, as a consequence, the H II and He III regions are much smaller than those from the unobscured QSO. In addition, the lack of UV photons and the larger mean free path of X-ray photons create I-fronts smoother than those of the unobscured QSO model. We note that the size of the H II region in the obscured QSO model is consistent with the simple Strömgren sphere estimate, which gives  $R_{\rm LobsCOSO}^{\rm HI} = R_{\rm LOSO}^{\rm HI} (\dot{N}_{\rm QSO}^{\rm QSO})^{1/3} \approx 3.8 h^{-1} \, \rm cMpc.$ 

To illustrate the difference in the structure near the H II and He III I-fronts, Fig. 11 shows the linear-scale maps of H II and He III fractions for galaxies only model (GAL\_R), galaxies+(unobscured) QSO model (GAL\_R+QSO\_UVXsec) and galaxies+obscured QSO model (GAL\_R+QSO\_obsc\_UVXsec) at the snapshots corresponding to the two QSO lifetimes of  $t_0 = 10^7$  and  $8 \times 10^7$  yr. Unlike the obscured QSO only model, when the contribution from galaxies is included, at  $t_0 = 10^7$  yr the H II I-front structures show little difference between the galaxies+unobscured QSO and galaxies+obscured QSO models. This is because the growth of the I-front is still dominated by galaxies at  $t_0 = 10^7$  yr. However, for a longer lifetime, the number of ionizing photons from the obscured OSO becomes larger than the one from the galaxies, and as a consequence, a wider HII I-front is formed. Thus, the imprint left on the HII region by an obscured QSO is more distinctive than the one left by an unobscured QSO, even in the presence of galaxies.

The impact of an obscured QSO is more visible in the ionization state of the intergalactic helium. Due to the lack of UV photons and the predominance of soft X-ray photons, the He III I-front produced by an obscured QSO is smoother and wider than the one from an unobscured QSO.

In summary, an obscured QSO can imprint distinctive features on the surrounding  $H_{II}$  regions by producing a smooth and broad I-front. The effect, though, is noticeable only if the



**Figure 11.** Linear-scale maps of H II (top panels) and He III (bottom) fractions for galaxies only model GAL\_R, galaxies+QSO model GAL\_R+QSO\_UVXsec and galaxies+obscured QSO model GAL\_R+QSO\_obsc\_UVXsec at  $t_Q = 10^7$  yr (first three columns), and model GAL\_R+QSO\_obsc\_UVXsec at  $t_Q = 8 \times 10^7$  yr (last column). The QSO is turned on at z = 10 in the medium already reionized by galaxies. The length of *x*- and *y*-axes is  $50 h^{-1}$  cMpc and the width of the slice is  $195 h^{-1}$  ckpc. The linear scale was chosen to show structure near the I-front more clearly.



**Figure 12.** Maps of temperature for models GAL (left) and QSO\_UVXsec (right). In both models, the sources are turned on in a fully neutral medium at z = 10 and shine for  $10^7$  yr. The maps have a side length of  $50 h^{-1}$  cMpc and the width of the slice is  $195 h^{-1}$  ckpc. The H II (He III) I-front is shown as blue solid (dotted) contour.

number of soft X-ray photons exceeds the UV photon budget from the galaxies.

### **4 THERMAL STATE OF THE IGM**

In the previous section, we examined the ionization state of the IGM. Here, we investigate the impact of varying sources, their properties and environments, and the physical processes of RT on the thermal state of the IGM.

The thermal structure of the IGM surrounding a QSO is affected in a complex, non-linear way, by the combined input of the galaxies and the QSO. We present our results with increasing sophistication to highlight the effect of photoionization heating across the I-fronts (Section 4.1), pre-heating by X-rays (Section 4.2), and the additional complexity when both galaxies and QSOs are taken into account (Section 4.3).

# 4.1 Thermal state induced by galaxies and a QSO in a neutral IGM

We first present the simplest case where heating is due to photoionization from only galaxies or QSO, i.e. the equivalent of Section 3.1. Fig. 12 shows temperature maps for the galaxies (GAL, left) and the QSO (QSO\_UVXsec, right) only model. The contours refer to the position of the H II (solid) and He III (dotted) I-fronts. In both models, the filamentary thermal structure in the H I regions is a result of adiabatic compression and hydrodynamic shocks along filaments of cosmic web. Gas within H II regions is heated by photoionization to  $\gtrsim 10^4$  K, and therefore, the thermal structure is well traced by the position of the I-fronts. Similarly to the ionization structure discussed in Section 3.1, galaxies produce small and patchy heated regions, whereas a large central hot region is present around the QSO, together with warm gas heated by X-rays ahead of the sharp I-front (see Section 4.2 for more details).

Fig. 13 shows the temperature–density diagram for the two source models discussed above, as well as for the hydrodynamical simulation without RT. The colour indicates H II (H I) regions where the local H II fraction is  $x_{HII} \ge 0.5(<0.5)$ . The temperature of the QSO's H II region (~17 000 K) is ~16 per cent higher than the one of galaxies' H II regions (~14 700 K), because the QSO harder spectrum heats the gas more effectively per H I and He I ionization (see Section 4.1.1), and provides an additional heating by He II photoionization. The temperature of the H II regions is nearly isothermal



**Figure 13.** Temperature–density diagram for models GAL (left), QSO\_UVXsec (middle) and for the hydrodynamic simulations without RT (right). The sources are turned on in a fully neutral medium at z = 10 and shine for  $10^7$  yr. The red (blue) colour indicates the H II (H I) regions defined as cells with  $x_{\rm H II} \ge 0.5$  (<0.5). The contours are overlaid as a guide. To emphasize the temperature–density relation both in H II and H I regions, two different *y*-axis scales are used.

in both models, because the gas is ionized within a short period of time (10<sup>7</sup> yr) and no substantial adiabatic or recombination cooling (which preferentially cools low- and high-density regions, respectively) has taken place. While the temperature–density relation of the neutral gas in the galaxies only model is solely determined by hydrodynamic processes (see a comparison between the GAL and Hydro panels), the X-ray photons emitted by the QSO propagate ahead of the H II I-front, partially ionizing the gas and heating it to  $\sim 10^3$  K (see also Section 4.2).

# 4.1.1 Photoionization heating

The extent of the IGM heating due to the passage of the I-fronts depends on the spectral shape of the sources, while it is insensitive to their ionizing photon luminosities. The heat gain per ionization across an I-front is (e.g. Abel & Haehnelt 1999)

$$\langle E_i \rangle = G_i / \Gamma_i \approx \frac{h \nu_i}{2 + \alpha_{\text{eff}}},$$
(8)

where  $G_i = \int_{v_i}^{\infty} \frac{4\pi J_v}{hv} \sigma_i(v)(hv - hv_i) dv$  is the thermal energy injected by photoionization,<sup>9</sup>  $J_v$  is the specific intensity,  $(hv - hv_i)$  is the excess energy of photoionization above the ionization threshold,  $\Gamma_i = \int_{v_i}^{\infty} \frac{4\pi J_v}{hv} \sigma_i(v) dv$  is the photoionization rate and  $\alpha_{\text{eff}}$  is the effective spectral index at the position of the I-front. The index *i* indicates the different species, i.e. i = HI, He I, He II. In the optical thin limit  $\alpha_{\text{eff}} = \alpha_{\text{G}}$  or  $\alpha_{\text{eff}} = \alpha_{\text{Q}}$ , while when spectral hardening occurs, the effective spectral index becomes smaller, i.e.  $\alpha_{\text{eff}} < \alpha_{\text{G}}$  or  $\alpha_{\text{eff}} < \alpha_{\text{Q}}$ .

From the energy conservation across the I-front, we obtain  $(3/2)k_B n_{gas}^{after} \Delta T_i \approx n_i^{before} \langle E_i \rangle$ , where  $\Delta T_i$  is the temperature jump across the I-front, and  $n_{gas}^{after} (n_i^{before})$  is the number density of gas of *i*th species after (before) the passage of the I-front.

<sup>&</sup>lt;sup>9</sup> We ignore the impact of secondary ionization for this estimate, although it is included in the simulations.



**Figure 14.** Spherically averaged temperature profiles around a QSO including only UV photons (QSO\_UV, blue dotted), UV and X-ray photons (QSO\_UVX, red dashed), UV and X-ray photon and secondary ionization (QSO\_UVXsec, black solid). The shaded regions indicate the  $1\sigma$  scatter around the mean.

The total temperature jumps ( $h\nu \rightarrow \infty$ ) across the H II, He II and He III I-fronts are then given by<sup>10</sup>

$$\Delta T_{\rm H\,{\scriptscriptstyle II}} = \frac{2}{3k_{\rm B}} \frac{\langle E_{\rm H\,{\scriptscriptstyle I}} \rangle}{2 + Y/X} \approx 5.0 \times 10^4 (2 + \alpha_{\rm eff})^{-1} \,\,{\rm K}, \tag{9}$$

$$\Delta T_{\rm He\,II} = \frac{2}{3k_{\rm B}} \frac{\langle E_{\rm He\,I} \rangle}{2(X/Y) + 2} \approx 7.6 \times 10^3 (1 + \alpha_{\rm eff})^{-1} \,\,\mathrm{K},\tag{10}$$

$$\Delta T_{\rm He\,III} = \frac{2}{3k_{\rm B}} \frac{\langle E_{\rm He\,II} \rangle}{2(X/Y) + 3} \approx 1.6 \times 10^4 (2 + \alpha_{\rm eff})^{-1} \,\,{\rm K}.$$
 (11)

Thus, the temperature jump after the passage of all the I-fronts is  $\approx 2.2 \times 10^4$  K for a QSO-type spectrum with  $\alpha_{eff} = 1.5$ , whereas  $\approx 1.5 \times 10^4 (1.2 \times 10^4)$  K for a galaxy-type spectrum with  $\alpha_{eff} = 3$  (without He II reionization). In this estimate, a QSO-type spectrum is expected to heat up the gas  $\sim 80$  per cent more effectively than a galaxy-type spectrum. This is somewhat larger than the difference found in our simulations. As shown in Section 4.2, neglecting secondary ionization, the temperature inside the QSO H II region becomes  $\sim 20000$  K. In addition, the cooling is neglected in the simplified argument. Taking into account these two factors, the above simple estimate explains, as a first approximation, the difference in the temperature seen in the simulations.

The above simplified argument demonstrates the physical origin of the temperature jump across the H II, He II and He III I-fronts, i.e. the energy conservation of spectral-weighted excess energy of photoelectrons across the I-fronts and the change of gas particle number. A harder spectrum more efficiently heats up the gas per ionization because the fraction of higher energy photons relative to photons near the ionization threshold is larger for a smaller spectral index.

### 4.2 Effect of X-rays and secondary ionization

Fig. 14 shows the spherically averaged profiles of temperature for three QSO only models including only UV photons (QSO\_UV), UV and X-ray photons neglecting secondary ionization (QSO\_UVX), and including it (QSO\_UVXsec). Compared to a UV only case in

<sup>10</sup> For this estimate, we have approximated the photoionization cross-sections of H<sub>I</sub>, He<sub>I</sub> and He<sub>II</sub> as power laws,  $\sigma_{H_1} \approx 6.3 \times 10^{-18} (\nu/\nu_{H_1})^{-3} \text{ cm}^2$ ,  $\sigma_{He_I} \approx 7.8 \times 10^{-18} (\nu/\nu_{He_I})^{-2} \text{ cm}^2$ ,  $\sigma_{He_{II}} \approx 1.6 \times 10^{-18} (\nu/\nu_{He_{II}})^{-3} \text{ cm}^2$ , respectively (Draine 2011).

which the temperature beyond the I-front drops to ~100 K, X-ray photons heat the gas to ~10<sup>3</sup> K. Including secondary ionization lowers the temperature by ~10 per cent because some of the excess energy of fast photoelectrons is diverted from heating to collisional ionization of hydrogen and helium. This effect is also clearly visible in the fully ionized region, at <10  $h^{-1}$  cMpc, where the temperature is reduced by ~20 per cent, from ~20 000 to ~17 000 K. Photoheating alone by X-ray photons, though, does not affect the temperature in the H II region, as it is set by the UV photons (as shown in Section 4.1.1).

Near the I-fronts at  $\sim 10-15 h^{-1}$  cMpc, the QSO model with secondary ionization shows a temperature higher than the model without it. This is related to the fact that our secondary ionization model pushes the I-front slightly outwards, i.e. the location of the photoionization heating by UV photons at the I-front is displaced. Therefore, secondary ionization indirectly increases the radius of the photoheated region.

In summary, X-ray photons heat the gas beyond the I-front because of their larger mean free path, but the inclusion of secondary ionization lowers the photoheating efficiency, because some of the excess energy of fast photoelectrons is diverted to collisional ionization of hydrogen and helium.

# 4.3 Thermal state induced by galaxies and a QSO in a pre-ionized IGM

If a QSO turns on in a medium ionized by pre-existing galaxies, the thermal state of the IGM is determined by the combined effect of both galaxies and the central QSO.

Fig. 15 shows temperature maps for galaxies only (GAL\_0.5R, GAL\_R, GAL\_2R) and galaxies+QSO (GAL\_0.5R+QSO\_UVXsec, GAL\_R+QSO\_UVXsec and GAL\_2R+QSO\_UVXsec) models, in which the QSO is turned on in a medium previously ionized by pre-existing galaxies. The green and blue solid (dotted) contours indicate the location of HII (HeIII) I-fronts due to galaxies and a QSO. As already noticed in Fig. 12, the thermal structure is traced by the position of the HII I-front due to the photoionization heating of hydrogen. Differently from a case in which reionization is driven by a QSO only (Section 4.1), pre-existing galaxies place the HII I-fronts further ahead of the QSO He III I-fronts. Thus, a large fraction of the thermal structure inside the HII region is determined by the pre-existing galaxies instead of the central QSO. The effect is more obvious as the total ionizing photon emissivity from galaxies increases. Similarly to what already noticed for the HII regions (Section 3.3), except for the pre-heating by X-rays from a QSO ahead of the HII I-front, the morphology and extent of the gas heated at  $\sim 10^4$  K are very similar in both galaxies only and galaxies+QSO models, as it is mainly determined by the UV photons emitted by galaxies.

In the following sections, we examine the thermal structure in more detail, focusing on the effect of galaxies and the additional heating by a QSO.

### 4.3.1 Heating by galaxies only

A galaxy-type spectrum contributes to the thermal structure of the IGM primarily by H<sub>I</sub> and He<sub>I</sub> photoionization heating. Fig. 16 shows the spherically averaged temperature profiles. Furthermore, in Fig. 17, the temperature–density diagram of H<sub>II</sub> (red) and H<sub>I</sub> (blue) regions shows that in galaxies only models (left three panels) the maximum temperature ( $\sim 2 \times 10^4$  K) depends weakly on the total ionizing photon emissivity, whereas the fraction of gas heated



**Figure 15.** Maps of temperature at z = 10 for galaxies only models GAL\_0.5R, GAL\_R, GAL\_2R, and galaxies+QSO models GAL\_0.5R+QSO\_UVXsec, GAL\_R+QSO\_UVXsec, GAL\_2R+QSO\_UVXsec. In both sets of models, galaxies start to reionize the IGM at z = 15, while the QSO is turned on at z = 10 for a duration of  $10^7$  yr in the medium already reionized by the pre-existing galaxies. The maps have a side length of  $50 h^{-1}$  cMpc and the width of the slice is  $195 h^{-1}$  ckpc. The galaxies' and QSO's H II (He III) I-front is shown as green and blue solid (dotted) contour, respectively. In the three rightmost panels, the H II I-fronts of the pre-existing galaxies are overlaid to aid the interpretation of the figure (see the text).



**Figure 16.** Spherically averaged temperature profiles of galaxies only models (top panel) GAL\_0.5R (blue dotted line), GAL\_R (black solid), GAL\_2R (red dashed), and galaxies+QSO models (bottom panel) GAL\_0.5R+QSO\_UVXsec (blue dotted), GAL\_R+QSO\_UVXsec (black solid), GAL\_2R+QSO\_UVXsec (red dashed). The shaded regions indicate the 1 $\sigma$  scatter around the mean.

close to the maximum temperature increases with total emissivity. This is because, for a fixed source spectrum, the heating rate per ionization is fixed (Section 4.1.1), and thus the heating efficiency remains the same regardless of the total ionizing photon production rate. When galaxies ionize the IGM gradually rather than in a short period of time (as discussed in Section 4.1), the H II temperature distribution is no longer isothermal as the gas engulfed earlier by the I-front has more time to cool. Furthermore, as the cooling time depends on the gas density, it is expected to vary according to location. This is clearly visible in the top panel of Fig. 16, where the spherically averaged temperature profiles of galaxies only models are plotted. Here, the temperature in the inner part of the H II region is lower than the gas temperature immediately behind the I-front,<sup>11</sup>

and the spread is large (see the difference in the spread in the temperature–density relation inside  $H \, \ensuremath{\Pi}$  regions shown in Figs 13 and 17).

On the other hand, the thermal structure in the neutral regions is nearly identical in all galaxies only models, as, similarly to Section 4.1, hydrodynamical processes, and not UV photons, are responsible for controlling the temperature in the neutral gas.

### 4.3.2 Heating by galaxies and a QSO

Fig. 15 shows that as the QSO increases the extent of the fully ionized region, the radius at which the gas is heated to  $\sim 10^4$  K is larger than in the corresponding galaxies only models. However, both the average profiles (Fig. 16) and the overall temperature–density relations (Fig. 17) are similar to those of the corresponding galaxies only models. This indicates that a QSO plays a small role in controlling the thermal state in the inner parts of the H II region, where the pre-existing galaxies have ionized the IGM before the QSO activity.

On the other hand, the top panels in Fig. 17 show that galaxies+QSO models reach temperatures that are typically higher than those in the corresponding galaxies only models. The differences become less evident with increasing ionizing emissivity from the galaxies (from left to right in the three rightmost panels). The reason for this is that when both the HII and HeIII I-fronts from the QSO are larger than the pre-existing HII region due to galaxies, the gas experiences the highest heating. However, when only the HII I-front from the QSO is larger than the pre-existing HII region (but the QSO He III I-front is still inside it), the portion of the gas 'newly' heated up by HI photoionization of a QSO has not yet undergone QSO-driven He II photoionization. This lack of He II photoionization by the QSO results in a slightly lower temperature. This non-linear heating process, which depends on the relative position of the various I-fronts, explains why QSO heating becomes less efficient with increasing contribution from galaxies.

This can be more clearly seen in Fig. 18, which shows differential maps of temperature between GAL\_R+QSO\_UVXsec and GAL\_R at two different QSO lifetimes. The solid (dotted) blue and green contours indicate the location of H II (He III) I-fronts produced by the QSO and the galaxies, respectively. The heating provided by the QSO in addition to the one by pre-existing galaxies is clearly associated with the positions of the various I-fronts. At  $t_Q = 10^7$  yr, the gas newly swept by the QSO H II I-front (between the blue solid and green solid contours) receives the highest temperature boost ( $\Delta T \sim 17000$  K, see Fig. 19), while the gas newly swept by the

<sup>&</sup>lt;sup>11</sup> Note that because photoionization of the residual neutral gas inside the  $H_{II}$  region can contribute to heating, the temperature towards the inner parts does not decrease monotonically.



**Figure 17.** Temperature–density diagram for galaxies only models GAL\_0.5R, GAL\_R, GAL\_2R and galaxies+QSO models GAL\_0.5R+QSO\_UVXsec, GAL\_R+QSO\_UVXsec, GAL\_2R+QSO\_UVXsec. The red (blue) colour indicates the H II (H I) regions defined as cells with  $x_{HII} \ge 0.5$  ( < 0.5). The contours are overlaid as a guide. To emphasize the temperature–density relation both in H II and H I regions, two different *y*-axis scales are used.



**Figure 18.** Differential temperature maps between models GAL\_R+QSO\_UVXsec and GAL\_R for QSO lifetimes of  $t_Q = 3 \times 10^6$  yr (left-hand panel) and  $t_Q = 10^7$  yr (right). The blue solid (dotted) contours indicate the location of the QSO's H II (He III) I-front, and the green solid (dotted) contours indicate the location of the H II (He III) I-front created by the pre-existing galaxies.

QSO He III I-front (between the blue dashed and green dashed contours) is additionally heated by  $\Delta T \sim 3000$  K (see Fig. 19). Note that at  $t_Q = 3 \times 10^6$  yr the radius of the QSO's He III region has not yet exceeded the radius of the HII region produced by the preexisting galaxies, so the gas between these two radii experiences a heating from the QSO of only  $\Delta T \sim 300$  K. At  $t_0 = 10^7$  yr, the QSO He III region has grown large enough to heat up all the H II gas already heated by the pre-existing galaxies. It is worth highlighting that, when a QSO shines in a region already reionized by galaxies, the temperature increment is mainly driven by HeII reionization, whereas outside the pre-existing H II region from galaxies the main contribution comes from H1 reionization by the central QSO. In general, the QSO heating is more effective where its radiation reaches the neutral gas, while photoionization of residual neutral gas in regions already ionized by pre-existing sources does not contribute substantially. Additionally, because of its harder spectrum, a QSO can heat gas more effectively than galaxies (by about a factor of  $\Delta T^{\rm QSO} / \Delta T^{\rm GAL} \approx [2 + \alpha_{\rm GAL}] / [2 + \alpha_{\rm QSO}] \approx 1.4$ ). As a result, the



**Figure 19.** Fraction of cells heated by  $\Delta T$  due to the QSO in GAL\_R+QSO\_UVXsec and QSO\_UVXsec models at  $t_Q = 10^7$  yr. The red solid (blue dotted) histogram refers to the distribution of the gas that has been swept by the H II + He II (He III) I-front. For a comparison, the black dashed histogram shows the distribution of the gas that has been swept by the H II + He II - front in the QSO only model QSO\_UVXsec. The two vertical lines are the analytic estimates given in Section 4.1.1.

gas swept *only* by the QSO's I-fronts can reach temperatures higher than the gas that has been pre-ionized by galaxies.

For a more quantitative analysis, Fig. 19 shows the fraction of gas heated by the passage of the QSO's H II and He III I-fronts. Because He I and H I reionization occur almost simultaneously (see Section 3.3), the position of the He II I-front is identical to that of the H II I-front. Their passage increases the temperature by  $\Delta T \sim 17000$  K. This is well captured by the analytic estimates in Section 4.1.1. The fraction of gas heated by the QSO's I-front in the galaxies+QSO and QSO only models is very similar. This is not surprising because the luminosity of the QSO is identical in the two models, and thus it can ionize and photoheat the same volume of gas, although with different geometry. On the other hand, the QSO's He III I-front increases the temperature by  $\sim$ 3000 K. Although this is somewhat lower than the simple analytic estimate, the results support the physical picture that the passage of the QSO's He III I-front is a substantial source of heating inside the pre-existing H II region.

Finally, similarly to the case of an unobscured QSO, when an obscured QSO is turned on, its X-ray photons preheat the neutral gas ahead of the I-fronts. In this case though, if the QSO dominates the ionization of the IGM, the thermal gradient near the I-front is expected to be smoother. However, if the surrounding galaxies have been ionizing the medium substantially, the thermal gradient remains sharp despite the presence of the obscured QSO.

In summary, the hydrogen and helium reionization driven by galaxies and QSOs has a non-linear impact on the gas thermal structure, which differs substantially from the one obtained in a simpler reionization model driven by galaxies or QSOs only. The relative position of the H II I-front of galaxies and the H II/He III I-fronts of the QSO determines the thermal structure of the IGM. In general, higher temperatures can be achieved if the gas is heated *only* by QSOs, while when the gas has been ionized by pre-existing galaxies, the QSO heating is less efficient. The order of the H II and He II/He III I-fronts is discussed in Appendix C for interested readers.

# 5 DOES THE QSO IMPRINT UNIQUE FEATURES ON ΗΠ REGIONS?

One of the outstanding questions regarding the role of QSOs during reionization is whether they leave distinctive features in the structure of H  $\producture$  regions. The answer to this depends on (i) the relative number of the ionizing photons emitted by a QSO and galaxies since the onset of reionization, and (ii) the spectrum of the QSO.

As a QSO is likely born in a region overdense in galaxies (e.g. Yu & Lu 2005; Alvarez & Abel 2007; Lidz et al. 2007; Geil & Wyithe 2008), while the QSO dominates the local photon emissivity during its activity, galaxies contribute to the ionizing budget for a longer time, and thus the structure of HII regions is determined by the relative importance of the two contributions (see discussion in Section 3.3.1, but also Lidz et al. 2007 and Datta et al. 2012). When the total ionizing budget from a QSO dominates over that of the surrounding galaxies since the onset of reionization, the local environment is more strongly affected by the QSO and the resulting HII region is more spherical than those obtained when galaxies are more relevant. This limit corresponds to the scenarios considered by Thomas & Zaroubi (2008) and Feng et al. (2013), and our models discussed in Section 3.1. A consequence of this argument is that a QSO can more easily imprint a distinctive H II region at earlier than later times because of a smaller cumulative contribution from galaxies (Geil & Wyithe 2008). On the other hand, in Lidz et al. (2007), Datta et al. (2012) and our galaxies+QSO models, the contribution from galaxies is more important. In this case, a QSO does not change drastically the morphology of the H II region, although it enhances its sphericity by a degree increasing with the ionizing photon production rate of the QSO.

The sphericity of the H $\mbox{II}$  region is, however, broken when (i) the QSO I-front merges with H $\mbox{II}$  regions of galaxies (e.g. Feng et al. 2013), (ii) the QSO I-front encounters high-density neutral gas, e.g. Lyman-limit systems, which casts shadows (see Sections 3.1, 3.3 and Keating et al. 2015), and (iii) a QSO shines anisotropically. In other words, the degree of sphericity is

influenced by both the QSO–galaxy and QSO–absorber clustering (Keating et al. 2015), and by a beamed emission, which might serve as another indicator of the QSO presence.

The spectrum of a QSO plays a pivotal role in determining the morphology of HII regions. By studying QSO models with UV-obscured and unobscured spectra, previous works (Zaroubi & Silk 2005; Kramer & Haiman 2008; Thomas & Zaroubi 2008) concluded that an obscured QSO spectrum produces a wide I-front. Thus, as a QSO spectrum becomes more UV-obscured and harder, it can imprint a distinctive ionization structure, providing smoother and more extended I-fronts, and more spherical H II regions. On the other hand, an unobscured QSO emitting UV photons renders the I-front more similar to one by galaxies. Our results are consistent with this picture, but add another ingredient. Although for a single LOS, a harder and UV-obscured spectrum thickens the I-front, large fluctuations in the I-front position are observed in many LOSs. Therefore, in order for the thickness of the I-front to be used as an indicator of the source type, it must exceed the scatter observed along the LOSs. In addition, the soft X-ray photon budget from the QSO must dominate the UV photon contribution from pre-existing galaxies in order for an obscured QSO to imprint a distinctive morphology on the HII region.

In summary, a QSO leaves a distinctive imprint on an ionized region in terms of its sphericity and the thickness of the I-front when the QSO has a hard UV-obscured spectrum and/or when its contribution to the total ionizing photon budget in its local environment dominates the one from galaxies since the onset of reionization. If instead the QSO spectrum is not obscured and the ionizing photon budget of the local galaxies is comparable to or larger than the one of the QSO, no obvious features would appear in the H $\,II$  region to indicate the presence of a QSO. In conclusion, a large quasispherical H $\,II$  region at high redshift is not necessarily associated with the presence of a QSO.

### **6 OBSERVATIONAL IMPLICATIONS**

A natural question is whether observations can be envisioned in order to provide information about the role of galaxies and QSOs in driving reionization.

Tomography of the 21 cm line from neutral hydrogen can directly image the morphology of HII regions during reionization (see the reviews by Furlanetto, Oh & Briggs 2006; Morales & Wyithe 2010; Mellema et al. 2013). Although the structure of a QSO H II region should appear as a coldspot in a 21 cm image and provides information about the ionizing sources (Madau, Meiksin & Rees 1997; Tozzi et al. 2000; Wyithe & Loeb 2004; Kramer & Haiman 2008; Thomas & Zaroubi 2008; Datta, Friedrich & Mellema 2012), as emphasized in this work, the morphology of HII regions in high-z QSO environments is complicated by the contribution of the surrounding galaxies and the spectral shape of the QSO. This implies that some degeneracy will remain when trying to constrain the properties of ionizing sources using 21 cm data alone. We note that the appearance of H II regions as coldspots depends on the surrounding thermal structure. We investigate this topic more in detail in a forthcoming paper.

Galaxy surveys in the direction of coldspots in 21 cm images can provide important complementary information (Beardsley et al. 2015). This strategy can be realized, for example, in ELAIS-N1 field targeted by LOFAR (Jelić et al. 2014) and Subaru/Hyper-SuprimeCam Survey.<sup>12</sup> Alternatively, 21 cm images can be formed in the direction of high-redshift QSOs after they are found by galaxy surveys. Ongoing wide-field surveys such as Dark Energy Survey and Subaru/Hyper-SuprimeCam Survey are expected to provide ~10 new QSOs at z ~ 7 (Reed et al. 2015; Matsuoka et al. 2016). This approach would allow us to directly infer the expected ionizing photon counts emitted from galaxies using surveys, together with their impact on the morphology (e.g. size) of their H II regions (coldspots) using 21 cm tomography. Therefore, this directly probes whether the estimated ionizing photon counts of galaxies and QSOs are sufficient to create the observed size of the H II region harbouring the sources. This strategy is arguably the most direct test of the sources of reionization.

An alternative strategy, which could already be realized with current observational facilities, is to perform a galaxy survey in regions around high-redshift QSOs, while the properties of the ionizing sources would be directly studied using the photometric/spectroscopic data from the surveys, the physical state of the IGM would be inferred from Ly  $\alpha$  absorption in the QSO spectra. Observing the ionizing photon production rate and the escape fractions of high-redshift galaxies and QSOs alone does not immediately imply that they are drivers of reionization, as they may be shining in a region already reionized by other sources. As demonstrated in our work, investigating the impact of galaxies and QSOs (as traced by a galaxy survey) on the ionization and thermal states of the IGM (as traced by e.g. QSO near-zone and Ly  $\alpha$  absorption line widths) would provide important complementary information about how the sources have driven reionization. For example, Ciardi et al. (2012) used the temperature measurement in the local environment of  $z \sim 6$  QSOs by Bolton et al. (2010) to derive constraints on the ionizing sources. Also, spectroscopic observations of QSOs along He II Ly  $\alpha$  forests have proven to be very insightful to understand the relation between QSOs and the IGM for HeII reionization at  $z \sim 2-3$  (Jakobsen et al. 2003; Syphers & Shull 2013, 2014).

Furthermore, re-examining the proximity zone of ULAS J1120+0641  $z \approx 7$  QSO (Mortlock et al. 2011) in view of our results will be interesting. Previous work (Bolton et al. 2011; Keating et al. 2015) did not explicitly include the contribution of galaxies in modelling the proximity zone. Instead, they explored various volume-averaged neutral fractions around the QSO to explain the observed proximity zone effect and concluded that a volumeaveraged neutral fraction of the IGM of  $\sim 10^{-3}$  to  $10^{-4}$  is required to match the observation. Although at z = 10, in our model we find that a residual neutral fraction of  $\sim 10^{-3}$  can be produced by the contribution of galaxies within the H II region hosting the QSO,<sup>13</sup> but otherwise the IGM is highly neutral. In this picture, the proximity zone effect of a QSO is determined both by the QSO itself and the surrounding galaxies. And the observed proximity zone is caused by the locally enhanced UV background by the QSO inside the large H II region that is collectively created with galaxies. Simpson et al. (2014) searched galaxies around ULAS J1120+0641. Spectroscopic follow-up of the dropout galaxies in the ULAS J1120+0641 QSO field and the interpretation using an RT simulation suite similar to those presented in this paper should constrain the role of galaxies and QSOs during the reionization era.

### 7 CONCLUSIONS

We have presented a detailed analysis of hydrogen and helium reionization scenarios in high-z QSO environments including both galaxies and a central QSO using a suite of cosmological multifrequency RT simulations. This allows us to understand the array of physical mechanisms that shape the ionization and thermal states of the IGM. We find the following:

(i) If the integrated number of ionizing photons emitted by the surrounding galaxies since the onset of reionization exceeds or is comparable to that emitted by the QSOs during its active phase, the morphology of the H  $\pi$  regions in galaxies only and galaxies+QSO models is similar. On the other hand, if the ionization budget is dominated by the QSO, distinctive features can be observed in the H  $\pi$  region.

(ii) The hard spectrum of the QSO always leaves a unique signature in the morphology of the He II and He III regions.

(iii) Soft X-ray photons from the QSOs produce extended partially ionized tails of hydrogen and helium around the central H  $\scriptstyle II$  and He II/He III regions. Ionization from secondary electrons enhances the contribution of photoionization by X-rays in the partially ionized tail. On the other hand, neither the morphology of the fully ionized regions nor the thickness of the I-fronts is sensitive to the X-ray photons.

(iv) UV-obscured QSOs can broaden the I-fronts significantly. A noticeable change in the ionization morphology occurs when soft X-ray photons (from the QSO), rather than UV photons, dominate the growth of I-fronts.

(v) The thermal state of the IGM is strongly affected in a complex, non-linear, way by photoionization heating of both hydrogen and helium. A larger number of total ionizing photons do not necessarily increase the gas temperature. The highest temperature is attained in the region ionized only by the QSO, as the gas temperature is primarily determined by the spectral type of the sources that first ionized the medium.

(vi) The X-ray photons from the QSO heat the partially ionized gas ahead of the I-fronts to  $T \sim 10^3$  K. The net X-ray heating is slightly reduced when secondary ionization is included because it adds another channel to deposit the energy into ionization. The X-ray pre-heating is a clean signature of QSO activity.

In summary, in the environment surrounding a high-z QSO, the physical state of the IGM in terms of hydrogen and helium reionization as well as gas temperature is determined by a complex and non-linear interplay of the galaxies and the QSO. This picture emphasizes the importance of correctly modelling hydrogen, helium and temperature evolution with a multifrequency treatment of the RT in 3D numerical simulations. The large suite of multifrequency RT simulations presented here provides a highly valuable theoretical resource to understand the physical mechanisms responsible for shaping the ionization and thermal structures of the IGM. This will facilitate the use of RT simulations in interpreting QSO spectra and upcoming 21 cm observations to better understand the role of galaxies and QSOs in driving reionization.

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<sup>12</sup> http://www.naoj.org/Projects/HSC/surveyplan.html

<sup>&</sup>lt;sup>13</sup> In this respect, the  $f_{H_1} = 0.02$  model of Keating et al. (2015, see their figs 3 and 6) roughly corresponds to our galaxies+QSO model.

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# **APPENDIX A: CONVERGENCE TEST**

We have tested the convergence of our results by increasing the number of photon packets emitted by the QSO from  $2 \times 10^8$  to  $10^9$ . The spherically averaged profiles of the ionized fractions and temperature are plotted in Fig. A1, and show that, while the number of photon packets is increased by a factor of 5, the resulting profiles are the same for the ionized fractions and differ for the temperature by 5 per cent at most in the partially ionized tail. In Fig. A2, maps of H II, He II and He III fractions are shown for the two cases. Although increasing the number of photon packets emitted produces a slightly smoother tail at a distance of  $\sim 20 h^{-1}$  cMpc from the centre, it is clear that the main fluctuations are not produced by a poor convergence of the Monte Carlo method but rather by shadowing of dense clumps. We thus use  $2 \times 10^8$  photon packets as default value for all our simulations.



**Figure A1.** Spherically averaged profiles of H II (red lines), He II (blue) and He III (green) fractions (top panel), and of the temperature (bottom panel) for model QSO\_UVXsec. The line style refers to  $2 \times 10^8$  (dashed lines) and  $10^9$  (solid) photon packets emitted by the central QSO.



**Figure A2.** Maps of H II (top panels), He II (middle) and He III (bottom) fractions for model QSO\_UVXsec, where the number of photon packets emitted by the central QSO is  $2 \times 10^8$  (left-hand panels) and  $10^9$  (right). The total length of the *x*- and *y*-axes is  $50 h^{-1}$  cMpc.



**Figure B1.** Halo merger time-scale and recombination time-scale as a function of the mass of the secondary halo,  $M_{\rm h, sec}$ , merging with the halo hosting a QSO. The latter has a mass  $M_{\rm h, host} = 10^{12} \,\mathrm{M_{\odot}}$  (dashed line) or  $10^{13} \,\mathrm{M_{\odot}}$  (solid). The horizontal solid and dot–dashed lines are the recombination time-scale of hydrogen and helium obtained for a clumping factor C = 3. A different value of *C* results in a linear upward/downward shift of the horizontal lines.

### APPENDIX B: EFFECT OF QSO DUTY CYCLE

We investigate the impact of the QSO duty cycle on reionization using an analytic argument, as it allows us to scan a large parameter space. Although we have run a simulation including previous activity of the QSO, because the mechanisms triggering it are not fully understood at high redshift, we defer to future work a more extensive numerical investigation. In this argument, we exclude the effect of galaxies.

The build-up of a black hole driving the QSO activity requires  $t = t_{\rm Edd} \ln(M_{\rm BH}/M_{\rm seed}) \sim 5 \times 10^7$  yr, with a seed mass of  $M_{\rm seed} = 10^{2-5}$  M<sub> $\odot$ </sub> and  $t_{\rm Edd} = 4 \times 10^7$  yr (e.g. Loeb & Furlanetto 2013). A QSO-host galaxy may thus have experienced multiple episodes of QSO activity (our fiducial QSO lifetime  $t_{\rm Q} = 10^7$  yr is smaller than the time-scale to build up an SMBH).

As a first approximation, if the duration of the QSO-quiet phase,  $t_{quiet}$ , is shorter than the recombination time-scale of the *i*th species i = H II, He III at mean density, i.e.  $t_{quiet} < \bar{t}_{rec,i}$ , the IGM remains ionized (fossil H II and He III regions) during the QSO-quiet phase (Furlanetto, Haiman & Oh 2008; Thomas & Zaroubi 2008). In this case, during the next active phase, the QSO turns on in a fossil ionized region, which should thus be taken into account. On the other hand, if  $t_{quiet} > \bar{t}_{rec,i}$ , the IGM recombines and becomes neutral before the next QSO phase, then the QSO must ionize again a fully neutral IGM. In this limit, only the phase of QSO activity at the redshift of interest contributes to reionization.

Assuming that the QSO activity is triggered by merger events of dark matter haloes (e.g. Hopkins et al. 2006),  $t_{quiet}$  is expected to be of the order of the halo merger time-scale. This can be estimated from the extended Press–Schechter approach (Lacey & Cole 1993) as the inverse of the halo merger rate at z = 10. Fig. B1 shows the QSO-quiet phase time-scale for a host with halo mass  $M_{h, host}$  merging with a secondary halo of mass  $M_{h, sec}$ , together with the recombination time-scales.<sup>14</sup> The figure suggests that to keep the

<sup>14</sup> The recombination time-scales are calculated as  $\bar{t}_{\text{rec},\text{H II}} = [\alpha_{\text{B},\text{H II}}\bar{n}_{\text{H}}(z)C]^{-1}$  and  $\bar{t}_{\text{rec},\text{H e III}} = [\alpha_{\text{B},\text{H e III}}\bar{n}_{\text{He}}(z)C]^{-1}$ , where *C* is the clumping factor.

hydrogen ionized (i.e.  $t_{quiet} < \bar{t}_{rec,H\,II}$ ), the QSO needs to be fed by minor mergers with halo of mass  $M_{h,sec} \lesssim 10^{10}(10^{11}) \,\mathrm{M_{\odot}}$  for  $M_{h,host} = 10^{12}(10^{13}) \,\mathrm{M_{\odot}}$ ; otherwise, the QSO H II region can recombine before the next phase of QSO activity. Because of the shorter recombination time-scale of helium, a QSO should be fed even more vigorously to maintain an He III region fully ionized (Bolton et al. 2012).

In summary, while in general the duty cycle of a QSO affects the ionization of the surrounding medium, its impact is controlled by the ratio between the time-scale of the QSO activity and the recombination time-scale. QSO-driven H II regions at z > 6 can survive when the QSOs are fuelled by frequent minor mergers. On the other hand, if the QSOs are fuelled by less frequent major mergers, the ionized gas has enough time to recombine before the next activity phase, during which the QSOs needs to carve a new H II region. In this case, the contribution of QSOs to reionization is less significant. Because of the shorter recombination time-scales of helium, the continuous fuelling of QSOs must occur even more vigorously to sustain full helium reionization.

# APPENDIX C: ORDER OF HII, HeII AND HeIII I-FRONTS

The relative position of H II and He II/He III I-fronts essentially determines the morphology and timing of hydrogen and helium reionizations. Interestingly, it depends on the type of ionizing sources, and for a very hard spectrum the I-front of helium can even precede the H I I-front (Tittley & Meiksin 2007; Shull et al. 2010).

This is well illustrated with the classical equation of cosmological I-front (see also Section 3.3.1). The relative position of H  $\pi$  and He  $\pi$  I-fronts of a QSO is

$$\frac{R_{I,QSO}^{\text{He III}}}{R_{I,QSO}^{\text{H I III}}} = \left(\frac{X}{Y}\right)^{1/3} \left(\frac{\nu_{\text{H I}}}{\nu_{\text{He III}}}\right)^{\alpha_Q/3}.$$
(C1)

This argument suggests that the He III I-front may be ahead of the HI I-front if the spectral index is  $\alpha_Q < 1.8$ . It is, however, an oversimplification and in fact it does not work in our simulations. The analysis in Section 3.4 suggests that a peculiar case in which the He II I-front proceeds ahead of the H II I-front requires an even harder spectrum. Although the He III I-front in the obscured QSO model follows more closely the H II I-front, we does not see any obvious sign of the inversion (but see Thomas & Zaroubi 2008). The order of H II, He II/He III I-fronts is an interesting, but not fully investigated topic. Note that this can have an impact on the thermal structure of the IGM because of the different photoionization heating across each I-front. Thus, this issue should be more thoroughly studied to fully understand the concerted hydrogen and helium reionization scenario in the QSO environment.

This paper has been typeset from a  $T_{\ensuremath{E}} X/I\!\!\! \mbox{\ensuremath{\Delta}} T_{\ensuremath{E}} X$  file prepared by the author.